

R Textbook Companion for  
Statistics for Business and Economics  
by Anderson, Sweeney and Williams<sup>1</sup>

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# **Book Description**

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R numbering policy used in this document and the relation to the above book.

**Exa** Example (Solved example)

**Eqn** Equation (Particular equation of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means an R code whose theory is explained in Section 2.3 of the book.

# Contents

<b>List of R Codes</b>	<b>4</b>
<b>2 Descriptive Statistics Tabular and Graphical Presentations</b>	<b>5</b>
<b>3 Descriptive Statistics Numerical Measures</b>	<b>16</b>
<b>4 Introduction to Probability</b>	<b>26</b>
<b>5 Discrete Probability Distribution</b>	<b>36</b>
<b>6 Continuous Probability Distribution</b>	<b>45</b>
<b>7 Sampling and Sampling Distribution</b>	<b>50</b>
<b>8 Interval Estimation</b>	<b>58</b>
<b>9 Hypothesis Testing</b>	<b>64</b>
<b>10 Inference About Means and Proportions With Two Populations</b>	<b>74</b>
<b>11 Inferences About Population Variances</b>	<b>83</b>
<b>12 Tests of Goodness of Fit and Independence</b>	<b>89</b>
<b>13 Experimental Design and Analysis of Variance</b>	<b>96</b>
<b>14 Simple Linear Regression</b>	<b>107</b>
<b>15 Multiple Regression</b>	<b>118</b>

<b>16</b>	<b>Regression Analysis Model Building</b>	<b>131</b>
<b>17</b>	<b>Index Numbers</b>	<b>142</b>
<b>18</b>	<b>Time Series Analysis and Forecasting</b>	<b>147</b>
<b>19</b>	<b>Non Parametric Tests</b>	<b>168</b>
<b>20</b>	<b>Statistical Process Control</b>	<b>175</b>
<b>21</b>	<b>Decision Analysis</b>	<b>178</b>

# List of R Codes

Exa 2.1a	Summarizing Categorical Data Part 1 . . . . .	5
Exa 2.1b	Summarizing Categorical Data Part 2 . . . . .	7
Exa 2.2a	Summarizing Quantitative Data . . . . .	9
Exa 2.3a	Scatter Plot and Tradeline . . . . .	11
Exa 2.4a	Cumulative Distributions . . . . .	13
Exa 2.5a	Exploratory Data Analysis The Stem and Leaf Display	14
Exa 3.1a	Measures of Location Mean Part 1 . . . . .	16
Exa 3.1b	Measures of Location Mean Part 2 . . . . .	16
Exa 3.1c	Measures of Location Median Part 1 . . . . .	17
Exa 3.1d	Measures of Location Median Part 2 . . . . .	17
Exa 3.1e	Measures of Location Percentiles and Quartiles . . . . .	18
Exa 3.2a	Measures of Variability Range and IQR . . . . .	19
Exa 3.2b	Measures of Variability Variance . . . . .	20
Exa 3.2c	Measures of Variability Standard Deviation . . . . .	20
Exa 3.3a	Z Score . . . . .	21
Exa 3.4a	Boxplot . . . . .	21
Exa 3.5a	Covariance and Correlation Coefficient . . . . .	22
Exa 3.5b	Sample Correlation Coefficient . . . . .	23
Exa 3.6a	Weighted Mean . . . . .	23
Exa 3.6b	Grouped Data Mean and Sample Variance . . . . .	24
Exa 4.1a	Combinations . . . . .	26
Exa 4.1b	Permutations . . . . .	27
Exa 4.1c	Assigning Probabilities . . . . .	27
Exa 4.1d	Probabilities Assigning Example . . . . .	28
Exa 4.2a	Probability of an Event . . . . .	29
Exa 4.3a	Probability Computation using Complement . . . . .	30
Exa 4.3b	Intersection and Union of Events . . . . .	30
Exa 4.3c	Addition Law . . . . .	31

Exa 4.4a	Conditional Probability . . . . .	32
Exa 4.4b	Multiplication Law . . . . .	33
Exa 4.5a	Bayes Theorem Tabular Approach . . . . .	34
Exa 5.1a	Discrete Probability Distribution Graph Expected value Variance and Standard Deviation . . . . .	36
Exa 5.2a	Binomial Probability Distribution . . . . .	37
Exa 5.2b	Binomial Probability Distribution Eg2 . . . . .	38
Exa 5.3a	Poisson Probability Distribution . . . . .	41
Exa 5.4a	Hypergeometric Probability Distribution . . . . .	42
Exa 5.5a	Expected Value and Variance . . . . .	43
Exa 6.1a	Uniform Probability Distribution . . . . .	45
Exa 6.2a	Normal Probability Distribution . . . . .	46
Exa 6.3a	Normal Approximation of Binomial Probabilities . . . . .	47
Exa 6.4a	Exponential Probability Distribution . . . . .	48
Exa 7.1a	Point Estimator . . . . .	50
Exa 7.2a	Sampling Distribution . . . . .	51
Exa 7.3a	Sampling Distribution of Sample Mean . . . . .	52
Exa 7.3b	Relationship between Sample Size and Sampling Distribution of xbar . . . . .	53
Exa 7.4a	Sampling Distribution of Sample Proportion . . . . .	54
Exa 7.4b	Practical value of the Sampling Distribution of Sample Proportion . . . . .	55
Exa 7.4c	Practical value of the Sampling Distribution of Sample Proportion Eg2 . . . . .	56
Exa 8.1a	Population Mean Sigma Known . . . . .	58
Exa 8.2a	Population Mean Sigma Unknown . . . . .	59
Exa 8.2b	Population Mean Sigma Unknown Eg2 . . . . .	60
Exa 8.3a	Determining the Sample Size . . . . .	61
Exa 8.4a	Population Proportion . . . . .	61
Exa 8.4b	Determining the Sample Size . . . . .	62
Exa 9.1a	Population Mean Sigma Known One Tailed Test . . . . .	64
Exa 9.1b	Population Mean Sigma Known Two Tailed Test . . . . .	65
Exa 9.1c	Relationship between Interval Estimation and Hypothesis Testing . . . . .	67
Exa 9.2a	Population Mean Sigma Unknown One Tailed Test . . . . .	68
Exa 9.2b	Population Mean Sigma Unknown Two Tailed Test . . . . .	69
Exa 9.3a	Population Proportion . . . . .	70
Exa 9.4a	Calculating the Probability of Type Second Errors . . . . .	72

Exa 9.5a	Determining the Sample Size . . . . .	73
Exa 10.1a	Inference about the Difference between the two Population Means Sigma 1 and Sigma 2 known . . . . .	74
Exa 10.1b	Hypothesis Tests About Difference between two Means . . . . .	75
Exa 10.2a	Inference about the Difference between the two Population Means Sigma 1 and Sigma 2 Unknown . . . . .	76
Exa 10.2b	Hypothesis Tests About Difference between two Means . . . . .	77
Exa 10.3a	Inference About the Difference Between Two Population Means Matched samples . . . . .	78
Exa 10.4a	Inference About the Difference Between Two Population Proportions . . . . .	80
Exa 10.4b	Hypothesis Tests About Difference between two Proportions . . . . .	81
Exa 11.1a	Inferences About Population Variance . . . . .	83
Exa 11.1b	Hypothesis Testing . . . . .	84
Exa 11.2a	Inferences About Two Population Variances . . . . .	86
Exa 12.1a	Goodness of Fit Test A Multinomial Population . . . . .	89
Exa 12.2a	Tests of Independence . . . . .	90
Exa 12.3a	Goodness of Fit Test Poisson Distribution . . . . .	91
Exa 12.3b	Goodness of Fit Test Normal Distribution . . . . .	93
Exa 13.1a	Analysis of Variance and the Completely Randomized Design . . . . .	96
Exa 13.2a	Analysis of Variance and the Completely Randomized Design . . . . .	98
Exa 13.3a	Multiple Comparison Procedures Fishers LSD . . . . .	99
Exa 13.4a	Randomized Block Design . . . . .	102
Exa 13.5a	Factorial Design . . . . .	104
Exa 14.1a	Least Squares Method . . . . .	107
Exa 14.2a	Coefficient of Determination . . . . .	108
Exa 14.3a	Test of Significance . . . . .	110
Exa 14.4a	Using the Estimated Regression Equation for Estimation and Prediction . . . . .	112
Exa 14.5a	Residual Analysis Validating Model Assumptions . . . . .	113
Exa 14.5b	Standardized Residuals . . . . .	114
Exa 14.6a	Detecting Outliers . . . . .	116
Exa 14.6b	Detecting Influential Observations . . . . .	116
Exa 15.1a	Least Squares Method . . . . .	118
Exa 15.2a	Two Independent Variables . . . . .	120

Exa 15.3a	Multiple Coefficient of Determination . . . . .	120
Exa 15.4a	Testing of significance . . . . .	122
Exa 15.5a	Categorical Independent Variables . . . . .	125
Exa 15.6a	Residual Analysis . . . . .	126
Exa 15.6b	Influential Observations . . . . .	128
Exa 15.7a	Logistic Regression . . . . .	129
Exa 16.1a	General Linear Model . . . . .	131
Exa 16.1b	Interaction . . . . .	133
Exa 16.1c	Transformations Involving the Dependent Variables . . . . .	135
Exa 16.2a	Analysis of a Large Problem . . . . .	138
Exa 16.3a	Multiple Regression Approach to Experimental Design	140
Exa 17.1a	Price Relatives . . . . .	142
Exa 17.2a	Aggregate Price Indexes . . . . .	143
Exa 17.3a	Computing an Aggregate Price Index from Price Relatives . . . . .	144
Exa 17.4a	Deflating a Series by Price Indexes . . . . .	145
Exa 18.1a	Time Series Patterns . . . . .	147
Exa 18.1b	Time Series Patterns Eg2 . . . . .	148
Exa 18.1c	Time Series Patterns Eg3 . . . . .	149
Exa 18.1d	Time Series Patterns Eg4 . . . . .	149
Exa 18.1e	Time Series Patterns Eg5 . . . . .	150
Exa 18.1f	Time Series Patterns Eg6 . . . . .	151
Exa 18.2a	Forecast Accuracy . . . . .	152
Exa 18.3a	Moving Averages . . . . .	155
Exa 18.3b	Exponential Smoothing . . . . .	157
Exa 18.4a	Trend Projection . . . . .	158
Exa 18.4b	Trend Projection Part2 . . . . .	159
Exa 18.4c	Nonlinear Trend Regression . . . . .	160
Exa 18.5a	Seasonality Without Trend . . . . .	161
Exa 18.5b	Seasonality and Trend . . . . .	163
Exa 18.6a	Time Series Decomposition . . . . .	164
Exa 18.6b	Deseasonalizing the Time Series . . . . .	165
Exa 19.1a	Rank Correlation . . . . .	168
Exa 19.2a	Sign Test . . . . .	169
Exa 19.3a	Wilcoxon Signed Rank Test . . . . .	171
Exa 19.4a	Mann Whitney Wilcoxon Test . . . . .	172
Exa 19.4b	Mann Whitney Wilcoxon Test Eg2 . . . . .	173
Exa 19.5a	Kruskal Wallis Test . . . . .	173

Exa 20.1a Sample Mean Chart Process Mean and SD Unknown .	175
Exa 21.1a Problem Formulation . . . . .	178

# Chapter 2

## Descriptive Statistics Tabular and Graphical Presentations

**R code Exa 2.1a** Summarizing Categorical Data Part 1

```
1 # Page no. :  
2 33  
3 # Frequency Distribution (Categorical Data)  
4  
5 # Dataset  
6  
7 soft_drink_names <- c("Coke Classic", "Diet Coke", "  
8     Pepsi", "Diet Coke", "Coke Classic", "Coke Classic  
9     ",  
10    "Dr. Pepper", "Diet Coke", "  
11    Pepsi", "Pepsi", "Coke  
12    Classic", "Dr. Pepper",  
13    "Sprite", "Coke Classic", "Diet  
14    Coke", "Coke Classic", "  
15    Coke Classic", "Sprite",  
16    "Coke Classic", "Diet Coke", "  
17    Coke Classic", "Diet Coke",  
18    "Coke Classic", "Sprite",
```

```

11      "Pepsi", "Coke Classic", "Coke
12          Classic", "Coke Classic", "
13              Pepsi", "Coke Classic",
14      "Sprite", "Dr. Pepper", "Pepsi"
15          , "Diet Coke", "Pepsi", "
16              Coke Classic",
17      "Coke Classic", "Coke Classic",
18          "Pepsi", "Dr. Pepper", "
19              Coke Classic", "Diet Coke",
20      "Pepsi", "Pepsi", "Pepsi", "
21          Pepsi", "Coke Classic", "Dr.
22              Pepper", "Pepsi", "Sprite")
23
24 soft_drink_table <- data.frame(table(soft_drink_
25     names))
26
27                                     # Page no. : 34
28
29 FD <- data.frame(Soft_drinks = soft_drink_table$soft
30     _drink_names,
31             Frequency = soft_drink_table$Freq)
32
33                                     # Frequency Distribution
34
35 RF <- FD$Frequency / sum(FD$Frequency)    # Relative
36     Frequency
37
38 FD <- cbind(FD,Relative_frequency = RF)
39
40 PF <- FD$Relative_frequency * 100    # Percentage
41     Frequency
42
43 FD <- cbind(FD, Percentage_frequency = PF)
44
45 View(FD)    # Viewing the Frequency Distribution
46     Table
47
48 # Total values of Frequency Distribution

```

```
35
36 total_freq <- sum(FD$Frequency)
37
38 total_rel_freq <- sum(FD$Relative_frequency)
39
40 total_per_freq <- sum(FD$Percentage_frequency)
41
42 cat("Total value for frequency is", total_freq, "\n")
43 cat("Total value for relative frequency is", total_
      rel_freq, "\n")
44 cat("Total value for percentage frequency is", total_
      per_freq)
```

---

### R code Exa 2.1b Summarizing Categorical Data Part 2

```
1 # Page no. :
      35
2
3 # Bar Charts and Pie Charts
4
5 # Dataset
6
7 soft_drink_names <- c("Coke Classic", "Diet Coke", "
      Pepsi", "Diet Coke", "Coke Classic", "Coke Classic"
      ,
      "Dr. Pepper", "Diet Coke", "
      Pepsi", "Pepsi", "Coke
      Classic", "Dr. Pepper",
      "Sprite", "Coke Classic", "
      Diet Coke", "Coke Classic",
      "Coke Classic", "Sprite",
      "Coke Classic", "Diet Coke",
      "Coke Classic", "Diet Coke",
      "Coke Classic", "Sprite",
```

```

11      "Pepsi", "Coke Classic", "Coke
12          Classic", "Coke Classic",
13          "Pepsi", "Coke Classic",
14      "Sprite", "Dr. Pepper", "Pepsi"
15          ", "Diet Coke", "Pepsi", "
16          Coke Classic",
17      "Coke Classic", "Coke Classic"
18          , "Pepsi", "Dr. Pepper", "
19          Coke Classic", "Diet Coke",
20      "Pepsi", "Pepsi", "Pepsi", "
21          Pepsi", "Coke Classic", "Dr
22          . Pepper", "Pepsi", "Sprite
23      ")
24
25
26 # Bar Chart
27
28 ggplot(soft_drink_table,aes(soft_drink_names,Freq,
29     fill = soft_drink_names))+geom_bar(stat =
30         "identity")+
31     labs(title="Bar chart" , x = "Soft Drink", y =
32         "Frequency")+ylim(0,20)
33
34 # Pie Chart
35
36 soft_drink_purchase_slices <- soft_drink_table$Freq
37 soft_drink_names_labels <- soft_drink_table$soft_
38     drink_names

```

```

35 soft_drink_purchase_pct <- (soft_drink_table$Freq/
      sum(soft_drink_table$Freq)) * 100
36
37 soft_drink_names_labels <- paste(soft_drink_names_
      labels,soft_drink_purchase_pct)
38 soft_drink_names_labels <- paste(soft_drink_names_
      labels, "%", sep = "")
39
40 pie(soft_drink_purchase_slices, labels = soft_drink_
      names_labels,
41       col = rainbow(length(soft_drink_names_labels)),
42       main = "Pie Chart for Soft Drink Purchase")

```

---

### R code Exa 2.2a Summarizing Quantitative Data

```

1                                     # Page no. :
39-40
2
3 # Frequency Distribution (Quantitative Data)
4
5 audit_data <- c
6   (12,15,20,22,14,14,15,27,21,18,19,18,22,33,16,18,17,23,28,13)
7
8
9 width <- (max(audit_data) - min(audit_data)) / no_of_
10 _classes
11 width <- ceiling(width)    # Rounding up of the value
12
13 breaks <- seq(10,34,by = width)
14
15 class_range <- cut(audit_data, breaks, right=T)
16

```

```

17 frequency <- table(class_range)
18
19 frequency_distribution <- data.frame(frequency)
20
21 frequency_distribution <- data.frame(class_range =
22                               frequency_distribution$class_range,
22                               frequency =
22                               frequency_
22                               distribution
22                               $Freq)
23
24 # Note that :- Book answer will differ with my
24     answer though number of classes and width of
25 # each class is same as in the book!!!
26
27                                     # Page no. :
27                                     41
28
29 relative_frequency <- round(frequency_distribution$frequency /
29                               sum(frequency_distribution$frequency)
30                               ,2)    # Rounding
30                               of data to 2
30                               digits
31
32 percentage_frequency <- relative_frequency * 100
33
34 audit_data_FD <- cbind(frequency_distribution,
35                               relative_frequency,
35                               percentage_frequency
35                               )
36
37 View(audit_data_FD)
38
39                                     # Page no. :
39                                     41-42
40
41 # Dot Plot and Histogram
42

```

```

43 # Install Library if not installed
44
45 # install.packages("ggplot2")
46
47 # Import Library
48
49 library(ggplot2)
50
51 # Dot Plot
52
53 dotchart(audit_data, main = "Dot Plot for the Audit
      Time Data", xlab = "Audit Time (days)",
54           cex = 0.5)    # cex is for scaling
55
56 # Note that: Book dot plot is different from my dot
      plot.
57
58 # Histogram
59
60 ggplot(audit_data_FD, aes(class_range, frequency,
      fill = class_range))+
61   geom_histogram(stat = "identity")+labs(title="
      Histogram for the Audit Time Data",
62                                         x = "Audit
      Time (
      days)",
      y = "
      Frequency
      ")+ylim
      (0,8)

```

---

### R code Exa 2.3a Scatter Plot and Tradeline

1 # Page no. :  
57–58

```

2
3 # Dataset
4
5 week <- c(1,2,3,4,5,6,7,8,9,10)
6 x <- c(2,5,1,3,4,1,5,3,4,2)
7 y <- c(50,57,41,54,54,38,63,48,59,46)
8 data <- data.frame(week,x,y)
9
10 # Install Library if not installed
11
12 # install.packages("ggplot2")
13
14 # Import Library
15
16 library(ggplot2)
17
18 # Scatter Plot
19
20 ggplot(data, aes(x,y)) + geom_point() + geom_smooth(
  method = "lm", se = F) +
21 labs(title = "Scatter Plot and Tradeline for the
  Stereo and Sound Equipment Store",
22
     x
     =
     "
     Number
     of
     Commercials
     "
     ,
     y
     =

```

```
  "
Sales

(
$ 
100
s
)
"
)
```

---

### R code Exa 2.4a Cumulative Distributions

```
1          # Page no. :
        44
2
3 # Cumulative Distributions
4
5 audit_time <- c("Less than or equal to 14", "Less
      than or equal to 19", "Less than or equal to 24",
6           "Less than or equal to 29", "Less
      than or equal to 34")
7 frequency <- c(4,8,5,2,1)    # Refer to table no. 2.5
      page no. 40
8 cumulative_freq <- cumsum(frequency)
9
10 DF <- data.frame(audit_time, frequency, cumulative_
      freq)
11
12 CRF <- DF$cumulative_freq / sum(DF$frequency)    #
      Cumulative Relative Frequency
13
14 CPF <- CRF * 100    # Cumulative Percentage Frequency
```

```

15
16 DF <- cbind(DF, CRF, CPF)
17 View(DF)
18
19 breaks <- seq(9, 34, by = 5)
20 cumfreq0 <- c(0, DF$cumulative_freq)
21
22 DF2 <- data.frame(breaks, cumfreq0)
23
24 # Install Library if not installed
25
26 # install.packages("ggplot2")
27
28 # Import Library
29
30 library(ggplot2)
31
32 ggplot(DF2, aes(breaks, cumfreq0, group = 1)) + geom_
    _point() + geom_line() +
33   xlim(c(0,35)) + labs(title = "Ogive For the Audit
      Time Data", x ="Audit Time (Days)",
34   y ="Cumulative Frequency")

```

---

### R code Exa 2.5a Exploratory Data Analysis The Stem and Leaf Display

```

1 # Page no. :
49
2
3 # Exploratory Data Analysis : The Stem – and – Leaf
  Display
4
5 data <- c(112, 72, 69, 97, 107, 73, 92, 76, 86, 73,
       126, 128, 118, 127, 124, 82, 104, 132, 134, 83,
6           92, 108, 96, 100, 92, 115, 76, 91, 102,
           81, 95, 141, 81, 80, 106, 84, 119, 113,

```

```
98, 75,
7 68, 98, 115, 106, 95, 100, 85, 94, 106,
    119)
8
9 stem(data)
10
11 # Page no. :
    51
12
13 data2 <- c(1565, 1852, 1644, 1766, 1888, 1912, 2044,
    1812, 1790, 1679, 2008, 1852, 1967, 1954,
14    1733)
15 stem(data2) # Answer is varing from the book
```

---

# Chapter 3

## Descriptive Statistics Numerical Measures

**R code Exa 3.1a** Measures of Location Mean Part 1

```
1 # Page no. :  
2 87  
3 # Mean  
4  
5 x <- c(46, 54, 42, 46, 32)  
6  
7 sample_mean <- mean(x)  
8  
9 cat("Sample mean for x is ", sample_mean)
```

---

**R code Exa 3.1b** Measures of Location Mean Part 2

```
1 # Page no. :  
2 88
```

```
3 # Dataset
4
5 graduate <- c(1,2,3,4,5,6,7,8,9,10,11,12)
6 salary <- c
    (3450,3550,3650,3480,3355,3310,3490,3730,3540,3925,3520,3480)

7
8
9 dataset <- data.frame(graduate, salary)
10
11 # Mean
12
13 mean_salary <- mean(dataset$salary)
14
15 cat("Mean monthly starting salary of 12 business
    school graduates is",mean_salary)
```

---

#### R code Exa 3.1c Measures of Location Median Part 1

```
1 # Page no.
   : 89
2
3 # Median
4
5 x <- c(32, 42, 46, 46, 54)
6
7 median <- median(x)
8
9 cat("Median value for x is ", median)
```

---

#### R code Exa 3.1d Measures of Location Median Part 2

```

1 # Page no
. : 89
2
3 salary <- c
(3450,3550,3650,3480,3355,3310,3490,3730,3540,3925,3520,3480)

4
5 # Median
6
7 median <- median(salary)
8
9 cat("The median of salary is ", median)

```

---

### R code Exa 3.1e Measures of Location Percentiles and Quartiles

```

1 # Page no.
: 90–91
2
3 salary <- c
(3450,3550,3650,3480,3355,3310,3490,3730,3540,3925,3520,3480)

4
5 # 85th and 50th Percentiles
6
7 solution <- quantile(salary, probs = c(0.85, 0.5))
8
9 cat("Value for 85th and 50th percentile are ",
      solution[1], ", ", solution[2])
10
11 # Note that: 85th percentile value is different from
the book
12
13
14 # 25th, 50th, 75th Percentiles (First, Second, Third
Quartiles)

```

```
15
16 values <- quantile(salary, probs = c(0.25, 0.5,
17   0.75))
18 cat("Value for first , second , third quartiles are " ,
19     values[1] , " , " , values[2] , " , " , values[3] )
20 # Note that: First and Second Quartile values are
21   different from the book
```

---

### R code Exa 3.2a Measures of Variability Range and IQR

```
1 # Page no. :
2   96–97
3
4 salary <- c
5   (3450 , 3550 , 3650 , 3480 , 3355 , 3310 , 3490 , 3730 , 3540 , 3925 , 3520 , 3480)
6
7 range <- range(salary)
8 diff <- range[2] - range[1]
9
10 cat("Range is" , diff)
11
12 # Inter-Quartile Range
13
14 IQR <- IQR(salary)
15
16 cat("IQR is " , IQR)
17
18 # Note that : IQR value of Book is different.
```

---

### R code Exa 3.2b Measures of Variability Variance

```
1 # Page no. :  
2 # 97–98  
3 students <- c(46, 54, 42, 46, 32)  
4  
5 # Variance  
6  
7 variance <- var(students)  
8  
9 cat("Variance of students is ", variance)
```

---

### R code Exa 3.2c Measures of Variability Standard Deviation

```
1 # Page no. :  
2 # 98–99  
3 salary <- c  
4 (3450, 3550, 3650, 3480, 3355, 3310, 3490, 3730, 3540, 3925, 3520, 3480)  
5  
6 # Variance  
7 variance <- var(salary)  
8  
9 # Standard Deviation  
10  
11 sd <- sd(salary)  
12  
13 cat("Variance of salary is ", variance)  
14 cat("Standard Deviation is ", sd)
```

---

### R code Exa 3.3a Z Score

```
1 # Page  
no. :  
104  
2  
3 # Z-score  
4  
5 students <- c(46,54,42,46,32)  
6  
7 deviation <- students - mean(students)  
8  
9 sample_variance <- var(students)  
10  
11 dataset <- data.frame(students,deviation)  
12  
13 z <- c()  
14  
15 for(i in 1:length(dataset$students)){  
16   z[i] <- deviation[i]/sqrt(sample_variance)  
17 }  
18  
19 dataset <- cbind(dataset, zScore = z)  
20  
21 View(dataset)
```

---

### R code Exa 3.4a Boxplot

```
1 # Page no.  
: 110  
2
```

```

3 salary <- c
  (3450,3550,3650,3480,3355,3310,3490,3730,3540,3925,3520,3480)

4
5 # Install Library if not installed
6
7 #install.packages("ggplot2")
8
9 # Import Library
10
11 library(ggplot2)
12
13 # Boxplot
14
15 ggplot(data.frame(salary), aes(x = "", y = salary))
  + geom_boxplot(fill = "purple")+
16   ggttitle("Boxplot for Salary") + ylab("Salary")

```

---

### R code Exa 3.5a Covariance and Correlation Coefficient

```

1 # Page no. :
  115–116 and 119
2
3 # Dataset
4
5 x <- c(2,5,1,3,4,1,5,3,4,2)
6 y <- c(50,57,41,54,54,38,63,48,59,46)
7
8 dataset <- data.frame(x,y)
9
10 # Covariance
11
12 covariance <- cov(dataset$x,dataset$y)
13
14 cat("Value of covariance is ",covariance)

```

```
15
16 # Correlation Coefficient
17
18 correlation <- cor(dataset$x,dataset$y)
19
20 cat("Value of correlation coefficient is ",  
     correlation)
```

---

### R code Exa 3.5b Sample Correlation Coefficient

```
1 # Page no.  
   : 121
2
3 # Data
4
5 x <- c(5,10,15)
6 y <- c(10,30,50)
7
8 # Sample Correlation Coefficient
9
10 corr <- cor(x, y)
11
12 cat("Sample correlation coefficient of x and y is ",  
      corr)
```

---

### R code Exa 3.6a Weighted Mean

```
1 # Page no. :  
   124 – 125
2
3 # Data
4
5 purchase <- c(1,2,3,4,5)
```

```

6 cost <- c(3.00,3.40,2.80,2.90,3.25)
7 pound <- c(1200,500,2750,1000,800)
8
9 dataset <- data.frame(purchase,cost,pound)
10
11 # Weighted Mean
12
13 mean <- weighted.mean(dataset$cost,dataset$pound)
14
15 cat("Weighted mean for the dataset is",mean)

```

---

### R code Exa 3.6b Grouped Data Mean and Sample Variance

```

1 # Page no.
   : 126
   - 127
2
3 # Data
4
5 audit <- c("10-14", "15-19", "20-24", "25-29", "30-34")
6 midpoint <- c(12,17,22,27,32)
7 frequency <- c(4,8,5,2,1)
8
9 dataset <- data.frame(audit, midpoint, frequency)
10
11 # Mean for Grouped Data
12
13 mean <- weighted.mean(dataset$midpoint,dataset$frequency)
14
15 cat("Mean for grouped data is",mean)
16
17 # Sample Variance for Grouped Data
18
19 var <- sum(dataset$frequency*((dataset$midpoint -

```

```
    mean)**2)) / (sum(dataset$frequency) - 1)
20
21 # Note that : Grouped sample variance has no inbuild
  function
22
23 cat("Sample variance for grouped data is", var)
```

---

# Chapter 4

## Introduction to Probability

R code Exa 4.1a Combinations

```
1 # Page no. :  
2 # 154  
3 # Combinations  
4  
5 # Eg. 1  
6  
7 N <- 5  
8 n <- 2  
9  
10 combinations <- choose(n = N, k = n)  
11  
12 cat("The total combinations are", combinations)  
13  
14 # Eg. 2  
15  
16 N <- 53  
17 n <- 6  
18  
19 combinations <- choose(n = N, k = n)  
20
```

```
21 cat("The total combinations are",combinations)
```

---

### R code Exa 4.1b Permutations

```
1 # Page no.  
  : 155  
2  
3 # Permutations  
4  
5 N <- 5  
6 n <- 2  
7  
8 permutations <- choose(n = N, k = n)*factorial(n)  
9  
10 cat("The total permutations are",permutations)
```

---

### R code Exa 4.1c Assigning Probabilities

```
1 # Page no. : 155  
  - 156  
2  
3 # Assigning Probabilities  
4  
5 x <- c(0,1,2,3,4)  
6 y <- c(2,5,6,4,3)  
7  
8 DF <- data.frame(x,y)  
9  
10 y_sum <- sum(DF$y)  
11  
12 prob <- DF$y / y_sum  
13  
14 DF <- cbind(DF,prob)
```

```
15  
16 View(DF)
```

---

### R code Exa 4.1d Probabilities Assigning Example

```
1 # Page no. :  
2 # 157 - 158  
3 # Probabilities Assigning Example  
4  
5 x <- c(2,2,2,3,3,3,4,4,4)  
6 y <- c(6,7,8,6,7,8,6,7,8)  
7  
8 z = list()  
9  
10 for(i in 1:length(x))  
11 {  
12   z[i] <- list(c(x[i],y[i]))  
13 }  
14  
15 past_project <- c(6,6,2,4,8,2,2,4,6)  
16  
17 DF <- data.frame(x,y,I(z),past_project)  
18  
19 past_project_sum <- sum(DF$past_project)  
20  
21 p <- DF$past_project / past_project_sum  
22  
23 DF <- cbind(DF,p)  
24  
25 total_probability <- sum(DF$p)  
26  
27 cat("Total probability for the Sample Point is",  
     total_probability)  
28
```

29 View(DF)

---

### R code Exa 4.2a Probability of an Event

```
1 # Page no. :  
161  
2  
3 # Probability of an Event  
4  
5 # C denotes the event that is completed in 10 months  
or less  
6  
7 C <- c(list(c(2,6)), list(c(2,7)), list(c(2,8)),  
list(c(3,7)), list(c(3,8)), list(c(4,6)))  
8 prob <- c(0.15,0.15,0.05,0.10,0.20,0.05)  
9  
10 dataset <- data.frame(I(C),prob)  
11  
12 event <- sum(dataset$prob)  
13  
14 # P(C) = P(2,6) + P(2,7) + P(2,8) + P(3,7) + P(3,8)  
+ P(4,6)  
15  
16 cat("Probability of an event P(C) is",event)  
17  
18 # L denotes the event that is completed in less than  
10 months  
19  
20 L <- c(list(c(2,6)), list(c(2,7)), list(c(3,7)))  
21 prob <- c(0.15,0.15,0.10)  
22  
23 dataset <- data.frame(I(L),prob)  
24  
25 # P(L) = P(2,6) + P(2,7) + P(3,7)  
26
```

```

27 event2 <- sum(dataset$prob)
28
29 cat("Probability of an event P(L) is",event2)
30
31 # M denotes the event that is completed in more than
   10 months
32
33 M <- c(list(c(3,8)), list(c(4,7)), list(c(4,8)))
34 prob <- c(0.05,0.10,0.15)
35
36 dataset <- data.frame(I(M),prob)
37
38 # P(M) = P(3,8) + P(4,7) + P(4,8)
39
40 event3 <- sum(dataset$prob)
41
42 cat("Probability of an event P(L) is",event3)

```

---

**R code Exa 4.3a** Probability Computation using Complement

```

1                                     # Page no. :
   165
2
3 # Probability Computation using Complement
4
5 p_comp_A <- 0.80
6
7 p_A <- 1 - p_comp_A
8
9 cat("Probability for A is",p_A)

```

---

**R code Exa 4.3b** Intersection and Union of Events

```

1 # Pahe no. : 167
2
3 # Intersection and Union of Events
4
5 a <- 5
6 n <- 50
7 c <- 6
8 d <- 2
9
10 p_L <- a / n
11
12 p_D <- c / n
13
14 p_L_and_D <- d / n
15
16
17 cat("Probability for L intersection D is", p_L_and_D)
18
19 p_L_or_D <- p_L + p_D - p_L_and_D
20
21 cat("Probability for L union D is", p_L_or_D)

```

---

### R code Exa 4.3c Addition Law

```

1 # Page no. :
2 168
3
4
5 p_S <- 0.30
6 p_W <- 0.20
7 p_S_and_W <- 0.12
8
9 p_S_or_W <- p_S + p_W - p_S_and_W
10

```

```
11 cat("Probability after applying addition law is ", p_S_or_W)
```

---

### R code Exa 4.4a Conditional Probability

```
1 # Page no. :  
2 # 171 - 174  
3 # Conditional Probability  
4  
5 position <- c("Promoted", "Not Promoted")  
6 gender <- c("Men", "Women")  
7 number1 <- c(288, 36) # Promoted  
8 number2 <- c(672, 204) # Not Promoted  
9  
10 DF <- data.frame(position, gender, number1, number2)  
11  
12 table <- round(prop.table(DF[,3:4]), 2)  
13 table <- as.matrix(table)  
14 table  
15  
16 position <- c("Promoted", "Not Promoted")  
17 men <- c(table[1,1][[1]], table[1,2][[1]])  
18 women <- c(table[2,1][[1]], table[2,2][[1]])  
19  
20 DF2 <- data.frame(position, men, women)  
21 View(DF2)  
22  
23 columnSums <- apply(DF2[,2:3], 2, sum)  
24 rowSums <- apply(DF2[,2:3], 1, sum)  
25  
26 cat("Total Probability For having Men is",  
      columnSums[1])  
27 cat("Total Probability For having Women is",  
      columnSums[2])
```

```

28 cat("Total Probability For Promotion", rowSums[1])
29 cat("Total Probability For Not a Promotion", rowSums
      [2])
30
31 cond1 <- DF2$men[1] / columnSums[1]
32
33 cat("Conditional Probability for Men and getting
      Promoted given the Probability
      of Total Men is", cond1)
34
35 cond2 <- DF2$women[1] / columnSums[2]
36
37
38 cat("Conditional Probability for Women and getting
      Promoted given the Probability
      of Total Women is", cond2)

```

---

### R code Exa 4.4b Multiplication Law

```

1 # Page no. :
      174 – 175
2
3 # Multiplication Law
4
5 # P(S | D) = 0.75
6
7 x <- 0.75
8
9 # Event S = 0.84
10
11 y <- 0.84
12
13 x_and_y <- x * y
14
15 cat("After applying multiplication law we get", x_
      and_y)

```

```

16
17 # Multiplication Law for Independent Events
18
19 A <- 0.80
20
21 B <- 0.80
22
23 A_and_B <- A * B
24
25 cat("After applying multiplication law for
      independent events A and B we get", A_and_B)

```

---

### R code Exa 4.5a Bayes Theorem Tabular Approach

```

1 # Page no. : 182
2
3 # Tabular Approach for Bayes' Theorem
4
5 events <- c("A1","A2")
6 prior_probabilities <- c(0.65,0.35)
7
8 conditional_probabilities <- c(0.02,0.05)
9
10 joint_probabilities <- prior_probabilities *
     conditional_probabilities
11
12 total_joint_probability <- sum(joint_probabilities)
13
14 posterior_probabilities <- joint_probabilities /
     total_joint_probability
15
16 DF <- data.frame(events,prior_probabilities,
     conditional_probabilities
17           ,joint_probabilities,posterior_
     probabilities)

```

```
18  
19 View(DF)  
20  
21 cat("Total posterior probability is", sum(DF$  
      posterior_probabilities))
```

---

# Chapter 5

## Discrete Probability Distribution

**R code Exa 5.1a** Discrete Probability Distribution Graph Expected value  
Variance and Standard Deviation

```
1 # Page no. : 198
   - 199
2
3 # Discrete Probability Distribution :
4
5 x <- c(0,1,2,3,4,5)
6 prob_of_x <- c(0.18,0.39,0.24,0.14,0.04,0.01)
7
8 dataset <- data.frame(x, prob_of_x)
9
10 # Install Library if not installed
11
12 # install.packages("ggplot2")
13
14 # Import Library
15
16 library(ggplot2)
17
```

```

18 ggplot(dataset, aes(x = x, y = prob_of_x)) + geom_
  bar(stat = "identity", fill = "blue") + labs(
19   title = "Graphical representation of the
    Probability Distribution",
20   x = "Number of Automobiles", y = "Probability")
21
22                                     # Page no. : 203
23
24 # Expected value
25
26 exp_values <- dataset$x * dataset$prob_of_x
27
28 dataset <- data.frame(cbind(dataset, exp_values))
29
30 expected_value <- sum(dataset$exp_values)
31 cat("Expected value for the given problem is",
     expected_value)
32
33                                     # Page no. : 204 -
  205
34
35 # Variance and Standard Deviation
36
37 deviation_of_x <- (dataset$x - expected_value)
38
39 deviation_square <- (deviation_of_x) ** 2
40 variance <- sum(dataset$prob_of_x * deviation_square
  )
41 standard_deviation <- sqrt(variance)
42
43 cat("Variance is", variance)
44 cat("Standard Deviation is", standard_deviation)

```

---

**R code Exa 5.2a** Binomial Probability Distribution

```

1 # Page no. : 211
2
3 # Binomial Probability Distribution
4
5 no_of_trials <- 3
6 no_of_successes <- 2
7 BPD <- choose(n = no_of_trials, k = no_of_successes)
8
9 cat("Answer is", BPD)
10
11 no_of_successes <- 3
12 BPD <- choose(n = no_of_trials, k = no_of_successes)
13 cat("Answer is", BPD)

```

---

### R code Exa 5.2b Binomial Probability Distribution Eg2

```

1 # Page no
2 . :
3 211
4
5 # Binomial Probability Distribution Eg-2
6
7 # Data
8 customer1 <- c("Purchase", "Purchase", "No Purchase")
9 customer2 <- c("Purchase", "No Purchase", "Purchase")
10 customer3 <- c("No Purchase", "Purchase", "Purchase")
11
12 customer <- data.frame(customer1, customer2, customer3)
13
14 len <- nrow(customer) # Trial
15
16 x <- 1    # For purchase
17 y <- 0    # For no purchase

```

```

17 p <- 0.30
18 q <- 1 - p
19 outcome <- c()
20
21 # Install Library if not installed
22
23 install.packages("Rlab")
24
25 # Import Library
26
27 library(Rlab)    # For dbern
28
29 for(i in 1:len)
30 {
31   if(customer1[i] == "Purchase" && customer2[i] == "
      Purchase" && customer3[i] == "Purchase")
32   {
33     outcome[i] = dbern(x,p) * dbern(x,p) * dbern(x,p
      )
34   } else if(customer1[i] == "Purchase" && customer2[
      i] == "Purchase" && customer3[i] == "No
      Purchase")
35   {
36     outcome[i] = dbern(x,p) * dbern(x,p) * dbern(y,p
      )
37   } else if(customer1[i] == "Purchase" && customer2[
      i] == "No Purchase" && customer3[i] == "
      Purchase")
38   {
39     outcome[i] = dbern(x,p) * dbern(y,p) * dbern(x,p
      )
40   } else if(customer1[i] == "Purchase" && customer2[
      i] == "No Purchase" && customer3[i] == "No
      Purchase")
41   {
42     outcome[i] = dbern(x,p) * dbern(y,p) * dbern(y,p
      )
43   } else if(customer1[i] == "No Purchase" &&

```

```

        customer2[i] == "Purchase" && customer3[i] == "
Purchase")
44 { 
45     outcome[i] = dbern(y,p) * dbern(x,p) * dbern(x,p
)
46 } else if(customer1[i] == "No Purchase" &&
customer2[i] == "Purchase" && customer3[i] == "
No Purchase")
47 { 
48     outcome[i] = dbern(y,p) * dbern(x,p) * dbern(y,p
)
49 } else if(customer1[i] == "No Purchase" &&
customer2[i] == "No Purchase" && customer3[i]
== "Purchase")
50 { 
51     outcome[i] = dbern(y,p) * dbern(y,p) * dbern(x,p
)
52 } else
53 { 
54     outcome[i] = dbern(y,p) * dbern(y,p) * dbern(y,p
)
55 }
56 }
57
58 customer <- cbind(customer,outcome)
59
60 View(customer)
61
62                                     # Page no. :
63                                     212 -
64                                     213
65
66 # Binomial Probability Function
67
68 x <- c(0,1,2,3)
69 fun <- c()
70
71 for (i in 0:length(x)) {

```

```

70   fun[i] <- dbinom(x[i], len, p)
71 }
72
73 dataset <- data.frame(x, fun)
74 View(dataset)
75
76 # Install Library if not installed
77
78 # install.packages("ggplot2")
79
80 # Import Library
81
82 library(ggplot2)
83
84 ggplot(dataset, aes(x = x, y = fun)) + geom_bar(stat =
85   "identity", fill = "blue") + labs(
86     title = "Graphical representation of the
87       Probability Distribution",
88     x = "Number of Customers", y = "Probability")
89
90 # Page no. :
91 # Expected Value, Variance and Standard Deviation
92 # for Binomial Probability Distribution
93
94 # Page no. :
95
96 # Expected Value, Variance and Standard Deviation
97 # for Binomial Probability Distribution
98
99
100
```

---

### R code Exa 5.3a Poisson Probability Distribution

```
1 # Page no. :  
2 # 218  
3 # Poisson Probability Distribution  
4  
5 x = 5  
6 expected_value <- 10  
7 e <- 2.72 # Exponential value  
8  
9 PPD <- dpois(x, expected_value) # Poisson  
    Probability Distribution  
10  
11 cat("Answer is", PPD)
```

---

### R code Exa 5.4a Hypergeometric Probability Distribution

```
1 # Page no. : 222  
2 # - 223  
3 # Hypergeometric Probability Distribution  
4  
5 # Probability for 1 defective item  
6  
7 N <- 12  
8 n <- 3  
9 r <- 5  
10 x <- 1  
11  
12 HPD <- dhyper(x = x, m = r, n = N-r, k = n)  
13  
14 cat("Answer is", HPD)  
15  
16 # Probability for atleast one defective item
```

```

17
18 HPD <- dhyper(x = 0,m = r,n = N-r,k = n) # Probability for no defective item
19
20 cat("Answer is",1 - HPD) # Probability for atleast one defective item
21
22 # Expected value , Variance and Standard Deviation
23
24 expected_value <- n * (r / N)
25 variance <- expected_value * (1 -(r/N)) * ((N-n)/(N-1))
26 standard_deviation <- sqrt(variance)
27
28 cat("Expected value",expected_value)
29 cat("Variance",variance)
30 cat("standard deviation",standard_deviation)

```

---

### R code Exa 5.5a Expected Value and Variance

```

1 # Page no. :
2 # 203 – 204
3
4
5 x <- c(0,1,2,3,4,5)
6 prob_of_x <- c(0.18,0.39,0.24,0.14,0.04,0.01)
7 expected_value <- x * prob_of_x
8
9 DF <- data.frame(x, prob_of_x, expected_value)
10
11 expected_mean <- sum(DF$expected_value)
12
13 cat("Expected mean is",expected_mean)
14

```

```
15 deviation <- DF$x - expected_mean
16 sq_deviation <- deviation ** 2
17 expected_value2 <- DF$prob_of_x * sq_deviation
18
19 DF <- cbind(DF, deviation, sq_deviation, expected_
    value2)
20 View(DF)
21
22 expected_variance <- sum(DF$expected_value2)
23
24 cat("Expected variance is", expected_variance)
25
26 expected_SD <- sqrt(expected_variance)
27
28 cat("Expected SD is", expected_SD)
```

---

# Chapter 6

## Continuous Probability Distribution

**R code Exa 6.1a** Uniform Probability Distribution

```
1 # Page no. : 234 –  
2  
3 # Uniform Probability Distribution  
4  
5 a <- 120  
6 b <- 140  
7 fun_over_x <- 1/20  
8  
9 # Since uniform probability is symmetric we can  
# split it into left and right parts which  
10 # are symmetric in nature  
11  
12 c <- 130 # (120+140)/2 = 130  
13  
14 # Probability of uniform probability distribution  
# is the area of the figure (rectangle)  
15  
16 # Area for the left symmetric part of the figure
```

```

17
18 area <- punif(c,a,b)
19 area_full <- 2 * area
20
21 cat(" Probability is",area_full)
22
23 # Expected value , Variance and standard Deviation
24
25 expected_value <- (a + b) / 2
26 variance <- (b - a) ** 2 / 12
27 standard_deviation <- sqrt(variance)
28
29 cat("Expected value is",expected_value)
30 cat("Variance is",variance)
31 cat("Standard deviation is",standard_deviation)

```

---

### R code Exa 6.2a Normal Probability Distribution

```

1 # Page no. : 246
   - 247
2
3 # Normal Probability Distribution
4
5 mean <- 36500
6 sigma <- 5000
7 x <- 40000
8 probability <- pnorm(40000, mean=36500, sd=5000,
   lower.tail= F)
9
10 cat("The probability of x exceed 40000 is",
     probability)
11
12 # Page no. : 247
13
14 probability <- 0.10

```

```

15 z_value <- round(qnorm(probability), 2)      # Round it
       to 2 decimal place
16 x <- (sigma * z_value) + mean
17
18 cat("Value of x for not more than 10% of area is
       selected is", x)

```

---

### R code Exa 6.3a Normal Approximation of Binomial Probabilities

```

1                                     # Page no. : 251 –
2                                         252
3 # Normal Approximation of Binomial Probabilities
4
5 n <- 100
6 p <- 0.1
7 q <- 1 - p
8
9 mu <- n * p
10 sigma <- sqrt(mu * q)
11
12 # P(x = 12) ==> P(11.5 <= x <= 12.5)
13
14 x1 <- 12.5
15 x2 <- 11.5
16 z_value1 <- (x1 - mu) / sigma
17 z_value2 <- (x2 - mu) / sigma
18
19 area1 <- pnorm(z_value1)
20 area2 <- pnorm(z_value2)
21
22 diff <- area1 - area2
23
24 cat("The normal approximation to the probability of
       12 successes in 100 trials is ", diff)

```

```

25
26 # Probability for 13
27
28 x <- 13.5
29 z <- (x - mu) / sigma
30 ans <- pnorm(z)
31
32 cat("Answer is", ans)

```

---

### R code Exa 6.4a Exponential Probability Distribution

```

1 # Page no. :
2 255
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22

```

```

# Exponential Probability Distribution
# P(x <= 6)
EPD <- pexp(x1, 1/mu)
# P(x <= 18)
EPD2 <- pexp(x2, 1/mu)
diff <- EPD2 - EPD
cat("The probability that loading a truck will take
between 6 and 18 minutes is ", diff)
SD <- mu
sigma <- SD ** 2

```

23

24 `cat("Variance is", sigma)`

---

# Chapter 7

## Sampling and Sampling Distribution

**R code Exa 7.1a** Point Estimator

```
1 # Page no  
2 . :  
3 274  
4  
5 annual_salary <- c  
6 (49094.30,53263.90,49643.50,49894.90,47621.60,55924.00,49092.30,5  
7 55109.70,45922.60,57268.40,55688.80,51564.70,5618  
8 51932.60,52973.00,45120.90,51753.00,54391.80,5016  
9 50979.40,55860.90,57309.10)  
10 program <- c("Yes","Yes","Yes","Yes","No","Yes","Yes",  
11 "Yes","Yes","Yes","Yes","Yes","No","Yes","No","No",  
12 "Yes",  
13 "No","Yes","Yes","Yes","Yes","Yes","Yes","No",  
14 "Yes","Yes")
```

```

          No" , "No" , "No" , "No" , "Yes" , "Yes" , "No" )
12
13 dataset <- data.frame(annual_salary, program)
14
15 sample_mean <- mean(dataset$annual_salary)
16 sample_sd <- sd(dataset$annual_salary)
17
18 cat("Sample mean of the data is", sample_mean)
19 cat("Sample standard deviation is", sample_sd)
20
21 # Note that : Book SD is different from our SD
22
23 # Sample Proportion
24
25 n <- nrow(dataset)
26 x <- 19
27
28 sample_proportion <- x / n
29
30 cat("Sample Proportion is", sample_proportion)

```

---

### R code Exa 7.2a Sampling Distribution

```

1                                     # Page no. 277
2                                         - 278
3
4
5 mean_annual_salary <- c("49500.00-49999.99",
6                               "50000.00-50499.99", "50500.00-50999.99",
7                               "51000.00-51499.99",
8                               "51500.00-51999.99", "52000.00-52499.99",
9                               "52500.00-52999.99", "53000.00-53499.99",

```

```

7                               " 53500.00 - 53999.99")
8 frequency <- c(2,16,52,101,133,110,54,26,6)
9 relative_frequency <- c
10                         (.004,.032,.104,.202,.266,.220,.108,.052,.012)
11 DF <- data.frame(mean_annual_salary,frequency,
12                     relative_frequency)
13 library(ggplot2)
14
15 ggplot(DF,aes(mean_annual_salary,relative_frequency)
16         ) +
17         geom_histogram(stat = "identity", fill = "purple")
18         + labs(title = "Relative Frequency Histogram",
19                 x = "Mean Salary",
20                 y = "frequency"
21         )

```

---

### R code Exa 7.3a Sampling Distribution of Sample Mean

```

1 # Page no. :
2                         281
3
4
5 sigma <- 4000
6 N <- 2500
7 n <- 30
8 x <- n / N
9
10 if(x > 0.05)    # Condition to include finite
11     population factor or not (< 5%)
12 {
13     standard_error <- sqrt((N-n)/(N-1)) * (sigma /
14     sqrt(n))

```

```

13 } else{
14   standard_error <- sigma / sqrt(n)
15 }
16
17 cat("Standard deviation of sample mean is",standard_
18 error)
19                                         # Page no. : 284
20
21 # To find probability that xbar is between 51300 and
22      52300
23
24 xbar1 <- 52300
25 xbar2 <- 51300
26 mu <- 51800
27
28 z1 <- (xbar1 - mu) / standard_error
29 z2 <- (xbar2 - mu) / standard_error
30
31 p1 <- pnorm(z1, lower.tail = T)
32 p2 <- pnorm(z2, lower.tail = T)
33
34 diff <- p1 - p2
35
36 cat("Probability that xbar is between 51300 and
37      52300 is", diff)

```

---

**R code Exa 7.3b** Relationship between Sample Size and Sampling Distribution of xbar

```

1                                         # Page no. :
2                                         285 -
3                                         286
4
5 # Relationship between Sample Size and Sampling

```

```

        Distribution of xbar
4
5 sigma <- 4000
6 n <- 100
7 population_mean <- 51800
8
9 standard_error <- sigma / sqrt(n)
10
11 xbar1 <- 52300
12 xbar2 <- 51300
13
14 z1 <- (xbar1 - population_mean) / standard_error
15 z2 <- (xbar2 - population_mean) / standard_error
16
17 p1 <- pnorm(z1, lower.tail = T)
18 p2 <- pnorm(z2, lower.tail = T)
19
20 diff <- p1 - p2
21
22 cat("Probability that xbar is between 51300 and
      52300 with increased sample size is", diff)

```

---

### R code Exa 7.4a Sampling Distribution of Sample Proportion

```

1 # Page no.
   : 290
2
3 # Sampling Distribution of pbar
4
5 population_proportion <- 0.60
6 n <- 30
7 N <- 2500
8
9 x <- n / N
10

```

```

11 if(x > 0.05)  # Condition to include finite
    population or not (< 5%)
12 {
13   standard_deviation <- sqrt((N-n)(N-1)) * sqrt((
    population_proportion *
14
(1
-
population
-
proportion
)
)
/
n
)

15 } else{
16   standard_deviation <- sqrt((population_proportion
      * (1 - population_proportion)) / n)
17 }
18
19 cat("Standard deviation for sample proportion is",
     standard_deviation)

```

---

**R code Exa 7.4b** Practical value of the Sampling Distribution of Sample Proportion

```

1                                     # Page no. : 291
2
3 # Practical value of the Sampling Distribution of
  pbar

```

```

4
5 population_proportion <- 0.60
6 standard_error <- 0.0894
7 sample_proportion <- 0.65
8
9 z_value <- (sample_proportion - population_
    proportion) / standard_error
10
11 prob1 <- pnorm(sample_proportion, population_
    proportion, standard_error, lower.tail =T)
12
13 sample_proportion2 <- 0.55
14
15 z_value <- (sample_proportion2 - population_
    proportion) / standard_error
16
17 prob2 <- pnorm(sample_proportion2, population_
    proportion, standard_error, lower.tail =T)
18
19 final_prob <- prob1 - prob2
20
21 cat("The final probability is",final_prob)

```

---

**R code Exa 7.4c** Practical value of the Sampling Distribution of Sample Proportion Eg2

```

1 # Page no. : 292 –
2 # 293
3 # Practical value of the Sampling Distribution of
4 # pbar Eg-2
5 population_proportion <- 0.60
6 n <- 100
7

```

```
8 standard_error <- sqrt(population_proportion*(1 -
    population_proportion)/(n))
9
10 sample_proportion <- 0.65
11
12 z_value <- (sample_proportion - population_
    proportion) / standard_error
13
14 prob1 <- pnorm(sample_proportion, population_
    proportion, standard_error, lower.tail =T)
15
16 sample_proportion2 <- 0.55
17
18 z_value <- (sample_proportion2 - population_
    proportion) / standard_error
19
20 prob2 <- pnorm(sample_proportion2, population_
    proportion, standard_error, lower.tail =T)
21
22 final_prob <- prob1 - prob2
23
24 cat("The final probability is",final_prob)
```

---

# Chapter 8

## Interval Estimation

R code Exa 8.1a Population Mean Sigma Known

```
1 # Page no. :  
# 310 – 314  
2 # Population Mean Sigma known  
3  
4 pop_sd <- 20  
5 sample_size <- 100  
6 sample_mean <- 82  
7  
8 standard_error <- pop_sd / sqrt(sample_size)  
9  
10 # 95% confidence interval  
11  
12 margin_of_error <- qnorm(0.975)*standard_error #  
# 95% confidence interval --> 1 - 0.025 = 0.975  
13  
14 IE <- sample_mean + c(-margin_of_error, margin_of_  
error)  
15  
16 cat("The margin of error is given by", margin_of_  
error)  
17 cat("The 95% interval estimate is given by", IE)
```

```

18
19 # 90% confidence interval
20
21 margin_of_error <- qnorm(0.95)*standard_error    #
90% confidence interval --> 1 - 0.05 = 0.95
22
23 IE <- sample_mean + c(-margin_of_error, margin_of_
error)
24
25 cat("The margin of error is given by", margin_of_
error)
26 cat("The 90% interval estimate is given by", IE)
27
28 # 99% confidence interval
29
30 margin_of_error <- qnorm(0.995)*standard_error    #
99% confidence interval --> 1 - 0.005 = 0.995
31
32 IE <- sample_mean + c(-margin_of_error, margin_of_
error)
33
34 cat("The margin of error is given by", margin_of_
error)
35 cat("The 99% interval estimate is given by", IE)

```

---

### R code Exa 8.2a Population Mean Sigma Unknown

```

1 # Page no. :
319 - 320
2
3
4 # Population Mean Sigma Unknown
5
6 credit_card_balances <- c
(9430,7535,4078,5604,5179,4416,10676,1627,10112,6567,13627,18719,1

```

```

7          10544,13659,7061,6245,13021,9719,2200,1074
8          7917,11346,12806,4972,11356,7117,9465,1926
9          6845,10493,615,13627,12557,6232,9691,11448
10         12851,5337,8372,7445,11032,6525,5239,6195,
11
12 test <- t.test(cradit_card_balances)
13 IE1 <- test$conf.int[1]
14 IE2 <- test$conf.int[2]
15
16 cat("The 95% interval estimate is given by", IE1, "
      to", IE2)

```

---

### R code Exa 8.2b Population Mean Sigma Unknown Eg2

```

1 # Page no. :
2                         321 – 322
3 # Population Mean Sigma Unknown Eg–2
4
5 data <- c
6   (52,44,55,44,45,59,50,54,62,46,54,42,60,62,43,42,48,55,57,56)
7
8 hist(data, col = "blue", main = "Histogram of
9   Training Times", xlab = "Training Times (days)",
10  ylab = "Frequency")
11 test <- t.test(data)
12 IE1 <- test$conf.int[1]

```

```
13 IE2 <- test$conf.int[2]
14
15 cat("The 95% interval estimate is given by", IE1, "
      to", IE2)
```

---

### R code Exa 8.3a Determining the Sample Size

```
1 # Page no. :
      326 – 327
2
3 # Determining the Sample Size
4
5 margin_of_error <- 2
6 z_value <- 1.96    # 95% Level of Confidence Interval
7
8 sample_standard_deviation <- 9.65
9
10 sample_size <- ((z_value)**2) * ((sample_standard_
      deviation)**2) / (margin_of_error)**2
11
12 cat("Sample size is", ceiling(sample_size))
13 # If Sample Size is not integer then we round up to
      next higher integer
```

---

### R code Exa 8.4a Population Proportion

```
1 # Page no. :
      329
2
3 # Population Proportion
4
5 N <- 900
6 n <- 396
```

```

7
8 p <- n / N
9 q <- 1 - p
10
11 # Confidence Interval is 95%
12
13 z_value <- qnorm(0.975)    # 95% confidence interval
14      --> 1 - 0.025 = 0.975
15 margin_of_error <- z_value * sqrt((p*q)/N)
16 IE <- p + c(-margin_of_error, margin_of_error)
17
18 cat("The margin of error is given by", margin_of_
19      error)
20 cat("The 95% interval estimate is given by", IE)

```

---

### R code Exa 8.4b Determining the Sample Size

```

1 # Page no. :
2                      330
3
4
5 margin_of_error <- 0.025
6 z_value <- 1.96    # 95% Level of Confidence Interval
7
8 p <- 0.44
9 q <- 1 - p
10
11 sample_size <- ((z_value)**2 * p * q) / (margin_of_
12      error)**2
13 cat("Sample size is", ceiling(sample_size))
14 # If Sample Size is not integer then we round up to
15      next higher integer

```

```
15  
16 # Page no. :  
    331  
17  
18 margin_of_error <- 0.025  
19 z_value <- 1.96 # 95% Level of Confidence Interval  
20  
21 p <- 0.50  
22 q <- 1 - p  
23  
24 sample_size <- ((z_value)**2 * p * q) / (margin_of_  
    error)**2  
25  
26 cat("Sample size is", ceiling(sample_size))  
27 # If Sample Size is not integer then we round up to  
    next higher integer
```

---

# Chapter 9

## Hypothesis Testing

R code Exa 9.1a Population Mean Sigma Known One Tailed Test

```
1 # Page no. :  
2 # 359 - 360  
3 # Population Mean Sigma Known One Tailed Test  
4  
5 sigma <- 0.18  
6 n <- 36  
7 xbar <- 2.92  
8 mu <- 3  
9  
10 z_value <- (xbar - mu) / (sigma / sqrt(n))  
11 z_value <- round(z_value,2)  
12  
13 alpha <- 0.01  
14  
15 # P Value Approach (Lower-Tail Test)  
16  
17 pval <- pnorm(z_value)  
18  
19 if(pval > alpha)  
20 {
```

```

21   cat("Since p-value ",pval," is greater than 0.01 ,  

     therefore we will accept null hypothesis")  

22 } else {  

23   cat("Since p-value ",pval," is less than 0.01 ,  

     therefore we will reject null hypothesis and  

     accept  

     alternative hypothesis.")  

25 }  

26  

27 # Critical Value Approach (Lower-Tail Test)  

28  

29 z_alpha <- qnorm(1 - (alpha))    # Area of 0.01 to  

     the left (1 - 0.01 = 0.99)  

30 critical_approch <- -z_alpha  

31  

32 if(z_value <= critical_approch)  

33 {  

34   cat("Since z-value", z_value , "is less then or  

     equal to", critical_approch , "therefore we  

     reject  

     the null hypothesis and accept the alternative  

     hypothesis.")  

36 } else{  

37   cat("Since z-value", z_value , "is more than",  

     critical_approch , "therefore we accept the null  

     hypothesis.")  

38 }

```

---

### R code Exa 9.1b Population Mean Sigma Known Two Tailed Test

```

1                      # Page no. :  

                     362 -  

                     364  

2  

3 # Population Mean Sigma Known Two Tailed Test

```

```

4
5 sample_size <- 50
6 sample_mean <- 297.6
7 population_mean <- 295
8 significance_level <- 0.05      # alpha
9 population_sd <- 12
10
11                                     # Page no. :
12                                     364
13 ## Critical value approach
14
15 z_value <- (sample_mean - population_mean) / (
16   population_sd / sqrt(sample_size))
17 z_half_alpha <- qnorm(1 - (significance_level/2))
18 critical_value_1 <- -z_half_alpha
19 critical_value_2 <- z_half_alpha
20
21 if(z_value >= critical_value_2 || z_value <=
22   critical_value_1)
23 {
24   cat("Since z-value", z_value, "does not lie in the
25       range", critical_value_1, "and", critical_
26       value_2
27       , "therefore we reject the null hypothesis and
28       accept the alternative hypothesis.")
29 }
30                                     # Page no. :
31                                     363 – 364
32 ## P-value approach
33

```

```

34 area_under_curve <- 1 - pnorm(z_value)
35 pval <- 2 * area_under_curve # P-value
36 if(pval > 0.05)
37 {
38   cat("Since p-value ",pval," is greater than 0.05 ,
39 therefore we will accept null hypothesis")
40 } else {
41   cat("Since p-value ",pval," is less than 0.05 ,
42 therefore we will reject null hypothesis and
accept
43   alternative hypothesis.")
44 }
```

---

**R code Exa 9.1c** Relationship between Interval Estimation and Hypothesis Testing

```

1 # Page no. :
2 # 366 – 367
3 # Relationship between Interval Estimation and
Hypothesis Testing
4
5 mu <- 295
6 alpha <- 0.05
7 n <- 50
8 xbar <- 297.6
9 sigma <- 12
10
11 z_value <- 1.96 # alpha = 0.05 so alpha/2 = 0.05 /
2 = 0.025 (z-value is for 0.025)
12
13 # 95% Confidence Interval
14
15 margin_of_error <- z_value * (sigma / sqrt(n))
16
```

```

17 IE <- xbar + c(-margin_of_error, margin_of_error) #  

    Interval Estimate  

18  

19 cat("Interval estimate for 95% Confidence Interval  

    is", IE)  

20  

21 if(mu >= IE[2] || mu <= IE[1])  

22 {  

23     cat("Null Hypothesis is rejected . . .")  

24 } else{  

25     cat("Null Hypothesis cannot be rejected . . .")  

26 }

```

---

### R code Exa 9.2a Population Mean Sigma Unknown One Tailed Test

```

1                                     # Page no. :  

                                         371 –  

                                         372  

2  

3 # Population Mean Sigma Unknown One Tailed Test  

4  

5 mu0 <- 7  

6 alpha <- 0.05  

7 xbar <- 7.25  

8 s <- 1.052  

9 n <- 60  

10  

11 t_value <- (xbar - mu0) / (s / sqrt(n))  

12  

13 df <- n - 1  

14  

15 # Upper Tail Test  

16  

17 pval <- pt(t_value, df = df, lower.tail = F)    # Book  

    answer is 0.354

```

```

18
19 if(pval > alpha)
20 {
21   cat("Since p-value ",pval , " is greater than 0.05 ,
22 therefore we will accept null hypothesis")
22 } else {
23   cat("Since p-value ",pval , " is less than 0.05 ,
24 therefore we will reject null hypothesis and
25 accept
25   alternative hypothesis.")

```

---

### R code Exa 9.2b Population Mean Sigma Unknown Two Tailed Test

```

1 # Page no. :
2 # 372 – 373
3
4
5 mu0 <- 40
6 alpha <- 0.05
7 xbar <- 37.4
8 s <- 11.79
9 n <- 25
10
11 t_value <- (xbar - mu0) / (s / sqrt(n))
12
13 df <- n - 1 # Degree of Freedom
14
15 # Two Tail Test
16 # P – value Approach
17
18 pval <- 2 *(1 - pt(t_value,df = df,lower.tail = F))
19   # Book answer is 0.2822

```

```

20 if(pval > alpha)
21 {
22   cat("Since p-value ",pval , " is greater than 0.05 ,
23 therefore we will accept null hypothesis")
23 } else {
24   cat("Since p-value ",pval , " is less than 0.05 ,
25 therefore we will reject null hypothesis and
26 accept
27 alternative hypothesis.")
28 }
29
30 # Critical Value Approach
31
32 t_half_alpha <- qt(1 - (alpha/2),df)
33 critical_value_1 <- -t_half_alpha
34 critical_value_2 <- t_half_alpha
35
36 if(t_value >= critical_value_2 || t_value <=
37   critical_value_1)
38 {
39   cat("Since t-value", t_value , "does not lie in the
40       range", critical_value_1 , "and", critical_
41       value_2
42       , "therefore we reject the null hypothesis and
43       accept the alternative hypothesis.")
44 } else{
45   cat("Since t-value", t_value , "lies in the range",
46       critical_value_1 , "and", critical_value_2
47       , "therefore we accept the null hypothesis.")
48 }

```

---

### R code Exa 9.3a Population Proportion

1

# Page no. :  
377 – 378

```

2
3 # Population Proportion
4
5 p0 <- 0.20
6 alpha <- 0.05
7 n <- 400
8 x <- 100
9
10 p_bar <- x / n
11
12 z_value <- (p_bar - p0) / sqrt((p0*(1 - p0)) / n)
13
14 # Upper Tail Test
15
16 # P-value Approach
17
18 pval <- pnorm(z_value, lower.tail = F)
19 if(pval > alpha)
20 {
21   cat("Since p-value ", pval, " is greater than 0.05 ,\n"
22       "therefore we will accept null hypothesis")
23 } else {
24   cat("Since p-value ", pval, " is less than 0.05 ,\n"
25       "therefore we will reject null hypothesis and\n"
26       "accept\n"
27       "alternative hypothesis .")
28 }
29
30 # Critical Value Approach
31
32 z_alpha <- qnorm(1 - alpha)
33 critical_value <- z_alpha
34
35 if(z_value >= critical_value)
36 {
37   cat("Since z-value", z_value, " is greater then or\n"
38       "equal to", critical_value, " therefore we\n"
39       "reject

```

```

35      the null hypothesis and accept the alternative
            hypothesis.”)
36 } else{
37   cat(“Since z-value”, z_value ,” is less than”,
        critical_value,” therefore we accept the null
        hypothesis.”)
38 }
```

---

### R code Exa 9.4a Calculating the Probability of Type Second Errors

```

1 # Page no. :
      382 – 383
2
3 # Calculating the Probability of Type Second Errors
4
5 mu0 <- 120
6 alpha <- 0.05
7 z_value <- 1.645
8 n <- 36
9 sigma <- 12
10
11 xbar <- mu0 - z_value * (sigma / sqrt(n))
12
13 mu <- 112
14 z <- (xbar - mu) / (sigma / sqrt(n))
15
16 # Upper Tail Test
17
18 beta_value <- pnorm(z, lower.tail = F)
19
20 cat(“The type 2nd error is”,beta_value)
21
22 # Page no. : 384
23
24 xbar <- 116.71
```

```
25 mu <- 115
26 sigma <- 12
27 n <- 36
28
29 z <- (xbar - mu) / (sigma / sqrt(n))
30
31 # Upper Tail Test
32
33 beta_value <- pnorm(z, lower.tail = F)
34
35 cat("The type 2nd error is", beta_value)
```

---

### R code Exa 9.5a Determining the Sample Size

```
1 # Page no. :
2 # 389
3 # Determining the Sample Size
4
5 alpha <- 0.05
6 beta <- 0.10
7 z_alpha <- 1.645
8 z_beta <- 1.28
9 mu0 <- 120
10 mua <- 115
11 sigma <- 12
12
13 n <- ((z_alpha + z_beta)**2) * (sigma)**2 / (mu0 -
14     mua)**2 # Sample Size
15 n <- ceiling(n)
16 cat("Sampling Size is", n)
```

---

# Chapter 10

## Inference About Means and Proportions With Two Populations

**R code Exa 10.1a** Inference about the Difference between the two Population Means Sigma 1 and Sigma 2 known

```
1 # Page no. :  
2 410  
3 # Inference about the Difference between the two  
4 # Population Means Sigma 1 and Sigma 2 known  
5 sigma1 <- 9  
6 sigma2 <- 10  
7 sample_size1 <- 36  
8 sample_size2 <- 49  
9 sample_mean1 <- 40  
10 sample_mean2 <- 35  
11  
12 point_estimate <- sample_mean1 - sample_mean2  
13  
14 z_value <- qnorm(0.975) # alpha/2 = 0.05/2 = 0.025
```

```

= 1 - 0.025 = 0.975
15
16 standard_error <- sqrt(((sigma1)^2)/(sample_size1))
+ (((sigma2)^2)/(sample_size2)))
17
18 IE1 <- point_estimate + z_value*standard_error
19 IE2 <- point_estimate - z_value*standard_error
20
21 cat("The interval estimation for the given
      information at 95% confidence level is ", IE2, "to
      "
22 , IE1)

```

---

### R code Exa 10.1b Hypothesis Tests About Difference between two Means

```

1 # Page no. : 410
- 412
2
3 # Hypothesis Tests About Difference between two
   Means
4
5 sigma1 <- 10
6 sigma2 <- 10
7 alpha <- 0.05
8 n1 <- 30
9 n2 <- 40
10 xbar1 <- 82
11 xbar2 <- 78
12 D0 <- 0
13
14 z_value <- ((xbar1 - xbar2) - D0) / sqrt(((sigma1)**2/n1) + ((sigma2)**2/n2))
15
16 # P-value Approach
17

```

```

18 # Two Tail Test
19
20 pval <- 2 * pnorm(z_value, lower.tail = F)
21
22 if(pval <= alpha)
23 {
24   cat("Since P-Value",pval," is less than or equal to
25       0.05 therefore we can reject Null Hypothesis")
25 } else {
26   cat("Since P-Value",pval," is more than 0.05
27       therefore we cannot reject Null Hypothesis")
28 }
29
30 # Critical Value Approach
31 z_half_alpha <- qnorm(0.975)    # alpha/2 = 0.05/2 =
32           0.025 = 1 - 0.025 = 0.975
32 critical_value_1 <- -z_half_alpha
33 critical_value_2 <- z_half_alpha
34
35 if(z_value >= critical_value_2 || z_value <=
36     critical_value_1)
36 {
37   cat("Since Z-value",z_value," does not lie in the
38       range",critical_value_1,"to",critical_value_2,
39       " therefore we can reject Null Hypothesis")
39 } else {
40   cat("Since Z-value",z_value," lie in the range",
41       critical_value_1,"to",critical_value_2,
42       " therefore we cannot reject Null Hypothesis")
42 }

```

---

**R code Exa 10.2a** Inference about the Difference between the two Population Means Sigma 1 and Sigma 2 Unknown

```

1 # Page no. :
        415 - 417
2
3 # Inference about the Difference between the two
   Population Means Sigma 1 and Sigma 2 Unknown
4
5 s1 <- 150
6 s2 <- 125
7 n1 <- 28
8 n2 <- 22
9 xbar1 <- 1025
10 xbar2 <- 910
11
12 point_estimate <- xbar1 - xbar2
13
14 numerator <- (((s1)**2 / n1) + ((s2)**2 / n2))**2)
15 denominator <- ((1 / (n1 - 1)) * (((s1)**2 / n1)**2))
   + ((1 / (n2 - 1)) * (((s2)**2 / n2)**2))
16
17 df <- numerator / denominator # Degree of Freedom
18
19 t_value <- qt(0.975,df) # alpha/2 = 0.05/2 = 0.025
   = 1- 0.025 = 0.975
20
21 standard_error <- sqrt(((s1)^2 / (n1)) + ((s2)^2 / (n2)))
22
23 IE1 <- point_estimate + t_value*standard_error
24 IE2 <- point_estimate - t_value*standard_error
25
26 cat("The interval estimation for the given
      information at 95% confidence level is ",IE2 ,
27 " to ", IE1)

```

---

**R code Exa 10.2b** Hypothesis Tests About Difference between two Means

```

1 # Page no. :
2 # 418 -
3 # 419
4
5 x <- c(300, 280, 344, 385, 372, 360, 288, 321, 376,
6 290, 301, 283)
7 y <- c(274, 220, 308, 336, 198, 300, 315, 258, 318,
8 310, 332, 263)
9
10 DF <- data.frame(x,y)
11
12 test <- t.test(DF$x, DF$y, paired = F, alternative =
13 "greater")
14
15 test
16
17 # Upper Tail Test
18
19 if(test$p.value <= 0.05) # 95% Confidence Level
20 {
21   cat("Since P-Value",test$p.value,"is less than or
22       equal to 0.05 therefore we can reject
23           Null Hypothesis")
24 } else {
25   cat("Since P-Value",test$p.value,"is more than
26       0.05 therefore we cannot reject Null Hypothesis
27   ")
28 }

```

---

**R code Exa 10.3a** Inference About the Difference Between Two Population Means Matched samples

```

1                                     # Page no. :
2                                         424 – 425
3 # Inference About the Difference Between Two
4                                         Population Means Matched samples
5 workers <- c(1,2,3,4,5,6)
6 method_1 <- c(6.0,5.0,7.0,6.2,6.0,6.4)
7 method_2 <- c(5.4,5.2,6.5,5.9,6.0,5.8)
8 diff <- method_1 - method_2
9
10 dataFrame <- data.frame(workers, method_1, method_2,
11                           diff)
12 test <- t.test(dataFrame$method_1, dataFrame$method_
13                  2, paired = T)
14 test
15 # Two Tail Test
16
17 if(test$p.value <= 0.05)
18 {
19     cat("Since P-Value",test$p.value,"is less than or
20         equal to 0.05 therefore we can
21         reject Null Hypothesis")
22 } else {
23     cat("Since P-Value",test$p.value,"is more than
24         0.05 therefore we cannot reject Null Hypothesis
25         ")
26 }
27 IE1 <- test$conf.int[1]
28 IE2 <- test$conf.int[2]
29
30 cat("The interval estimation for the given
31     information at 95% confidence level is ",IE1 , "to

```

```
31        "",  
31        IE2)
```

---

**R code Exa 10.4a** Inference About the Difference Between Two Population Proportions

```
1                                  # Page no. :  
1                                  431  
2  
3 # Inference About the Difference Between Two  
3     Population Proportions  
4  
5 n1 <- 250  
6 n2 <- 300  
7 x1 <- 35  
8 x2 <- 27  
9 alpha <- 0.1  
10  
11 pbar1 <- x1 / n1  
12 pbar2 <- x2 / n2  
13  
14 qbar1 <- 1 - pbar1  
15 qbar2 <- 1 - pbar2  
16  
17 # Interval Estimation  
18  
19 diff_prop <- pbar1 - pbar2  
20  
21 z_half_alpha <- qnorm(0.95)    # alpha / 2 = 0.1 /  
21                                    2 = 0.05 = 0.95 (1 - 0.05)  
22  
23 margin_of_error <- z_half_alpha * sqrt((pbar1 *  
23                                qbar1)/n1 + (pbar2 * qbar2)/n2 )  
24  
25 IE1 <- diff_prop + margin_of_error
```

```

26 IE2 <- diff_prop - margin_of_error
27
28 cat("The interval estimation for the given
      information at 90% confidence level is ",IE2 , "to
      ", IE1)

```

---

**R code Exa 10.4b** Hypothesis Tests About Difference between two Proportions

```

1 # Page no. :
        432 – 433
2
3 # Hypothesis Tests About Difference between two
   Proportions
4
5 pbar1 <- 0.14
6 pbar2 <- 0.09
7 n1 <- 250
8 n2 <- 300
9 alpha <- 0.10    # Significance Level
10
11 pbar <- ((n1 * pbar1) + (n2 * pbar2)) / (n1 + n2)
      # Pooled Estimator
12
13 z_value <- (pbar1 - pbar2) / sqrt((pbar*(1 - pbar))*((1/n1)+(1/n2)))
14
15 # Two Tail Test
16
17 pval <- 2 * pnorm(z_value, lower.tail = F)
18
19 if(pval <= alpha)
20 {
21   cat("Since P-Value",pval,"is less than or equal to
      0.10 therefore we can reject Null Hypothesis")

```

```
22 } else {  
23   cat("Since P-Value",pval," is more than 0.10  
      therefore we cannot reject Null Hypothesis")  
24 }
```

---

# Chapter 11

## Inferences About Population Variances

R code Exa 11.1a Inferences About Population Variance

```
1 # Page no. :  
2 453  
3 # Inferences About the Population Variance  
4  
5 n <- 20  
6 variance <- 0.0025  
7 df <- 19  # Degrees of Freedom  
8  
9 chisq_1 <- qchisq(0.975, df)  
10 chisq_2 <- qchisq(0.025, df)  
11  
12 # Interval Estimation  
13  
14 IE1 <- sqrt((df * variance) / chisq_1)  
15 IE2 <- sqrt((df * variance) / chisq_2)  
16  
17 cat("Interval Estimation at 95% confidence interval  
for population standard deviation is", IE1,
```

18        " to" , IE2)

---

### R code Exa 11.1b Hypothesis Testing

```
1                                                                                  # Page no. :  
2                                                                                  455 - 456  
3 # Hypothesis Testing  
4  
5 n <- 24  
6 alpha <- 0.05    # Significance Level  
7 sigma0_sq <- 4  
8 variance <- 4.9  
9  
10 chisq_value <- ((n - 1) * variance) / sigma0_sq  
11  
12 df <- n - 1    # Degree of Freedom  
13  
14 # Upper Tail Test  
15  
16 # P-value Approach  
17  
18 pval <- pchisq(chisq_value, df, lower.tail = F)  
19  
20 if(pval <= alpha)  
21 {  
22     cat("Since pval",pval,"is less than or equal to  
          0.05 therefore we can reject Null Hypothesis")  
23 } else{  
24     cat("Since pval",pval,"is greater than 0.05  
          therefore we cannot reject Null Hypothesis")  
25 }  
26  
27 # Critical Value Approach  
28
```

```

29 chisqvalue <- qchisq(0.95, df)      # Chi-square value
       for 0.95 (1 - 0.05)
30
31 if(chisq_value >= chisqvalue)
32 {
33   cat("Since Chi-square value", chisq_value, "is
       greater than or equal to Chi-square value",
       chisqvalue,
       "therefore we will reject Null Hypothesis")
35 } else {
36   cat("Since Chi-square value", chisq_value, "is less
       than Chi-square value", chisqvalue,
       "therefore we cannot reject Null Hypothesis")
38 }
39
40
41                                     # Page no. :
       456 -
       457
42
43 n <- 30
44 alpha <- 0.05    # Significance Level
45 sigma0_sq <- 100
46 variance <- 162
47
48 chisq_value <- ((n - 1) * variance) / sigma0_sq
49
50 df <- n - 1    # Degree of Freedom
51
52 # Two Tail Test
53
54 # P-value Approach
55
56 pval <- 2 * pchisq(chisq_value, df, lower.tail = F)
57
58 if(pval <= alpha)
59 {
60   cat("Since pval", pval, "is less than or equal to"

```

```

    0.05 therefore we can reject Null Hypothesis")
61 } else{
62   cat("Since pval",pval,"is greater than 0.05
       therefore we cannot reject Null Hypothesis")
63 }
```

---

### R code Exa 11.2a Inferences About Two Population Variances

```

1 # Page no. :
        462 – 464
2
3 # Inferences About Two Population Variances
4
5 alpha <- 0.10 # Significance Level
6 n1 <- 26
7 n2 <- 16
8 sv1 <- 48
9 sv2 <- 20
10
11 f_value <- (sv1) / (sv2)
12
13 df1 <- n1 - 1 # Degrees of Freedom 1
14 df2 <- n2 - 1 # Degrees of Freedom 2
15
16 # Two Tail Test
17
18 # P-value Approach
19
20 pval <- 2 * pf(f_value,df1,df2,lower.tail = F)
21
22 if(pval <= alpha)
23 {
24   cat("Since pval",pval,"is less than or equal to
        0.10 therefore we can reject Null Hypothesis")
25 } else{
```

```

26   cat("Since pval",pval," is greater than 0.10
           therefore we cannot reject Null Hypothesis")
27 }
28
29 # Critical Value Approach
30
31 half_alpha <- alpha / 2
32 fval <- qf(0.95,df1,df2)    # half_alpha = 0.05 = 1
                                - 0.05 = 0.95
33
34 if(f_value >= fval)
35 {
36   cat("Since F value",f_value," is greater than or
           equal to F value",fval,
           " therefore we will reject Null Hypothesis")
38 } else {
39   cat("Since F value",f_value," is less than F value"
           ,fval,
           " therefore we cannot reject Null Hypothesis")
41 }
42
43                         # Page no. :
464
44
45 alpha <- 0.05      # Significance Level
46 n1 <- 41
47 n2 <- 31
48 sv1 <- 120
49 sv2 <- 80
50
51 f_value <- (sv1) / (sv2)
52
53 df1 <- n1 - 1      # Degrees of Freedom 1
54 df2 <- n2 - 1      # Degrees of Freedom 2
55
56 # Upper Tail Test
57
58 # P-value Approach

```

```

59
60 pval <- pf(f_value,df1,df2,lower.tail = F)
61
62 if(pval <= alpha)
63 {
64   cat("Since pval",pval,"is less than or equal to
65     0.10 therefore we can reject Null Hypothesis")
66 } else{
67   cat("Since pval",pval,"is greater than 0.10
68     therefore we cannot reject Null Hypothesis")
69 }
70
71 # Critical Value Approach
72
73 fval <- qf(0.90,df1,df2)    # alpha = 0.05 = 1 - 2
74   * 0.05 = 0.90
75
76 if(f_value >= fval)
77 {
78   cat("Since F value",f_value,"is greater than or
79     equal to F value",fval,
80     "therefore we will reject Null Hypothesis")
81 } else {
82   cat("Since F value",f_value,"is less than F value"
83     ,fval,
84     "therefore we cannot reject Null Hypothesis")
85 }

```

---

# Chapter 12

## Tests of Goodness of Fit and Independence

R code Exa 12.1a Goodness of Fit Test A Multinomial Population

```
1 # Page no. :  
2 # 474 – 476  
3 # Goodness of Fit Test A Multinomial Population  
4  
5 category <- c("Company A", "Company B", "Company C")  
6 prop <- c(0.30, 0.50, 0.20)  
7 freq1 <- c(48, 98, 54)  
8 freq2 <- c(60, 100, 40)  
9 diff <- freq1 - freq2  
10 sq_diff <- (diff)**2  
11 answer <- sq_diff / freq2  
12 DF <- data.frame(category, prop, freq1, freq2, diff,  
sq_diff, answer)  
13  
14 total_observe_freq <- sum(DF$freq1)  
15 chisq_value <- sum(DF$answer)  
16  
17 alpha <- 0.05
```

```

18 df <- nrow(DF) - 1      # Degrees of Freedom
19
20 # Upper Tail Test
21
22 # P-value Approach
23
24 pval <- pchisq(chisq_value,df,lower.tail = F)
25
26 if(pval <= alpha)
27 {
28   cat("Since pval",pval,"is less than or equal to
29       0.05 therefore we can reject Null Hypothesis")
30 } else{
31   cat("Since pval",pval,"is greater than 0.05
32       therefore we cannot reject Null Hypothesis")
33 }
34
35 # Critical Value Approach
36
37 chisqValue <- qchisq(0.95,df)    # 1 - alpha = 1 -
38     0.05 = 0.95
39
40 if(chisq_value >= chisqValue)
41 {
42   cat("Since Chi-square value",chisq_value,"is
43       greater than or equal to Chi-square value",
44       chisqValue,
45       "therefore we will reject Null Hypothesis")
46 } else {
47   cat("Since Chi-square value",chisq_value,"is less
48       than Chi-square value",chisqValue,
49       "therefore we cannot reject Null Hypothesis")
50 }

```

---

### R code Exa 12.2a Tests of Independence

```

1 # Page no. :
2 # 480 - 482
3 # Tests of Independence
4
5 gender <- c("Male", "Female")
6 light <- c(20,30)
7 regular <- c(40,30)
8 dark <- c(20,10)
9 total <- c(80,70)
10
11 DF <- data.frame(gender, light, regular, dark, total
12 )
13 test <- chisq.test(DF[,2:4])
14 test
15
16 # Upper Tail Test
17
18 if(test$p.value <= 0.05)
19 {
20   cat("Since pval",test$p.value," is less than or
21       equal to 0.05 therefore we can reject
22       Null Hypothesis")
23 } else{
24   cat("Since pval",test$p.value," is greater than
25       0.05 therefore we cannot reject Null
26       Hypothesis")
27 }

```

---

### R code Exa 12.3a Goodness of Fit Test Poisson Distribution

```

1 # Page no. :
2 # 488 - 490

```

```

3 # Goodness of Fit Test Poisson Distribution
4
5 x <- c(0,1,2,3,4,5,6,7,8,9)
6 observed_freq <- c(2,8,10,12,18,22,22,16,12,6)
7 y <- x * observed_freq
8 e <- 2.72
9
10 mu <- sum(y) / sum(observed_freq)
11 fun_of_x <- round(((mu)**x) * (e)**(-mu) / factorial
(x), 4) # Function of x
12
13 expected_freq <- round(sum(observed_freq)*fun_of_x,
2)
14
15 diff <- observed_freq - expected_freq
16
17 sq_diff <- round((diff)**2,2)
18
19 answer <- round(sq_diff / expected_freq,2)
20
21 DF <- data.frame(x,observed_freq,expected_freq,diff,
sq_diff,answer)
22
23 total_observe_freq <- sum(DF$observed_freq)
24 total_expexted_freq <- sum(DF$expected_freq)
25
26 chisq_value <- sum(DF$answer)
27
28 df <- nrow(DF) - 2 # Degrees of Freedom (k - p - 1
where k = 10, p = 1)
29
30 alpha <- 0.05
31
32 # Upper Tail Test
33
34 # P-value Approach
35
36 pval <- pchisq(chisq_value,df,lower.tail = F)

```

```

37
38 if(pval <= alpha)
39 {
40   cat("Since pval",pval," is less than or equal to
41       0.05 therefore we can reject Null Hypothesis")
41 } else{
42   cat("Since pval",pval," is greater than 0.05
43       therefore we cannot reject Null Hypothesis")
43 }
44
45 # In Book it is taken 9 categories but we consider
46      10 so p-value may vary but answer is correct

```

---

### R code Exa 12.3b Goodness of Fit Test Normal Distribution

```

1                                     # Page no. :
2                                         491 – 494
3
4
5 data <- c
6           (71,66,61,65,54,93,60,86,70,70,73,73,55,63,56,62,76,54,82,79,76,68,
7
8           61,61,64,65,62,90,69,76,79,77,54,64,74,65,65,61,56,63,80,56)
9
10
11 xbar <- mean(data)
12 s <- sd(data)
13
14 cat("Value of mean is",xbar)
15 cat("Value of standard variance is",s)
16
17 percentage <- c(0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.9)
18 z <- c()
19 test_score <- c()

```

```

17
18 for (i in 1:length(percentage)) {
19   z[i] <- round(qnorm(percentage[i]),2)
20   test_score[i] <- round(xbar + (z[i] * round(s,2)),
21                           2)
21 }
22
23 DF <- data.frame(percentage, z, test_score)
24
25 interval <- c("Less than 55.10", "55.10 to 59.68", "
26           59.68 to 63.01", "63.01 to 65.82",
27           "65.82 to 68.42", "68.42 to 71.02", "
28           71.02 to 73.83", "73.83 to 77.16",
29           "77.16 to 81.74", "81.74 and over")
30
31 diff <- observed_freq - expected_freq
32 sq_diff <- (diff)**2
33
34 answer <- (sq_diff) / expected_freq
35
36 dataset <- data.frame(interval, observed_freq,
37                         expected_freq, diff, sq_diff, answer)
38
39 chisq <- sum(dataset$answer)
40
41 alpha <- 0.10    # Significance Level
42 df <- nrow(dataset) - 3    # Degrees of Freedom (k -
43                           p - 1 where k = 10, p = 2)
44
45 # Upper Tail Test
46
47 # P-value Approach
48 pval <- pchisq(chisq,df,lower.tail = F)
49

```

```
50 if(pval <= alpha)
51 {
52   cat("Since pval",pval,"is less than or equal to
      0.05 therefore we can reject Null Hypothesis")
53 } else{
54   cat("Since pval",pval,"is greater than 0.05
      therefore we cannot reject Null Hypothesis")
55 }
```

---

# Chapter 13

## Experimental Design and Analysis of Variance

**R code Exa 13.1a** Analysis of Variance and the Completely Randomized Design

```
1 # Page no. :  
2 # 510 - 512  
3 # Analysis of Variance and the Completely Randomized  
4 # Design  
5 method_A <- c(58,64,55,66,67)  
6 method_B <- c(58,69,71,64,68)  
7 method_C <- c(48,57,59,47,49)  
8  
9 DF <- data.frame(method_A,method_B,method_C)  
10  
11 mean1 <- sum(DF$method_A) / nrow(DF) # Sample Mean  
12 mean2 <- sum(DF$method_B) / nrow(DF) # Sample Mean  
13 mean3 <- sum(DF$method_C) / nrow(DF) # Sample Mean  
14
```

```

14
15 variance1 <- sum((DF$method_A - mean1)**2) / (nrow(
16   DF)-1) # Sample Variance 1
16 variance2 <- sum((DF$method_B - mean2)**2) / (nrow(
17   DF)-1) # Sample Variance 2
17 variance3 <- sum((DF$method_C - mean3)**2) / (nrow(
18   DF)-1) # Sample Variance 3
18
19 sd1 <- sqrt(variance1) # Sample Standard Variance
20   1
20 sd2 <- sqrt(variance2) # Sample Standard Variance
21   2
21 sd3 <- sqrt(variance3) # Sample Standard Variance
22   3
22
23 sample_mean <- (mean1 + mean2 + mean3) / 3 # Overall Sample Mean
24
25 variance <- ((mean1 - sample_mean)**2 + (mean2 -
26   sample_mean)**2 + (mean3 - sample_mean)**2) /
27   (3 - 1)
26 # Sample Varince for Overall Sample Mean (3 -->
27   Methods)
27
28 sigma_sq <- nrow(DF) * variance # Between-
29   treatment Estimate of Sigma Square
30
30 estimate_sigma_sq <- (variance1 + variance2 +
31   variance3) / 3 # Within-treatment Estimate of
32   Sigma Square
31
32 ratio <- sigma_sq / estimate_sigma_sq
33
34 cat("Ratio of Between-treatment Estimate of Sigma
35   Square by Within-treatment Estimate
36   of Sigma Square is",ratio)

```

---

**R code Exa 13.2a** Analysis of Variance and the Completely Randomized Design

```
1 # Page no. : 518
2
3 # Analysis of Variance and the Completely Randomized Design
4
5 method_A <- c(58,64,55,66,67)
6 method_B <- c(58,69,71,64,68)
7 method_C <- c(48,57,59,47,49)
8
9 DF <- data.frame(method_A,method_B,method_C)
10
11 k <- ncol(DF)    # Number of Treatments
12 n <- nrow(DF)    # Number of Observations for each Treatment
13 N <- n * k      # Total Observations
14
15 df_numerator <- k - 1    # Degrees of Freedom for Numerator
16 df_denomenator <- N - k    # Degrees of Freedom for Denomenator
17
18 alpha <- 0.05
19
20 x <- c(t(as.matrix(DF)))
21 f <- c("method_A", "method_B", "method_C")
22 tm <- gl(k, 1, n*k, factor(f))
23 result <- anova(lm(x ~ tm))    # Similar to aov(x ~ tm)
24
25 result
26
```

```

27 # Upper Tail Test
28
29 # Critical Value Approach
30
31 fval <- qf(0.95, df_numerator, df_denomenator) # 1
   - alpha = 1 - 0.05 = 0.95
32 fval <- round(fval, 2)
33
34 fvalue <- result$`F value`[1]
35
36 if(fvalue >= fval)
37 {
38   cat("Since F value", fvalue, "is greater than or
      equal to F value", fval,
      "therefore we will reject Null Hypothesis")
39 } else {
40   cat("Since fvalue value", fvalue, "is less than
      fvalue value", fval,
41         "therefore we cannot reject Null Hypothesis")
42 }
43
44
45 # P-value Approach
46
47 pval <- pf(fvalue, df_numerator, df_denomenator, lower.
   tail = F)
48
49 if(pval <= alpha)
50 {
51   cat("Since pval", pval, "is less than or equal to
      0.05 therefore we can reject Null Hypothesis")
52 } else{
53   cat("Since pval", pval, "is greater than 0.05
      therefore we cannot reject Null Hypothesis")
54 }

```

---

### R code Exa 13.3a Multiple Comparison Procedures Fishers LSD

```
1 # Page no. : 525  
# - 526  
2  
3 # Multiple Comparison Procedures : Fisher ' s LSD  
4  
5 method_A <- c(58,64,55,66,67)  
6 method_B <- c(58,69,71,64,68)  
7 method_C <- c(48,57,59,47,49)  
8  
9 DF <- data.frame(method_A,method_B,method_C)  
10  
11 k <- ncol(DF)      # Number of Treatments  
12 n <- nrow(DF)      # Number of Observations for each  
Treatment  
13 N <- n * k      # Total Observations  
14  
15 x <- c(t(as.matrix(DF)))  
16 f <- c("method_A" , "method_B" , "method_C")  
17 tm <- gl(k, 1, n*k, factor(f))  
18 result <- anova(lm(x ~ tm))    # Similar to aov(x ~  
tm)  
19  
20 # Approach - 1  
21  
22 # Fisher ' s LSD Procedure for Method A and Method B  
23  
24 t_value1 <- (mean(DF$method_A) - mean(DF$method_B))  
/ sqrt(result$'Mean Sq'[2] * ((1 / n)  
25
```

```

26
27 t_value1 <- round(t_value1, 2)
28
29 df <- N - k    # Degrees of Freedom
30
31 # Two Tail Test
32
33 # P-value Approach
34
35 alpha <- 0.05
36
37 pval <- 2 * pt(t_value1, df, lower.tail = T)
38
39 if(pval <= alpha)
40 {
41   cat("Since pval",pval,"is less than or equal to
42       0.05 therefore we can reject Null Hypothesis")
43 } else{
44   cat("Since pval",pval,"is greater than 0.05
45       therefore we cannot reject Null Hypothesis")
46 }
47
48 tval <- qt(0.975,df)      # alpha/2 = 0.05 / 2 =
49      0.025 = (1 - 0.025) = 0.975
50 tval <- round(tval, 3)
51
52 LSD <- tval * sqrt(result$`Mean Sq`[2] * ((1 / n) +
53      (1 / n)))
54 LSD <- round(LSD, 2)
55
56 # Approach - 2
57
58 # Fisher 's LSD Procedure for Method A and Method C
59
60 diff_A_C <- mean(DF$method_A) - mean(DF$method_C)

```

```

57
58 if(diff_A_C > LSD)
59 {
60   cat("Since the value of difference", diff_A_C,"is
       greater than LSD",LSD,"therefore we will reject
       Null Hypothesis")
61 } else{
62   cat("Since the value of difference", diff_A_C,"is
       less than LSD",LSD,"therefore we cannot reject
       Null Hypothesis")
63 }
64
65 }
66
67 # Fisher 's LSD Procedure for Method B and Method C
68
69 diff_B_C <- mean(DF$method_B)- mean(DF$method_C)
70
71 if(diff_B_C > LSD)
72 {
73   cat("Since the value of difference", diff_B_C,"is
       greater than LSD",LSD,"therefore we will reject
       Null Hypothesis")
74 } else{
75   cat("Since the value of difference", diff_B_C,"is
       less than LSD",LSD,"therefore we cannot reject
       Null Hypothesis")
76 }
77
78 }

```

---

### R code Exa 13.4a Randomized Block Design

```

1 # Page no. :
2 # 534
3 # Randomized Block Design
4
5 blocks <- c("Controller 1", "Controller 2", "

```

```

Controller 3", "Controller 4", "Controller 5", "
Controller 6")
6 system_A <- c(15, 14, 10, 13, 16, 13)
7 system_B <- c(15, 14, 11, 12, 13, 13)
8 system_C <- c(18, 14, 15, 17, 16, 13)
9
10 DF <- data.frame(blocks, system_A, system_B, system_
C)
11
12 k <- ncol(DF) - 1 # Number of Treatments (blocks
# is not the treatment)
13 b <- nrow(DF) # Number of blocks
14 N <- k * b # Total sample Size
15
16 x <- c(t(as.matrix(DF[, -1])))
17 f <- c("system_A", "system_B", "system_C")
18 tm <- gl(k, 1, N, factor(f))
19 blk <- gl(b, k, N)
20 result <- anova(lm(x ~ tm + blk)) # Similar to aov
(x ~ tm)
21
22 result
23
24 f_value <- result$`F value`[1]
25
26 # Upper Tail Test
27
28 # P-value Approach
29
30 pval <- result$`Pr(>F)`[1]
31
32 if(pval <= 0.05)
33 {
34   cat("Since pval", pval, "is less than or equal to
0.05 therefore we can reject Null Hypothesis")
35 } else{
36   cat("Since pval", pval, "is greater than 0.05
therefore we cannot reject Null Hypothesis")

```

**R code Exa 13.5a Factorial Design**

```

1 # Page no. : 542
2
3 # Factorial Experiment
4
5 program <- c("Three-hour review", "Three-hour review",
6           "One-day program", "One-day program", "10-week
7           course",
8           "10-week course")
9 business <- c(500, 580, 460, 540, 560, 600)
10 engineering <- c(540, 460, 560, 620, 600, 580)
11 arts_and_science <- c(480, 400, 420, 480, 480, 410)
12
13 DF <- data.frame(program, business, engineering,
14                     arts_and_science)
15
16 a <- 3 # Number of levels in Factor A (Unique
17         Programs)
18 b <- 3 # Number of levels in Factor B (Columns
19         Except program)
20 r <- 2 # Number of Replications (Each Program has
21         2 Replications)
22 N <- a * b * r # Total Observations
23
24 x <- c(t(as.matrix(DF[,-1])))
25 f1 <- c("Three-hour review", "One-day program", "10-
26         week course")
27 f2 <- c("business", "engineering", "arts and science
28         ")
29 tm2 <- gl(a, 1, N, factor(f1))
30 tm1 <- gl(b, r * a, N, factor(f2))
31 result <- anova(lm(x ~ tm1 * tm2)) # Similar to

```

```

    aov(x ~ tm)
24
25 result
26
27 alpha <- 0.05
28
29 # Upper Tail Test
30
31 pval1 <- result$'Pr(>F) '[1]
32 pval2 <- result$'Pr(>F) '[2]
33 pval3 <- result$'Pr(>F) '[3]
34
35 if(pval1 <= alpha)
36 {
37   cat("Since pval",pval1," is less than or equal to
38       0.05 therefore we can reject Null Hypothesis
39       for Undergraduation.")
39 } else{
40   cat("Since pval",pval1," is greater than 0.05
41       therefore we cannot reject Null Hypothesis
42       for Undergraduation.")
42 }
43
44 if(pval2 <= alpha)
45 {
46   cat("Since pval",pval2," is less than or equal to
47       0.05 therefore we can reject Null Hypothesis
48       for programs.")
48 } else{
49   cat("Since pval",pval2," is greater than 0.05
50       therefore we cannot reject Null Hypothesis
51       for programs.")
51 }
52
53 if(pval3 <= alpha)
54 {
55   cat("Since pval",pval3," is less than or equal to
      0.05 therefore we can reject Null Hypothesis

```

```
56     for interaction.”)
57 } else{
58   cat(“Since pval”,pval3,” is greater than 0.05
      therefore we cannot reject Null Hypothesis
59     for interaction.”)
60 }
```

---

# Chapter 14

## Simple Linear Regression

R code Exa 14.1a Least Squares Method

```
1 # Page no. : 565  
# - 566  
2  
3 # Least Squares Method  
4  
5 restaurant <- c(1,2,3,4,5,6,7,8,9,10)  
6 student_population <- c(2,6,8,8,12,16,20,20,22,26)  
7 quartely_sales <- c  
    (58,105,88,118,117,137,157,169,149,202)  
8  
9 DF <- data.frame(restaurant, student_population,  
    quartely_sales)  
10  
11 # Install Library if not installed  
12  
13 # install.packages("ggplot2")  
14  
15 # Import Library  
16  
17 library(ggplot2)  
18
```

```

19 ggplot(DF,aes(student_population , quartely_sales)) +
  geom_point() +
20   labs(title = "Scatter Plot between Student
    Population and Quartely Sales",x = "Student
    Population (1000s)", y = "Quartely Sales ($
    1000s)") +
21
22
23                                     # Page no. : 567 -
24                                     569
25
26 regressor <- lm(quartely_sales ~ student_population ,
  data = DF)
27 res <- summary(regressor)
28
29 res
30 b1 <- res$coefficients [[2]]
31
32 b0 <- res$coefficients [[1]]
33
34 cat("Estimated Regression Equation is y_cap =",b0,"+
  ",b1,"x")
35
36 ggplot(DF,aes(student_population , quartely_sales)) +
  geom_point() +
37   geom_smooth(method='lm' , se = F) + labs(title = "
    Scatter Plot between Student Population
  and Quartely Sales",x = "Student Population (1000s)"
  , y = "Quartely Sales ($1000s)")
```

---

### R code Exa 14.2a Coefficient of Determination

```

1                                     # Page no. :
2                                     576 -
3                                     580
```

```

2
3 # Coefficient of Determination
4
5 restaurant <- c(1,2,3,4,5,6,7,8,9,10)
6 student_population <- c(2,6,8,8,12,16,20,20,22,26)
7 quartely_sales <- c
8     (58,105,88,118,117,137,157,169,149,202)
9
10 DF <- data.frame(restaurant, student_population,
11                     quartely_sales)
12
13 regressor <- lm(quartely_sales ~ student_population,
14                     data = DF)
15 res <- summary(regressor)
16
17 table <- anova(regressor)
18
19 SSE <- table$`Sum Sq`[2]      # Sum of Squares due to
20             Error
21
22 cat("Value of SSE is",SSE)
23
24 SSR <- table$`Sum Sq`[1]      # Sum of Squares due to
25             Regression
26
27 SST <- SSE + SSR      # Total Sum of Squares
28
29 cat("Value of SST is",SST)
30
31 r_sq <- res$r.squared      # Coefficient of
32             Determination
33 corrcoeff <- sqrt(r_sq)      # Correlation Coefficient
34
35 cat("Value of Coefficient of Determination is",r_sq)
36 cat("Value of correlation Coefficient is",corrcoeff)

```

---

### R code Exa 14.3a Test of Significance

```
1 # Page no. :
  485 - 489
2
3 # Test of Significance
4
5 restaurant <- c(1,2,3,4,5,6,7,8,9,10)
6 student_population <- c(2,6,8,8,12,16,20,20,22,26)
7 quartely_sales <- c
  (58,105,88,118,117,137,157,169,149,202)
8
9 DF <- data.frame(restaurant, student_population,
quartely_sales)
10
11 regressor <- lm(quartely_sales ~ student_population,
  data = DF)
12 res <- summary(regressor)
13
14 standard_error_MSE <- res$sigma
15
16 cat("Value of square root of MSE is",standard_error_
MSE)
17
18 b1 <- res$coefficients [2]
19
20 tval <- res$coefficients [6]
21
22
23 # T Test
24
25 # Two Tail Test
26
27 # P-value Approach
```

```

28
29 pval <- round(res$coefficients[8],3)
30
31 if(pval >= 0.01)
32 {
33   cat("Since pval",pval,"is greater than or equal to
34 } else{
35   cat("Since pval",pval,"is less than 0.01 therefore
36 }
37 }
38
39 # F Test
40
41 test <- anova(regressor)
42
43 fval <- test$'F value'
44
45 pval <- round(test$'Pr(>F')[1],3)    # P value is
46   extremely small ie negligible to 0
47 if(pval >= 0.01)
48 {
49   cat("Since pval",pval,"is greater than or equal to
50 } else{
51   cat("Since pval",pval,"is less than 0.01 therefore
52 }
53 }
54
55 # Confidence Interval
56
57 confidence <- confint(regressor, "student_population
58   ", level = 0.99)

```

```
58 IE1 <- confidence[1]
59 IE2 <- confidence[2]
60
61 cat("The 99 % confidence interval is ", IE1, " to ",
IE2)
```

---

**R code Exa 14.4a** Using the Estimated Regression Equation for Estimation and Prediction

```
1 # Page no. : 595 –
      597
2
3 # Using the Estimated Regression Equation for
      Estimation and Prediction
4
5 restaurant <- c(1,2,3,4,5,6,7,8,9,10)
6 student_population <- c(2,6,8,8,12,16,20,20,22,26)
7 quartely_sales <- c
      (58,105,88,118,117,137,157,169,149,202)
8
9 DF <- data.frame(restaurant, student_population,
      quartely_sales)
10
11 regressor <- lm(quartely_sales ~ student_population,
      data = DF)
12 res <- summary(regressor)
13
14 pred <- predict(regressor, data.frame(student_
      population=10), interval="confidence")
15
16 PE <- pred[1]
17 IE1 <- pred[2]
18 IE2 <- pred[3]
19
20 cat("Point estimate is ", PE)
```

```

21 cat("Confidence Interval is ", IE1, "to", IE2)
22
23 pred2 <- predict(regressor, data.frame(student_
    population=10), interval="predict")
24
25 IE1 <- pred2[2]
26 IE2 <- pred2[3]
27
28 cat("Prediction Confidence Interval is ", IE1, "to",
    IE2)

```

---

### R code Exa 14.5a Residual Analysis Validating Model Assumptions

```

1 # Page no. : 605
   - 609
2
3 # Residual Analysis : Validating Model Assumptions
4
5 x <- c(2,6,8,8,12,16,20,20,22,26) # Student
   Population
6 y <- c(58,105,88,118,117,137,157,169,149,202) #
   Sales
7
8 estimated_sales <- 60 + (5 * x) # Regression
   Equation = 60 + 5 x
9
10 residuals <- y - estimated_sales
11
12 DF <- data.frame(x, y, estimated_sales, residuals)
13
14 # Install Library if not installed
15
16 # install.packages("ggplot2")
17
18 # Import Library

```

```

19
20 library(ggplot2)
21
22 ggplot(DF,aes(x, residuals)) + geom_point() + geom_
23     hline(yintercept = 0, linetype=2) +
24 labs(title = "Residual Plot", x = "X", y = "Residual
25 ")
26
27 ggplot(DF,aes(estimated_sales, residuals)) + geom_
28     point() + geom_hline(yintercept = 0,
29         linetype=2) + labs(title = "Plot between
30             Estimated Sales and Residuals", x =
31                 "Estimated Sales", y =
32                     "Residual")

```

---

### R code Exa 14.5b Standardized Residuals

```

1 # Page no. : 610 –
2
3 # Standardized Residuals
4
5 i <- c(1,2,3,4,5,6,7,8,9,10)
6 x <- c(2,6,8,8,12,16,20,20,22,26)    # Student
7 n <- 10
8 s <- 13.829    # Standard error
9 y <- c(58,105,88,118,117,137,157,169,149,202)    #
10 Sales
11 estimated_sales <- 60 + (5 * x)    # Regression
12 Equation = 60 + 5 x
13 x_deviation <- x - mean(x)
14

```

```

15 x_deviation_sq <- (x_deviation)**2
16
17 z <- round(x_deviation_sq / sum(x_deviation_sq),4)
18
19 h <- round((1 / n) + z, 4)
20
21 s_i <- round(s * sqrt(1 -h), 4)    # Standard
                                         Deviation for Residual i
22
23 residuals <- y - estimated_sales
24
25 standard_residuals <- round((residuals) / (s_i), 4)
26
27 DF <- data.frame(x, y, estimated_sales, x_deviation,
                     x_deviation_sq, z, h, s_i, residuals, standard_
                     residuals)
28
29 # Install Library if not installed
30
31 # install.packages("ggplot2")
32
33 # Import Library
34
35 library(ggplot2)
36
37 ggplot(DF,aes(x, standard_residuals)) + geom_point()
       + geom_hline(yintercept = 0, linetype=2) +
38   labs(title = "Scatter Plot between x and
         Standard Residuals", x = "X",
         y = "Standard Residuals")
39
40
41 normal_scores <- round(qqnorm(1:10)$x, 2)
42 standard_residuals <- sort(standard_residuals,
                             decreasing = F)
43
44 table <- data.frame(normal_scores, standard_
                           residuals)
45

```

```
46 ggplot(table,aes(normal_scores, standard_residuals))  
+ geom_point() +  
47 geom_smooth(method = "lm", se = F) +  
48 labs(title = "Scatter Plot between Normal Scores and  
Standard Residuals", x = "Normal Scores",  
49 y = "Standard Residuals")
```

---

### R code Exa 14.6a Detecting Outliers

```
1 # Page no. : 615  
2  
3 # Detecting Outliers  
4  
5 x <- c(1,1,2,3,3,3,4,4,5,6)  
6 y <- c(45,55,50,75,40,45,30,35,25,15)  
7  
8 DF <- data.frame(x,y)  
9  
10 ggplot(DF,aes(x, y)) + geom_point() + geom_smooth(  
method = "lm", se = F) +  
11 labs(title = "Scatter Plot between x and Y Showing  
Outlier", x = "X", y = "Y")
```

---

### R code Exa 14.6b Detecting Influential Observations

```
1 # Page no. :  
2 617 – 618  
3  
3 # Detecting Influential Observations  
4  
5 x <- c(10, 10, 15, 20, 20, 25, 70)  
6 y <- c(135, 130, 120, 115, 120, 110, 100)  
7
```

---

```

8 DF <- data.frame(x, y)
9
10 # Install Library if not installed
11
12 # install.packages("ggplot2")
13
14 # Import Library
15
16 library(ggplot2)
17
18 ggplot(DF, aes(x, y)) + geom_point() + labs(title =
  "Scatter Plot between x and y", x = "X",
19                                     y = "Y")
20
21 point <- x[7] # From Scatter Plot
22
23 h <- (1 / nrow(DF)) + (((point - mean(DF$x))**2) / (
  sum((DF$x - mean(DF$x))**2)))
24
25 cat("Leverage at point 7 is", h)

```

---

# Chapter 15

## Multiple Regression

R code Exa 15.1a Least Squares Method

```
1 # Page no. :  
2 # 646 - 647  
3 # Least Squares Method  
4  
5 driving_assignment <- c(1,2,3,4,5,6,7,8,9,10)  
6 x <- c(100,50,100,100,50,80,75,65,90,90) # Miles  
    Traveled  
7 y <- c(9.3,4.8,8.9,6.5,4.2,6.2,7.4,6.0,7.6,6.1) #  
    Travel Time (hours)  
8  
9 DF <- data.frame(driving_assignment, x ,y)  
10  
11 # Install Library if not installed  
12  
13 # install.packages("ggplot2")  
14  
15 # Import Library  
16  
17 library(ggplot2)  
18
```

```

19 ggplot(DF,aes(x, y)) + geom_point() + labs(title = "
Scatter Plot between Miles Traveled
20 and Travel Time", x = "Miles Traveled", y = "
Travel Time in Hours")
21
22 # Page no. : 647
- 648
23
24 model <- lm(y ~ x, data = DF)
25 summ <- summary(model)
26 summ
27
28 b0 <- model$coefficients[1]
29 b1 <- model$coefficients[2]
30
31 cat("Linear Regression Equation is y_cap =",b0,"+", 
b1,"x1")
32
33 # F Test
34
35 fval <- summ$fstatistic[1]
36
37 # Upper Tail Test
38
39 # P-value Approach
40
41 alpha <- 0.05
42
43 pval <- summ$coefficients[8] # P-value
44
45 if(pval >= alpha)
46 {
47   cat("Since pval",pval,"is greater than or equal to
0.01 therefore we cannot reject the Null
Hypothesis")
48 } else{
49   cat("Since pval",pval,"is less than 0.05 therefore
we can reject the Null Hypothesis")

```

```
50  
51 }
```

---

### R code Exa 15.2a Two Independent Variables

```
1 # Page no. : 648  
# - 649  
2  
3 # Two Independent Variables  
4  
5 driving_assignment <- c(1,2,3,4,5,6,7,8,9,10)  
6 x1 <- c(100,50,100,100,50,80,75,65,90,90) # Miles  
Traveled  
7 x2 <- c(4,3,4,2,2,2,3,4,3,2) # Number of  
Deliveries  
8 y <- c(9.3,4.8,8.9,6.5,4.2,6.2,7.4,6.0,7.6,6.1) #  
Travel Time (hours)  
9  
10 DF <- data.frame(driving_assignment, x1, x2, y)  
11  
12 model <- lm(y ~ x1 + x2, data = DF)  
13 summary(model)  
14  
15 b0 <- model$coefficients[1]  
16 b1 <- model$coefficients[2]  
17 b2 <- model$coefficients[3]  
18  
19 cat("Multiple Regression Equation is y_cap =" ,b0 ,"+"  
,b1 , "x1 +" ,b2 , "x2")
```

---

### R code Exa 15.3a Multiple Coefficient of Determination

```

1 # Page no. :
2 # 654 - 655
3 # Multiple Coefficient of Determination
4
5 driving_assignment <- c(1,2,3,4,5,6,7,8,9,10)
6 x1 <- c(100,50,100,100,50,80,75,65,90,90) # Miles
7 Traveled
8 x2 <- c(4,3,4,2,2,2,3,4,3,2) # Number of
9 Deliveries
10 y <- c(9.3,4.8,8.9,6.5,4.2,6.2,7.4,6.0,7.6,6.1) # Travel Time (hours)
11
12 DF <- data.frame(driving_assignment, x1, x2, y)
13
14 model <- lm(y ~ x1 + x2, data = DF)
15 summ <- summary(model)
16
17 mean_y <- mean(DF$y) # Mean of Travel time
18
19 predicted_travel_time <- round(predict(model), 2)
20
21 DF <- cbind(DF, predicted_travel_time)
22
23 SSR <- sum((DF$predicted_travel_time - mean_y)**2)
24 # Sum of Squares due to Regression
25
26 cat("Value of SSR is", SSR)
27
28 SSE <- sum((DF$y - DF$predicted_travel_time)**2) # Sum of Squares due to Error
29
30 cat("Value of SSE", SSE)
31
32 SST <- SSR + SSE # Total Sum of Squares
33
34 cat("Value of SST", SST)
35
36

```

```

33 r_sq <- summ$r.squared # Multiple Coefficient of
   Determination
34
35 cat("Value of Multiple Coefficient of Determination
   is", r_sq)
36
37 adj_r_sq <- summ$adj.r.squared # Adjusted Multiple
   Coefficient of Determination
38
39 cat("Value of Adjusted Multiple Coefficient of
   Determination is", adj_r_sq)

```

---

### R code Exa 15.4a Testing of significance

```

1 # Page no. :
   660 - 662
2
3 # Testing for Significance
4
5 driving_assignment <- c(1,2,3,4,5,6,7,8,9,10)
6 x1 <- c(100,50,100,100,50,80,75,65,90,90) # Miles
   Traveled
7 x2 <- c(4,3,4,2,2,2,3,4,3,2) # Number of
   Deliveries
8 y <- c(9.3,4.8,8.9,6.5,4.2,6.2,7.4,6.0,7.6,6.1) # 
   Travel Time (hours)
9
10 DF <- data.frame(driving_assignment, x1, x2, y)
11
12 model <- lm(y ~ x1 + x2, data = DF)
13 summ <- summary(model)
14
15 SSR <- 21.6252 # Sum of Squares due to Regression
16
17 SSE <- 2.2952 # Sum of Squares due to Error

```

```

18
19 n <- nrow(DF)      # Total Observations
20
21 p <- 2      # Number of Independent Variables
22
23 MSR <- SSR / p    # Mean Square due to Regression
24
25 cat("Value of MSR is",MSR)
26
27 MSE <- SSE / (n - p - 1)    # Mean Square due to
28   Error
29
30 # F Test
31 fval <- summ$fstatistic[1]
32
33 alpha <- 0.01
34
35 # Upper Tail Test
36
37 # P-value Approach
38
39 pval <- summ$coefficients[11]
40
41 if(pval >= alpha)
42 {
43   cat("Since pval",pval,"is greater than or equal to
44       0.01 therefore we cannot reject the Null
45       Hypothesis")
46 } else{
47   cat("Since pval",pval,"is less than 0.01 therefore
48       we can reject the Null Hypothesis")
49
50 }
51 s <- summ$sigma    # Standard Error of the Estimate
52
53 cat("Value of Standard Error of the Estimate is",s)

```

```

52
53 coeff <- as.data.frame(summ$coefficients)
54
55 b1 <- coeff$Estimate[2]
56 b2 <- coeff$Estimate[3]
57
58 s1 <- coeff['Std. Error'][2]      # Standard Error of
      the x1 (Miles Traveled)
59 s2 <- coeff['Std. Error'][3]      # Standard Error of
      the x2 (Number of Deliveries)
60
61 df <- n - p - 1      # Degrees of Freedom
62
63 # T Test
64
65 tval1 <- round(b1 / s1, 3)
66 tval2 <- round(b2 / s2, 3)
67
68 # Upper Tail Test
69
70 # P-value Approach
71
72 pval1 <- round(pt(tval1, df, lower.tail = F), 5)
73 pval2 <- round(pt(tval2, df, lower.tail = F), 5)
74
75
76 if(pval1 >= alpha && pval2 >= alpha)
77 {
78   cat("Since pval1", pval1, "and pval2", pval2, "is
        greater than or equal to 0.01 therefore we
        cannot reject the
        Null Hypothesis")
79 } else{
80   cat("Since pval1", pval1, "and pval2", pval2, "is less
        than 0.01 therefore we can reject the Null
        Hypothesis")
81
82
83 }

```

---

### R code Exa 15.5a Categorical Independent Variables

```
1 # Page no. :  
2 # 668 - 671  
3 # Categorical Independent Variables  
4  
5 service <- c(1:10)  
6 month <- c(2,6,8,3,2,7,9,8,4,6)  
7 repair <- c("electrical","mechanical","electrical","  
8 mechanical","electrical","electrical",  
"mechanical","mechanical","electrical","  
electrical")  
9 time <- c(2.9, 3.0, 4.8, 1.8, 2.9, 4.9, 4.2, 4.8,  
4.4, 4.5)  
10  
11 DF <- data.frame(service, month, repair, time)  
12  
13 # With one Independent variable  
14  
15 regressor <- lm(time ~ month, data = DF)  
16 res <- summary(regressor)  
17  
18 res  
19  
20 b0 <- res$coefficients[1]  
21 b1 <- res$coefficients[2]  
22  
23 cat("Equation is y = ", b0 ,"+",b1,"x1")  
24  
25 # With Categorical Variable  
26  
27 DF$repair <- factor(DF$repair,  
28 levels = c('electrical', '
```

```

29               mechanical'),
30               labels = c(1, 0))
31 regressor <- lm(time ~ month + repair, data = DF)
32 res <- summary(regressor)
33
34 res
35
36 b0 <- res$coefficients[1]
37 b1 <- res$coefficients[2]
38 b2 <- res$coefficients[3]
39
40 # For Electrical Repair
41
42 bterm <- b0 + b2 * 1
43
44 cat("Equation for electrical is y = ", bterm ,"+",
45      b1,"x1" )
46 # For Mechanical Repair
47
48 bterm2 <- b0 + b2 * 0
49
50 cat("Equation for mechanical is y = ", bterm2 ,"+",
51      b1,"x1" )

```

---

### R code Exa 15.6a Residual Analysis

```

1 # Page no. :
2                         676 – 679
3 # Residual Analysis
4
5 miles <- c(100, 50, 100, 100, 50, 80, 75, 65, 90,
6      90)

```

```

6 deliveries <- c(4, 3, 4, 2, 2, 2, 3, 4, 3, 2)
7 time <- c(9.3, 4.8, 8.9, 6.5, 4.2, 6.2, 7.4, 6.0,
    7.6, 6.1)
8
9 DF <- data.frame(miles, deliveries, time)
10
11 regressor <- lm(time ~ miles + deliveries, data = DF
    )
12 res <- summary(regressor)
13
14 predict <- predict(regressor)
15 residuals <- DF$time - predict
16 std_residuals <- rstandard(regressor)
17
18 DF <- cbind(DF, predict, residuals, std_residuals)
19
20 View(DF)
21
22 # Install Library if not installed
23
24 # install.packages("ggplot2")
25
26 # Import Library
27
28 library(ggplot2)
29
30 ggplot(DF, aes(predict, std_residuals)) + geom_point
    () + geom_hline(yintercept = 0,
31     linetype=2) + labs(title = "Plot between
        predicted values and standardizes residuals
        ", x =
            "Prediction", y
            =
            "Standardization
            Residual")
32
33
34
35 leverage <- hatvalues(regressor)

```

```
36 cook_dist <- cooks.distance(regressor)
37
38 DF <- cbind(DF, leverage, cook_dist)
39
40 View(DF)
```

---

### R code Exa 15.6b Influential Observations

```
1 # Page no. :
  679 – 680
2
3 # Influential Observations
4
5 x <- c(1, 1, 2, 3, 4, 4, 5, 15)
6 y <- c(18, 21, 22, 21, 23, 24, 26, 39)
7
8 DF <- data.frame(x, y)
9
10 regressor <- lm(y ~ x, data = DF)
11 res <- summary(regressor)
12
13 lev <- hatvalues(regressor)
14 DF <- cbind(DF, lev)
15
16 View(DF)
17
18
19 # Install Library if not installed
20
21 # install.packages("ggplot2")
22
23 # Import Library
24
25 library(ggplot2)
26
```

```

27 ggplot(DF,aes(x, y)) + geom_point() + geom_smooth(
  method = "lm", se = F) +
28   labs(title = "Plot between x and y", x = "X", y =
  "Y")
29
30
31 cat("Equation is y = ",res$coefficients[1],"+",res$coefficients[2],"x1")
32
33
34 # Removing Influential Observation
35
36 x <- c(1, 1, 2, 3, 4, 4, 5)
37 y <- c(18, 21, 22, 21, 23, 24, 26)
38
39 DF <- data.frame(x, y)
40
41 regressor <- lm(y ~ x, data = DF)
42 res <- summary(regressor)
43
44 cat("Equation is y = ",res$coefficients[1],"+",res$coefficients[2],"x1")

```

---

### R code Exa 15.7a Logistic Regression

```

1 # Page no. :
  684 - 686
2
3 # Logistic Regression
4
5 customer <- c(1,2,3,4,5,6,7,8,9,10)
6 spending <- c
  (2.291,3.215,2.135,3.924,2.528,2.473,2.384,7.076,1.182,3.345)
7 card <- c(1,1,1,0,1,0,0,0,1,0)

```

```
8 coupon <- c(0,0,0,0,0,1,0,0,1,0)
9
10 DF <- data.frame(customer, spending, card, coupon)
11
12 regressor <- glm(coupon ~ spending + card, data = DF
13 )
13 summary(regressor)
14
15 # Book answer is different
```

---

# Chapter 16

## Regression Analysis Model Building

R code Exa 16.1a General Linear Model

```
1 # Page no. : 714  
# - 717  
2  
3 # General Linear Model  
4  
5 x <- c(41,106,76,10,22,12,85,111,40,51,9,12,6,56,19)  
# Months Employed  
6 y <- c  
(275,296,317,376,162,150,367,308,189,235,83,112,67,325,189)  
# Scales Sold  
7  
8 DF <- data.frame(x,y)  
9  
10 # Install Library if not installed  
11  
12 # install.packages("ggplot2")  
13  
14 # Import Library  
15
```

```

16 library(ggplot2)
17
18 ggplot(DF, aes(x,y)) + geom_point() + labs(title = "
    Scatter Plot between Months
Employed and Scales sold", x = "Months Employed",
    y = "Scales Sold")
20
21 model <- lm(y ~ x, data = DF)
22 summary(model)
23
24 b1 <- model$coefficients[1]
25 b2 <- model$coefficients[2]
26
27 cat("Regression Equation is sales =",b1,"+",b2,"
months")
28 # Book Answer is sales = 111 + 2.38 months (Data
    is wrongly used in book)
29
30 predicted_scales_sold <- predict(model)
31
32 DF <- cbind(DF, predicted_scales_sold)
33
34 # Standard Residuals
35
36 standard_residuals <- rstandard(model)
37
38 DF <- cbind(DF, standard_residuals)
39
40 ggplot(DF,aes(predicted_scales_sold, standard_
    residuals)) + geom_point() +
41     geom_hline(yintercept = 0, linetype=2) +
42     labs(title = "Scatter Plot between Predicted scales
        sold and Standard Residuals",
43         x = "Predicted scales sold", y = "Standard
        Residuals")
44
45 # Page no. :
    716 - 717

```

```

46
47 x2 <- x**2
48
49 DF2 <- data.frame(x,x2,y)
50
51 model2 <- lm(y ~ x + x2, data = DF2)
52 summary(model2)
53
54 b1 <- model2$coefficients[1]
55 b2 <- model2$coefficients[2]
56 b3 <- model2$coefficients[3]
57
58 cat("Regression Equation is sales =",b1,"+",b2,"months",
      "+",b3,"monthsq")
59 # Book Answer is sales = 45.3 + 6.34 months - 0.0345
      monthsq (Data is wrongly used in book)
60
61 predicted_scales_sold2 <- predict(model2)
62
63 DF2 <- cbind(DF2, predicted_scales_sold2)
64
65 # Standard Residuals
66
67 standard_residuals2 <- rstandard(model2)
68
69 DF2 <- cbind(DF2, standard_residuals2)
70
71 ggplot(DF2,aes(predicted_scales_sold2, standard_
      residuals2)) + geom_point() +
72     geom_hline(yintercept = 0, linetype=2) +
73     labs(title = "Scatter Plot between Predicted
      scales sold and Standard Residuals",
74           x = "Predicted scales sold", y = "Standard
      Residuals")

```

---

### R code Exa 16.1b Interaction

```
1 # Page no. : 718  
# - 721  
2  
3 # Interaction  
4  
5 price <- c(2.00, 2.50, 3.00, 2.00, 2.50, 3.00, 2.00,  
2.50, 3.00, 2.00, 2.50, 3.00,  
6 2.00, 2.50, 3.00, 2.00, 2.50, 3.00, 2.00,  
2.50, 3.00, 2.00, 2.50, 3.00)  
7 advertising <- c(50, 50, 50, 50, 50, 50, 50, 50, 50,  
50, 50, 50, 100, 100, 100, 100,  
8 100, 100, 100, 100, 100, 100, 100)  
9 sales <- c(478, 373, 335, 473, 358, 329, 456, 360,  
322, 437, 365, 342, 810, 653, 345, 832, 641,  
10 372, 800, 620, 390, 790, 670, 393)  
11  
12 DF <- data.frame(price, advertising, sales)  
13  
14 # Install Library if not install  
15  
16 # install.packages("dplyr")  
17  
18 # Import Library  
19  
20 library(dplyr)  
21  
22 DF %>% group_by(price, advertising) %>% summarize(  
Average=mean(sales))  
23  
24 model <- lm(sales ~ price + advertising + (price *  
advertising), data = DF)  
25 res <- summary(model)  
26  
27 b0 <- res$coefficients[1]  
28 b1 <- res$coefficients[2]  
29 b2 <- res$coefficients[3]
```

```

30 b3 <- res$coefficients[4]
31
32 cat("Equation is sales = ", b0, "+", b1, "Price +",
      b2, "AdvExp +", b3, "PriAdv")

```

---

### R code Exa 16.1c Transformations Involving the Dependent Variables

```

1 # Page no. : 721
   - 724
2
3 # Transformations Involving the Dependent Variables
4
5 x <- c
   (2289,2113,2180,2448,2026,2702,2657,2106,3226,3213,3607,2888)
   # Weight
6 y <- c
   (28.7,29.2,34.2,27.9,33.3,26.4,23.9,30.5,18.1,19.5,14.3,20.9)
   # Miles Per Gallon
7
8 DF <- data.frame(x,y)
9
10 # Install Library if not install
11
12 # install.packages("ggplot2")
13
14 # Import Library
15
16 library(ggplot2)
17
18 ggplot(DF, aes(x,y)) + geom_point() + labs(title = "
   Scatter Plot between Weight and Miles
19                                         Per
                                         Gallon
   ", x =
   "

```

```

Weight
", y =
"
Miles
Per
Gallon
")

20
21 model <- lm(y ~ x, data = DF)
22 summary(model)
23
24 b1 <- model$coefficients[1]
25 b2 <- model$coefficients[2]
26
27 cat("Regression Equation is sales =", b1, "+", b2, "
months")
28
29 # Prediction
30
31 predicted_miles_per_gallon <- predict(model)
32
33 DF <- cbind(DF, predicted_miles_per_gallon)
34
35 # Standard Residuals
36
37 standard_residuals <- rstandard(model)
38
39 DF <- cbind(DF, standard_residuals)
40
41
42 ggplot(DF, aes(predicted_miles_per_gallon, standard_
    residuals)) + geom_point() +
43     geom_hline(yintercept = 0, linetype=2) +
44     labs(title = "Scatter Plot between Predicted Miles
        per Gallon and Standard Residuals",
45         x = "Predicted Miles per Gallon", y = "
            Standard Residuals")
46

```

```

47 # Log Transformation
48
49 #log_x <- log(x)
50 log_y <- log(y)
51
52 DF2 <- data.frame(x, log_y)
53
54 options(scipen = 999)    # To display not in
                           scientific notation
55 model <- lm(log_y ~ x, data = DF2)
56 summary(model)
57
58 b1 <- model$coefficients[1]
59 b2 <- model$coefficients[2]
60
61 cat("Regression Equation is sales =", b1, "+", b2, "
months")
62
63 # Prediction
64
65 predicted_miles_per_gallon <- predict(model)
66
67 DF2 <- cbind(DF2, predicted_miles_per_gallon)
68
69 # Standard Residuals
70
71 standard_residuals <- rstandard(model)
72
73 DF2 <- cbind(DF2, standard_residuals)
74
75
76 ggplot(DF2, aes(predicted_miles_per_gallon, standard_
      residuals)) + geom_point() +
77   geom_hline(yintercept = 0, linetype=2) + labs(
      title = "Scatter Plot between Log
78 Transformation of Predicted Miles per Gallon and
      Standard Residuals",
79      x = "Predicted Miles per Gallon", y = "

```

Standard Residuals")

---

### R code Exa 16.2a Analysis of a Large Problem

```
1 # Page no. : 736
   - 738
2
3 # Analysis of a Large Problem
4
5 Sales <- c(3669.88, 3473.95, 2295.10, 4675.56,
6           6125.96, 2134.94, 5031.66, 3367.45, 6519.45,
7           4876.37, 2468.27, 2533.31, 2408.11,
8           2337.38, 4586.95, 2729.24, 3289.40,
9           2800.78,
10          3264.20, 3453.62, 1741.45, 2035.75,
11          1578.00, 4167.44, 2799.97)
12 Time <- c(43.10, 108.13, 13.82, 186.18, 161.79,
13          8.94, 365.04, 220.32, 127.64, 105.69, 57.72,
14          23.58,
15          13.82, 13.82, 86.99, 165.85, 116.26,
16          42.28, 52.84, 165.04, 10.57, 13.82,
17          8.13, 58.44,
18          21.14)
19 Poten <- c(74065.1, 58117.3, 21118.5, 68521.3,
20           57805.1, 37806.9, 50935.3, 35602.1, 46176.8,
21           42053.2,
22           36829.7, 33612.7, 21412.8, 20416.9,
23           36272.0, 23093.3, 26878.6, 39572.0,
24           51866.1, 58749.8,
25           23990.8, 25694.9, 23736.3, 34314.3,
26           22809.5)
27 AdvExp <- c(4582.9, 5539.8, 2950.4, 2243.1, 7747.1,
28           402.4, 3140.6, 2086.2, 8846.2, 5673.1, 2761.8,
29           1991.8, 1971.5, 1737.4, 10694.2, 8618.6,
30           7747.9, 4565.8, 6022.7, 3721.1,
```

```

861.0, 3571.5,
16           2845.5, 5060.1, 3552.0)
17 Share <- c(2.51, 5.51, 10.91, 8.27, 9.15, 0.15,
18           8.54, 7.07, 12.54, 8.85, 5.38, 5.43, 8.48, 7.80,
19           10.34, 5.15, 6.64, 5.45, 6.31, 6.35,
20           7.37, 8.39, 5.15, 12.88, 9.14)
21 Change <- c(0.34, 0.15, -0.72, 0.17, 0.50, 0.15,
22           0.55, -0.49, 1.24, 0.31, 0.37, -0.65, 0.64, 1.01,
23           0.11, 0.04, 0.68, 0.66, -0.10, -0.03,
24           -1.63, -0.43, 0.04, 0.22, -0.74)
25 Accounts <- c(74.86, 107.32, 96.75, 195.12, 180.44,
26           104.88, 256.10, 126.83, 203.25, 119.51, 116.26,
27           142.28, 89.43, 84.55, 119.51, 80.49,
28           136.58, 78.86, 136.58, 138.21,
29           75.61, 102.44,
30           76.42, 136.58, 88.62)
31 Work <- c(15.05, 19.97, 17.34, 13.40, 17.64, 16.22,
32           18.80, 19.86, 17.42, 21.41, 16.32, 14.51,
33           19.35, 20.02, 15.26, 15.87, 7.81, 16.00,
34           17.44, 17.98, 20.99, 21.66, 21.46,
35           24.78,
36           24.96)
37 Rating <- c(4.9, 5.1, 2.9, 3.4, 4.6, 4.5, 4.6, 2.3,
38           4.9, 2.8, 3.1, 4.2, 4.3, 4.2, 5.5, 3.6, 3.4,
39           4.2, 3.6, 3.1, 1.6, 3.4, 2.7, 2.8, 3.9)
40
41 DF <- data.frame(Sales, Time, Poten, AdvExp, Share,
42                     Change, Accounts, Work, Rating)
43 View(DF)
44
45 library(corrplot)
46
47 matrix <- round(cor(DF), 3)
48 matrix
49
50 regressor <- lm(Sales ~ Time + Poten + AdvExp +
51                     Share + Change + Accounts + Work + Rating,
52                     data = DF)

```

```

40 summary(regressor)
41
42 cat("Equation is Sales = ", regressor$coefficients
43   [1], "+", regressor$coefficients[2], "Time +",
44   regressor$coefficients[3], "Poten +", regressor$coefficients[4], "AdvExp +", regressor$coefficients[5],
45   "Share +", regressor$coefficients[6], "Change +",
46   regressor$coefficients[7], "Accounts +",
47   regressor$coefficients[8], "Work +", regressor$coefficients[8], "Rating")
48
49 # Book Answer is different
50
51 regressor2 <- lm(Sales ~ Poten + AdvExp + Share,
52   data = DF)
53 summary(regressor2)
54
55 cat("Equation is Sales = ", regressor2$coefficients
56   [1], "+", regressor2$coefficients[3], "Poten +",
57   regressor2$coefficients[4], "AdvExp +", regressor2$coefficients[5],
58   "Share")
59
60 # Book Answer is different

```

---

### R code Exa 16.3a Multiple Regression Approach to Experimental Design

```

1 # Page no. : 745 –
2                                         747
3 # Multiple Regression Approach to Experimental
4                                         Design
5 A <- c(58,64,55,66,67)

```

```
6 B <- c(58,69,71,64,68)
7 C <- c(48,57,59,47,49)
8
9 DF <- data.frame(A,B,C)
10
11 newA <- c(1,1,1,1,1,0,0,0,0,0,0,0,0,0,0)
12 newB <- c(0,0,0,0,0,1,1,1,1,1,0,0,0,0,0)
13 y <- c(58,64,55,66,67,58,69,71,64,68,48,57,59,47,49)
14
15 DF2 <- data.frame(newA, newB, y)
16
17 regressor <- lm(y ~ newA + newB, data = DF2)
18 summary(regressor)
19
20 cat("Equation is y = ",regressor$coefficients[1]," +"
21 ,regressor$coefficients[2],"A +",
22     regressor$coefficients[3],"B")
```

---

# Chapter 17

## Index Numbers

R code Exa 17.1a Price Relatives

```
1 # Page no. : 765
2
3 # Price Relatives
4
5 year <- c
6   (1990,1991,1992,1993,1994,1995,1996,1997,1998,1999,2000,2001,2002
7
8
9 DF <- data.frame(year,price_per_gallon)
10
11 base_year <- 1990
12 base_year_price <- DF$price_per_gallon[DF$year ==
13   base_year]
14 price_relative <- round(((DF$price_per_gallon) / (
15     base_year_price)) * 100, 2)
```

```
16 DF <- cbind(DF, price_relative)
17
18 View(DF)
```

---

### R code Exa 17.2a Aggregate Price Indexes

```
1 # Page no. :
2 766
3 # Aggregate Price Indexes
4
5 item <- c("Gallon of gasoline", "Quart of oil", "Tire",
6 , "Insurance policy")
7 year_1990 <- c(1.30, 2.10, 130.00, 820.00)
8 year_2008 <- c(3.25, 8.00, 140.00, 1030.00)
9 quantity <- c(1000, 15, 2, 1)
10 DF <- data.frame(item, year_1990, year_2008, quantity)
11
12 base_year <- 1990
13
14 sum_of_1990_items <- sum(DF$year_1990)
15
16 sum_of_2008_items <- sum(DF$year_2008)
17
18 aggregate_index_2008 <- (sum_of_2008_items / sum_of_
19 1990_items) * 100
20 cat("The unweighted aggregate index for year 2008 is
", aggregate_index_2008)
21
22
23 sum_of_1990_items <- sum(DF$year_1990 * DF$quantity)
24 # Weighted Sum
```

```

25 sum_of_2008_items <- sum(DF$year_2008 * DF$quantity)
# Weighted Sum
26
27 aggregate_index_2008 <- (sum_of_2008_items / sum_of_
1990_items) * 100
28
29 cat("The weighted aggregate index for year 2008 is",
aggregate_index_2008)

```

---

**R code Exa 17.3a** Computing an Aggregate Price Index from Price Relatives

```

1 # Page no. : 769
- 770
2
3 # Computing an Aggregate Price Index from Price
Relatives
4
5 item <- c("Gallon of gasoline","Quart of oil","Tire"
,"Insurance policy")
6 year_1990 <- c(1.30,2.10,130.00,820.00)
7 year_2008 <- c(3.25,8.00,140.00,1030.00)
8 quantity <- c(1000,15,2,1)
9
10 DF <- data.frame(item,year_1990,year_2008,quantity)
11
12 base_year <- 1990
13
14 price_relative <- (DF$year_2008 / DF$year_1990) *
100
15
16 weight <- DF$year_1990 * DF$quantity
17
18 weight_price_relative <- price_relative * weight
19

```

```

20 DF <- cbind(DF, price_relative, weight, weight_price
21           _relative)
22 aggregate_2008 <- sum(DF$weight_price_relative) /
23           sum(DF$weight)
24 cat("Aggregate Price Index for year 2008 is",
25     aggregate_2008)

```

---

### R code Exa 17.4a Deflating a Series by Price Indexes

```

1 # Page no. :
2           774
3
4
5 year <- c(2004,2005,2006,2007,2008)
6 hourly_wage <- c(15.69,16.12,16.76,17.45,18.07)
7 CPI <- c(188.9,195.3,201.6,207.3,215.3)
8
9 DF <- data.frame(year, hourly_wage, CPI)
10
11 # Install Library if not installed
12
13 # install.packages("ggplot2")
14
15 # Import Library
16
17 library(ggplot2)
18
19 ggplot(DF, aes(year, hourly_wage)) + geom_line() +
20   geom_point() +
21   labs(title = "Year V/S Hourly Wage Graph", x =
22       "Year", y = "Hourly Wage")

```

```
22
23 deflated_hourly_wage <- (DF$hourly_wage / DF$cpi) *
  100
24
25 DF <- cbind(DF, deflated_hourly_wage)
26
27 ggplot(DF, aes(year, deflated_hourly_wage)) + geom_
  line() + geom_point() +
28 ylim(c(7.75,9.0)) +
29 labs(title = "Year V/S Real Hourly Wage Graph", x
  = "Year", y = "Real Hourly Wage")
```

---

# Chapter 18

## Time Series Analysis and Forecasting

R code Exa 18.1a Time Series Patterns

```
1 # Page no. : 786  
# - 787  
2  
3 # Time Series Patterns  
4  
5 week <- c(1,2,3,4,5,6,7,8,9,10,11,12)  
6 sales <- c(17,21,19,23,18,16,20,18,22,20,15,22)  
7  
8 DF <- data.frame(week,sales)  
9  
10 # Install Library if not installed  
11  
12 # install.packages("ggplot2")  
13  
14 # Import Library  
15  
16 library(ggplot2)  
17  
18 ggplot(DF,aes(week,sales)) + geom_line() + geom_
```

```
19     point() + ylim(c(0,25)) + labs(title =
          "Week V/S Sales Time Series
          Plot", x = "Weeks", y =
          "Sales")
```

---

### R code Exa 18.1b Time Series Patterns Eg2

```
1 # Page no. : 787
   - 788
2
3 # Time Series Patterns Eg-2
4
5 week <- c
6   (1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22)
7
8 sales <- c
9   (17,21,19,23,18,16,20,18,22,20,15,22,31,34,31,33,28,32,30,29,34,33)
10
11
12 # Install Library if not installed
13
14 # Import Library
15
16 library(ggplot2)
17
18 ggplot(DF,aes(week,sales)) + geom_line() + geom_
19   point() + ylim(c(0,40)) +
labs(title = "Week V/S Sales Time Series Plot", x =
          "Weeks", y =
          "Sales")
```

---

### R code Exa 18.1c Time Series Patterns Eg3

```
1 # Page no. :  
2 # 788 - 789  
3 # Time Series Patterns Eg-3  
4  
5 year <- c(1,2,3,4,5,6,7,8,9,10)  
6 sales <- c  
    (21.6,22.9,25.5,21.9,23.9,27.5,31.5,29.7,28.6,31.4)  
7  
8 DF <- data.frame(year,sales)  
9  
10 # Install Library if not installed  
11  
12 # install.packages("ggplot2")  
13  
14 # Import Library  
15  
16 library(ggplot2)  
17  
18 ggplot(DF,aes(year,sales)) + geom_line() + geom_  
    point() + ylim(c(20,34)) +  
19 labs(title = "Years V/S Sales Time Series Plot", x  
    = "Years", y = "Sales")
```

---

### R code Exa 18.1d Time Series Patterns Eg4

```
1 # Page no. : 789  
2 # - 790
```

```

3 # Time Series Patterns Eg-4
4
5 year <- c(1,2,3,4,5,6,7,8,9,10)
6 revenue <- c
    (23.1,21.3,27.4,34.6,33.8,43.2,59.5,64.4,74.2,99.3)

7
8 DF <- data.frame(year,revenue)
9
10 # Install Library if not installed
11
12 # install.packages("ggplot2")
13
14 # Import Library
15
16 library(ggplot2)
17
18 ggplot(DF,aes(year,revenue)) + geom_line() + geom_
    point() + ylim(c(0,120)) +
19 labs(title = "Years V/S Revenue Time Series Plot",
      x = "Years", y = "Revenue")

```

---

### R code Exa 18.1e Time Series Patterns Eg5

```

1 # Page no. : 790
    - 791
2
3 # Time Series Patterns Eg-5
4
5 year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
    "Y2 Q1", "Y2 Q2", "Y2 Q3", "Y2 Q4", "Y3 Q1",
6
    "Y3 Q2", "Y3 Q3", "Y3 Q4", "Y4 Q1",
    "Y4 Q2", "Y4 Q3", "Y4 Q4", "Y5 Q1
    ", "Y5 Q2",
7
    "Y5 Q3", "Y5 Q4") # Years and

```

```

          Quarters
8 sales <- c(125, 153, 106, 88, 118, 161, 133, 102,
    138, 144, 113, 80, 109, 137, 125, 109, 130, 165,
9           128, 96)
10
11 DF <- data.frame(year_quart, sales)
12
13 # Install Library if not installed
14
15 # install.packages("ggplot2")
16
17 # Import Library
18
19 library(ggplot2)
20
21 ggplot(DF, aes(year_quart, sales, group = 1)) + geom_
    line() + geom_point() + ylim(c(0,180)) +
22   labs(title = "Years/quart V/S Sales Time Series
    Plot", x = "Year/Quarter", y = "Sales")

```

---

### R code Exa 18.1f Time Series Patterns Eg6

```

1                                     # Page no. :
2                                     791 - 792
3
4
5 year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
    "Y2 Q1", "Y2 Q2", "Y2 Q3", "Y2 Q4", "Y3 Q1",
6           "Y3 Q2", "Y3 Q3", "Y3 Q4", "Y4 Q1",
    "Y4 Q2", "Y4 Q3", "Y4 Q4")
7           # Years and Quarters
8 sales <- c(4.8, 4.1, 6.0, 6.5, 5.8, 5.2, 6.8, 7.4,
    6.0, 5.6, 7.5, 7.8, 6.3, 5.9, 8.0, 8.4)
9

```

```

10 DF <- data.frame(year_quart, sales)
11
12 # Install Library if not installed
13
14 # install.packages("ggplot2")
15
16 # Import Library
17
18 library(ggplot2)
19
20 ggplot(DF, aes(year_quart, sales, group = 1)) + geom_
  line() + geom_point() + ylim(c(0.0,9.0)) +
21   labs(title = "Years/quart V/S Sales Time Series
    Plot", x = "Year/Quarter", y = "Sales")

```

---

### R code Exa 18.2a Forecast Accuracy

```

1 # Page no. :
  793 - 795
2
3 # Forecast Accuracy
4
5 week <- c(1,2,3,4,5,6,7,8,9,10,11,12)
6 sales <- c(17,21,19,23,18,16,20,18,22,20,15,22)
7 forecast <- c(NA,17,21,19,23,18,16,20,18,22,20,15)
8
9 DF <- data.frame(week,sales,forecast)
10
11 forecast_error <- DF$sales - DF$forecast
12
13 absolute_forecast_error <- abs(forecast_error)
14
15 square_absolute_forecast_error <- absolute_forecast_
  error**2
16

```

```

17 percent_error <- round((forcast_error / DF$sales) *
18   100, 2)
19 absolute_percent_error <- abs(percent_error)
20
21 DF <- cbind(DF,forcast_error,absolute_forecast_error,
22   ,square_absolute_forcast_error,
23   percent_error,absolute_percent_error)
24 View(DF)
25
26 total_forcast_error <- sum(DF$forcast_error, na.rm =
27   T)
28 total_absolute_forcast_error <- sum(DF$absolute_
29   forecast_error, na.rm = T)
30 total_sq_abs_error <- sum(DF$square_absolute_forecast
31   _error, na.rm = T)
32 total_percent_error <- sum(DF$percent_error, na.rm =
33   T)
34 total_absolute_percent_error <- sum(DF$absolute_
35   percent_error, na.rm = T)
36 # Native Value
37
38 MAE <- round(total_absolute_forcast_error / (nrow(DF
39   )-1), 2) # Not including 1st row
40 # Mean Absolute Error
41 MSE <- round(total_sq_abs_error / (nrow(DF)-1), 2)
42 # Not including 1st row
43 # Mean Square Error
44 MAPE <- round(total_absolute_percent_error / (nrow(
45   DF)-1), 2) # Not including 1st row

```

```

45 # Mean Absolute Percent Error
46
47 cat("Value of MAE is",MAE)
48 cat("Value of MSE is",MSE)
49 cat("Value of MAPE is",MAPE)
50
51 # Average of Past Values
52
53 forcast2 <- c(NA
54 ,17.00,19.00,19.00,20.00,19.60,19.00,19.14,19.00,19.33,19.40,19.00
55
56 DF2 <- data.frame(week,sales,forcast2)
57
58 forcast_error2 <- DF2$sales - DF2$forcast2
59 absolute_forecast_error2 <- abs(forcast_error2)
60
61 square_absolute_forcast_error2 <- absolute_forecast_
62 error2**2
63 percent_error2 <- round((forcast_error2 / DF2$sales)
64 * 100, 2)
65
66 absolute_percent_error2 <- abs(percent_error2)
67
68 DF2 <- cbind(DF2,forcast_error2,absolute_forecast_
69 error2,square_absolute_forcast_error2,
70 percent_error2,absolute_percent_error2)
71
72 View(DF2)
73
74 total_forcast_error2 <- sum(DF2$forcast_error2, na.
75 rm = T)
75
74 total_absolute_forcast_error2 <- sum(DF2$absolute_
75 forecast_error2, na.rm = T)

```

```

76 total_sq_abs_error2 <- sum(DF2$square_absolute_
    forcast_error2, na.rm = T)
77
78 total_percent_error2 <- sum(DF2$percent_error2, na.
    rm = T)
79
80 total_absolute_percent_error2 <- sum(DF2$absolute_
    percent_error2, na.rm = T)
81
82 MAE2 <- round(total_absolute_forcast_error2 / (nrow(
    DF2)-1), 2) # Not including 1st row
83 # Mean Absolute Error
84
85 MSE2 <- round(total_sq_abs_error2 / (nrow(DF2)-1),
    2) # Not including 1st row
86 # Mean Square Error
87
88 MAPE2 <- round(total_absolute_percent_error2 / (nrow(
    DF2)-1), 2) # Not including 1st row
89 # Mean Absolute Percent Error
90
91 cat("Value of MAE is",MAE2)
92 cat("Value of MSE is",MSE2)
93 cat("Value of MAPE is",MAPE2)

```

---

### R code Exa 18.3a Moving Averages

```

1 # Page no. : 798
   - 799
2
3 # Moving Averages
4
5 week <- c(1,2,3,4,5,6,7,8,9,10,11,12)
6 sales <- c(17,21,19,23,18,16,20,18,22,20,15,22)
7 forcast <- c(NA,NA,NA,19,21,20,19,18,18,20,20,19)

```

```

8
9 DF <- data.frame(week,sales,forcast)
10
11 forcast_error <- DF$sales - DF$forcast
12
13 absolute_forecast_error <- abs(forcast_error)
14
15 square_absolute_forcast_error <- absolute_forecast_
    error**2
16
17 percent_error <- round((forcast_error / DF$sales) *
    100, 2)
18
19 absolute_percent_error <- abs(percent_error)
20
21 DF <- cbind(DF,forcast_error,absolute_forecast_error,
    ,square_absolute_forcast_error,
    percent_error,absolute_percent_error)
22
23
24 View(DF)
25
26 # Install Library if not installed
27
28 # install.packages("ggplot2")
29
30 # Import Library
31
32 library(ggplot2)
33
34 ggplot(DF,aes(week)) + geom_line(aes(y = forcast),
    color = "red")+
35     geom_line(aes(y = sales), color = "blue") + geom_
        point(aes(y = forcast)) +
36     geom_point(aes(y = sales))+ 
37     ylim(c(0,25)) +
38     labs(title = "Week V/S Sales Time Series Plot", x
        = "Week", y = "Sales")

```

---

### R code Exa 18.3b Exponential Smoothing

```
1 # Page no. : 802  
# - 803  
2  
3 # Exponential Smoothing  
4  
5 week <- c(1,2,3,4,5,6,7,8,9,10,11,12)  
6 sales <- c(17,21,19,23,18,16,20,18,22,20,15,22)  
7 forcast <- c(NA,17.00,17.80, 18.04, 19.03, 18.83,  
     18.26, 18.61, 18.49, 19.19, 19.35, 18.48)  
8 forcast_error <- sales - forcast  
9 forcast_error_sq <- (forcast_error)**2  
10  
11 DF <- data.frame(week, sales, forcast, forcast_error  
    , forcast_error_sq)  
12  
13 View(DF)  
14  
15 # Install Library if not installed  
16  
17 # install.packages("ggplot2")  
18  
19 # Import Library  
20  
21 library(ggplot2)  
22  
23 ggplot(DF,aes(week)) + geom_line(aes(y = forcast),  
    color = "red") +  
    geom_line(aes(y = sales), color = "blue") + geom_  
        point(aes(y = forcast)) +  
    geom_point(aes(y = sales)) +  
    ylim(c(0,25)) +  
    labs(title = "Week V/S Sales Time Series Plot", x
```

```
= "Week" , y = "Sales")
```

---

### R code Exa 18.4a Trend Projection

```
1 # Page no. :  
2 # 807 - 808  
3 # Trend Projection  
4  
5 year <- c(1,2,3,4,5,6,7,8,9,10)  
6 sales <- c  
    (21.6,22.9,25.5,21.9,23.9,27.5,31.5,29.7,28.6,31.4)  
7  
8 DF <- data.frame(year,sales)  
9  
10 # Install Library if not installed  
11  
12 # install.packages("ggplot2")  
13  
14 # Import Library  
15  
16 library(ggplot2)  
17  
18 ggplot(DF,aes(year,sales)) + geom_line() + geom_  
    point() + ylim(c(20,34)) +  
19 labs(title = "Years V/S Sales Time Series Plot", x  
    = "Years" , y = "Sales")  
20  
21 ggplot(DF,aes(year,sales)) + geom_line() + geom_  
    point() + ylim(c(20,34)) +  
22 geom_smooth(method = "lm" , se = F) +  
23 labs(title = "Years V/S Sales Time Series and  
    Linear Function Plot" , x = "Years" , y = "Sales")
```

---

### R code Exa 18.4b Trend Projection Part2

```
1 # Page no. : 809 –  
2 812  
3 # Trend Projection Part–2  
4  
5 year <- c(1,2,3,4,5,6,7,8,9,10)  
6 sales <- c  
    (21.6,22.9,25.5,21.9,23.9,27.5,31.5,29.7,28.6,31.4)  
7 forcast <- c  
    (21.5,22.6,23.7,24.8,25.9,27.0,28.1,29.2,30.3,31.4)  
8  
9 DF <- data.frame(year,sales,forcast)  
10  
11 regressor <- lm(sales ~ year, data = DF)  
12  
13 cat("Linear Trend Equation is T =",regressor$  
      coefficients[1],"+",regressor$coefficients[2],"t"  
      )  
14  
15 res <- anova(regressor)  
16  
17 cat("MSE is ",res$`Sum Sq'[2]/10)  
18  
19 cat("MSE is ",res$`Mean Sq'[2])  
20  
21 regressor  
22 res  
23  
24 # Install Library if not installed  
25
```

```

26 # install.packages("ggplot2")
27
28 # Import Library
29
30 library(ggplot2)
31
32 ggplot(DF,aes(year,sales)) + geom_line() + geom_
    point() + ylim(c(20,34)) +
33 geom_smooth(method = "lm", se = F) +
34 labs(title = "Years V/S Sales Time Series Plot", x
    = "Years", y = "Sales")

```

---

### R code Exa 18.4c Nonlinear Trend Regression

```

1 # Page no. : 814 –
     816
2
3 # Nonlinear Trend Regression
4
5 year <- c(1,2,3,4,5,6,7,8,9,10)
6 revenue <- c
    (23.1,21.3,27.4,34.6,33.8,43.2,59.5,64.4,74.2,99.3)

7 year_sq <- year**2
8
9 DF <- data.frame(year,revenue,year_sq)
10
11 # Install Library if not installed
12
13 # install.packages("gpplot2")
14
15 # Import Library
16
17 library(ggplot2)
18

```

```

19 ggplot(DF,aes(year,revenue)) + geom_line() + geom_
  point() + ylim(c(0,120)) +
20   labs(title = "Years V/S Revenue Time Series Plot",
        x = "Year", y = "Revenue")
21
22 regressor <- lm(revenue ~ year + year_sq, data = DF)
23 summary(regressor)
24 anova(regressor)
25
26 ggplot(DF,aes(year,revenue)) + geom_line() + geom_
  point() + ylim(c(0,120)) + geom_smooth(method =
27
  lm
  "
  ,
  se
  =
  F
  )
  +
28   labs(title = "Years V/S Revenue Time Series Plot",
        x = "Year", y = "Revenue")

```

---

### R code Exa 18.5a Seasonality Without Trend

```

1 # Page no. : 821
  - 822
2
3 # Seasonality Without Trend
4

```

```

5 year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
6   "Y2 Q1", "Y2 Q2", "Y2 Q3", "Y2 Q4", "Y3 Q1",
7   "Y3 Q2", "Y3 Q3", "Y3 Q4", "Y4 Q1",
8   "Y4 Q2", "Y4 Q3", "Y4 Q4", "Y5 Q1",
9   ", "Y5 Q2",
10  "Y5 Q3", "Y5 Q4") # Years and
11 quarters
12
13 # Install Library if not installed
14
15 # install.packages("ggplot2")
16
17 # Import Library
18
19 library(ggplot2)
20
21 ggplot(DF, aes(year_quart, sales, group = 1)) + geom_
22   line() + geom_point() + ylim(c(0,180)) +
23   labs(title = "Years/quart V/S Sales Time Series
24     Plot", x = "Year/Quarter", y = "Sales")
25
26 q1 <- c(1,0,0,0,1,0,0,0,1,0,0,0,0,1,0,0,0,1,0,0,0)
27 q2 <- c(0,1,0,0,0,1,0,0,0,1,0,0,0,1,0,0,0,1,0,0,0)
28 q3 <- c(0,0,1,0,0,0,1,0,0,0,1,0,0,0,1,0,0,0,1,0,0)
29 DF <- cbind(DF, q1, q2, q3)
30
31 regressor <- lm(sales ~ q1 + q2 + q3, data = DF)
32 summary(regressor)
33
34 b0 <- regressor$coefficients[1]
35 b1 <- regressor$coefficients[2]

```

```

36 b2 <- regressor$coefficients[3]
37 b3 <- regressor$coefficients[4]
38
39 cat("Equation is sales = ",b0,"+",b1,"Qtr1 +",b2,
      "Qtr2 +",b3,"Qtr3")

```

---

### R code Exa 18.5b Seasonality and Trend

```

1 # Page no. : 823 –
     824
2
3 # Seasonality and Trend
4
5 year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
   "Y2 Q1", "Y2 Q2", "Y2 Q3", "Y2 Q4", "Y3 Q1",
   "Y3 Q2", "Y3 Q3", "Y3 Q4", "Y4 Q1",
   "Y4 Q2", "Y4 Q3", "Y4 Q4")
6
7 # Years and Quarters
8 sales <- c(4.8, 4.1, 6.0, 6.5, 5.8, 5.2, 6.8, 7.4,
   6.0, 5.6, 7.5, 7.8, 6.3, 5.9, 8.0, 8.4)
9
10 DF <- data.frame(year_quart, sales)
11
12 # Install Library if not installed
13
14 # install.packages("ggplot2")
15
16 # Import Library
17
18 library(ggplot2)
19
20 ggplot(DF,aes(year_quart,sales, group = 1)) + geom_
     line() + geom_point() + ylim(c(0.0,9.0)) +
21 labs(title = "Years/quart V/S Sales Time Series
      Plot", x = "Year/Quarter", y = "Sales")

```

```

22
23 q1 <- c(1,0,0,0,1,0,0,0,1,0,0,0,1,0,0,0)
24 q2 <- c(0,1,0,0,0,1,0,0,0,1,0,0,0,1,0,0)
25 q3 <- c(0,0,1,0,0,0,1,0,0,0,1,0,0,0,1,0)
26 period <- c(1:16)
27
28 DF <- cbind(DF,q1,q2,q3,period)
29
30 regressor <- lm(sales ~ q1 + q2 + q3 + period, data
= DF)
31 summary(regressor)
32
33 b0 <- regressor$coefficients[1]
34 b1 <- regressor$coefficients[2]
35 b2 <- regressor$coefficients[3]
36 b3 <- regressor$coefficients[4]
37 b4 <- regressor$coefficients[5]
38
39 cat("Equation is sales = ",b0,"+",b1,"Qtr1 +",b2,
"Qtr2 +",b3,"Qtr3 +",b4,"t")

```

---

### R code Exa 18.6a Time Series Decomposition

```

1 # Page no. :
2 # 832 – 833
3 # Time Series Decomposition
4
5 year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
6 "Y2 Q1", "Y2 Q2", "Y2 Q3", "Y2 Q4", "Y3 Q1",
7 "Y3 Q2", "Y3 Q3", "Y3 Q4", "Y4 Q1",
8 "Y4 Q2", "Y4 Q3", "Y4 Q4")
7 # Years and Quarters
8 sales <- c(4.8, 4.1, 6.0, 6.5, 5.8, 5.2, 6.8, 7.4,
6.0, 5.6, 7.5, 7.8, 6.3, 5.9, 8.0, 8.4)

```

```

9 moving_avg <- c(NA
,5.350,5.600,5.875,6.075,6.300,6.350,6.450,6.625,6.725,6.800,6.875
10 ,7.15,NA,NA)
11 centered_avg <- c(NA,NA
,5.475,5.738,5.975,6.188,6.325,6.400,6.538,6.675,6.763,6.838,6.938
12 ,NA,NA)
13
14 DF <- data.frame(year_quart, sales,moving_avg,
centered_avg)
15
16 # Install Library if not installed
17
18 # install.packages("ggplot2")
19
20 # Import Library
21
22 library(ggplot2)
23
24 ggplot(DF,aes(year_quart, group = 1)) + geom_line(
  aes(y = sales),color = "red") +
25   geom_point(aes(y = sales)) + geom_line(aes(y =
  centered_avg),color = "blue") +
26   geom_point(aes(y = centered_avg))+ 
27   ylim(c(0.0,9.0)) +
28   labs(title = "Years/quart V/S Sales Time Series
  Plot", x = "Year/Quarter", y = "Sales")

```

---

### R code Exa 18.6b Deseasonalizing the Time Series

```

1 # Page no. : 835 -
836
2
3 # Deseasonalizing the Time Series

```

```

4
5 year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
6   "Y2 Q1", "Y2 Q2", "Y2 Q3", "Y2 Q4", "Y3 Q1",
7   "Y3 Q2", "Y3 Q3", "Y3 Q4", "Y4 Q1",
8   "Y4 Q2", "Y4 Q3", "Y4 Q4")
9
10 # Years and Quarters
11 period <- c(1:16)
12 sales <- c(4.8, 4.1, 6.0, 6.5, 5.8, 5.2, 6.8, 7.4,
13   6.0, 5.6, 7.5, 7.8, 6.3, 5.9, 8.0, 8.4)
14 index <- c
15   (0.93, 0.84, 1.09, 1.14, 0.93, 0.84, 1.09, 1.14, 0.93,
16   0.84, 1.09, 1.14, 0.93, 0.84, 1.09, 1.14, 0.93)
17
18 deseasonalized_sales <- c
19   (5.16, 4.88, 5.50, 5.70, 6.24, 6.19, 6.24, 6.49, 6.45,
20   6.67, 6.88, 6.84, 6.77
21
22   7.02, 7.34, 7.37)
23
24 DF <- data.frame(year_quart, period, sales, index,
25   deseasonalized_sales)
26
27 # Install Library if not installed
28
29 # install.packages("ggplot2")
30
31 # Import Library
32
33 library(ggplot2)
34
35 ggplot(DF, aes(year_quart, deseasonalized_sales, group
36   = 1)) + geom_line() + geom_point() +
37   ylim(c(0.0, 9.0)) +
38   labs(title = "Years/quart V/S Deseasonalized Sales
39       Time Series Plot", x = "Year/Quarter",
40       y = "Deseasonalized Sales")
41
42 regressor <- lm(deseasonalized_sales ~ period, data
43   = DF)
44
45 summary(regressor)

```

```
31 anova(regressor)
32
33 b0 <- regressor$coefficients[1]
34 b1 <- regressor$coefficients[2]
35
36 cat("Equation is deseasonalized sales = ",b0,"+",b1,
      "Period")
```

---

# Chapter 19

## Non Parametric Tests

R code Exa 19.1a Rank Correlation

```
1 # Page no. : 887  
# - 889  
2  
3 # Rank Correlation  
4  
5 sales_person <- c('A', 'B', 'C', 'D', 'E', 'F', 'G', 'H', 'I',  
  ', 'J')  
6 x <- c(2,4,7,1,6,3,10,9,8,5) # Ranking of  
  Potential  
7 y <- c(400,360,300,295,280,350,200,260,220,385) #  
  Two Years Sales  
8 z <- c(1,3,5,6,7,4,10,8,9,2) # Ranking According  
  to y  
9  
10 DF <- data.frame(sales_person,x,y,z)  
11  
12 d <- DF$x - DF$z  
13 d_sq <- d**2  
14  
15 DF <- cbind(DF,d,d_sq)  
16
```

```

17 total_d_sq <- sum(DF$d_sq)
18
19 n <- nrow(DF)
20
21 r_s <- 1 - ((6 * total_d_sq)/(n * (n**2 + 1))) #  

    Spearman Rank-Correlation Coefficient
22
23 mean_rs <- 0
24
25 sigma_rs <- sqrt(1 / (n - 1))
26
27 z_val <- (r_s - mean_rs) / sigma_rs
28
29 alpha <- 0.05
30
31 # Two Tail Test
32
33 # P-value Approach
34
35 pval <- 2 * pnorm(z_val, lower.tail = F)
36
37 if(pval >= alpha)
38 {
39     cat("Since pval",pval,"is greater than or equal to  

        0.05 therefore we cannot reject the Null  

        Hypothesis")
40 } else{
41     cat("Since pval",pval,"is less than 0.05 therefore  

        we can reject the Null Hypothesis")
42 }

```

---

### R code Exa 19.2a Sign Test

1 # Page no. : 858  
   - 861

```

2
3 # Sign Test
4
5 store <- c(56, 19, 36, 128, 12, 63, 39, 84, 102, 44)
6 sales <- c(485, 562, 415, 860, 426, 474, 662, 380,
      515, 721)
7
8 DF <- data.frame(store, sales)
9
10 median <- 450
11 sign <- c()
12
13 for (i in 1:nrow(DF)) {
14   if(DF$sales[i] >= median)
15   {
16     sign[i] = "+"
17   }else
18   {
19     sign[i] <- "-"
20   }
21 }
22
23 DF <- cbind(DF,sign)
24 View(DF)
25
26 positive <- table(DF$sign)[[2]]
27 n <- nrow(DF)
28
29 test <- binom.test(positive, n)
30 test
31
32 if(test$p.value >= 0.05)
33 {
34   cat("We cannot reject null hypothesis")
35 } else
36 {
37   cat("We can reject null hypothesis")
38 }

```

```

39
40
41 N <- 60
42 n1 <- 22    # "+ sign
43 n2 <- 38    # "- sign
44 med <- 236000
45
46 mean <- 0.50 * N
47 sd <- sqrt(0.25 * N)
48
49 CF <- 22.5    # Correction Factor
50
51 p <- pnorm(CF, mean = mean, sd = sd)
52
53 if(p >= 0.05)
54 {
55   cat("We cannot reject null hypothesis")
56 } else
57 {
58   cat("We can reject null hypothesis")
59 }

```

---

### R code Exa 19.3a Wilcoxon Signed Rank Test

```

1 # Page no. : 866 –
     868
2
3 # Wilcoxon Signed – Rank Test
4
5 worker <- c(1:11)
6 A <- c(10.2, 9.6, 9.2, 10.6, 9.9, 10.2, 10.6, 10.0,
      11.2, 10.7, 10.6)
7 B <- c(9.5, 9.8, 8.8, 10.1, 10.3, 9.3, 10.5, 10.0,
      10.6, 10.2, 9.8)
8

```

```

9 DF <- data.frame(worker, A, B)
10
11 options(warn = -1)
12
13 test <- wilcox.test(DF$A, DF$B, paired = T)
14 test
15
16 if(test$p.value >= 0.05)
17 {
18   cat("We cannot reject null hypothesis")
19 } else
20 {
21   cat("We can reject null hypothesis")
22 }

```

---

### R code Exa 19.4a Mann Whitney Wilcoxon Test

```

1 # Page no. : 873 –
2
3 # Mann – Whitney – Wilcoxon – Test
4
5 college <- c(1:4)
6 m1 <- c(15, 3, 23, 8)
7
8 high <- c(1:5)
9 m2 <- c(18, 20, 32, 9, 25)
10
11 test <- wilcox.test(m1, m2, correct = F)
12 test
13
14 if(test$p.value >= 0.05)
15 {
16   cat("We cannot reject null hypothesis")
17 } else

```

```
18 {  
19   cat("We can reject null hypothesis")  
20 }
```

---

#### R code Exa 19.4b Mann Whitney Wilcoxon Test Eg2

```
1 # Page no. :  
2 # 876-878  
3 # Mann - Whitney - Wilcoxon - Test Eg - 2  
4  
5 account1 <- c(1:12)  
6 account2 <- c(1:10)  
7  
8 balance1 <- c(1095, 955, 1200, 1195, 925, 950, 805,  
9     945, 875, 1055, 1025, 975)  
10 balance2 <- c(885, 850, 915, 950, 800, 750, 865,  
11     1000, 1050, 935)  
12  
13 test <- wilcox.test(balance1, balance2, correct = F)  
14 test  
15 if(test$p.value >= 0.05)  
16 {  
17   cat("We cannot reject null hypothesis")  
18 } else  
19 {  
20   cat("We can reject null hypothesis")  
21 }
```

---

#### R code Exa 19.5a Kruskal Wallis Test

```

1 # Page no. : 883 -
2 # 884
3 # Kruskal - Wallis Test
4
5 A <- c(25, 70, 60, 85, 95, 90, 80)
6 B <- c(60, 20, 30, 15, 40, 35)
7 C <- c(50, 70, 60, 80, 90, 70, 75)
8
9 x <- list(A,B,C)
10
11 test <- kruskal.test(x)
12 test
13
14 if(test$p.value >= 0.05)
15 {
16   cat("We cannot reject null hypothesis")
17 } else
18 {
19   cat("We can reject null hypothesis")
20 }

```

---

# Chapter 20

## Statistical Process Control

R code Exa 20.1a Sample Mean Chart Process Mean and SD Unknown

```
1 # Page no. : 913 –  
2  
3 # Sample Mean Chart : Process Mean and SD Unknown  
4  
5 o1 <- c(3.5056, 3.4882, 3.4897, 3.5153, 3.5059,  
6 3.4977, 3.4910, 3.4991, 3.5099, 3.4880, 3.4881,  
7 3.5043, 3.5043, 3.5004, 3.4846, 3.5145,  
8 3.5004, 3.4959, 3.4878, 3.4969)  
9 o2 <- c(3.5086, 3.5085, 3.4898, 3.5120, 3.5113,  
10 3.4961, 3.4913, 3.4853, 3.5162, 3.5015, 3.4887,  
11 3.4867, 3.4769, 3.5030, 3.4938, 3.4832,  
12 3.5042, 3.4823, 3.4864, 3.5144)  
13 o3 <- c(3.5144, 3.4884, 3.4995, 3.4989, 3.5011,  
14 3.5050, 3.4976, 3.4830, 3.5228, 3.5094, 3.5141,  
15 3.4946, 3.4944, 3.5082, 3.5065, 3.5188,  
16 3.4954, 3.4964, 3.4960, 3.5053)  
17 o4 <- c(3.5009, 3.5250, 3.5130, 3.4900, 3.4773,  
18 3.5014, 3.4831, 3.5083, 3.4958, 3.5102, 3.5175,  
19 3.5018, 3.5014, 3.5045, 3.5089, 3.4935,  
20 3.5020, 3.5082, 3.5070, 3.4985)
```

```

13 o5 <- c(3.5030, 3.5031, 3.4969, 3.4837, 3.4801,
14           3.5060, 3.5044, 3.5094, 3.5004, 3.5146, 3.4863,
15           3.4784, 3.4904, 3.5234, 3.5011, 3.4989,
16           3.4889, 3.4871, 3.4984, 3.4885)
17
18 sample_mean <- rowMeans(DF)
19 sample_range <- c(0.0135, 0.0368, 0.0233, 0.0316,
20           0.0340, 0.0099, 0.0213, 0.0264, 0.0270, 0.0266,
21           0.0312, 0.0259, 0.0274, 0.0230,
22           0.0243, 0.0356, 0.0153, 0.0259,
23           0.0206, 0.0259)
24
25 AR <- mean(DF$sample_range) # Average Range
26 OM <- mean(DF$sample_mean) # Overall Mean
27 n <- 5 # Sample Observations
28 d2 <- 2.362
29 A2 <- 3 / (d2 * sqrt(n))
30
31 UCL <- OM + (A2 * AR) # Upper Control Limit
32 LCL <- OM - (A2 * AR) # Lower Control Limit
33
34 cat("UCL is ", UCL)
35 cat("LCL is ", LCL)
36
37 library(qicharts2)
38
39 qic(DF$sample_mean, xlab = "Sample Number", ylab = "
40           Sample Mean", title = "Sample Mean Chart")
41 d3 <- 0.864
42
43 D1 <- 1 + (3 * (d3 / d2))
44 D2 <- 1 - (3 * (d3 / d2))

```

```

45
46 UCL2 <- AR * D1
47 LCL2 <- AR * D2
48
49 cat("UCL is ",UCL2)
50 cat("LCL is",LCL2) # Book answer is different
51
52 qic(DF$sample_range, xlab = "Sample Number", ylab =
      "Sample Range", title = "R Chart")
53
54 p <- 0.03
55 n <- 200
56
57 sigma <- sqrt((p * (1 - p)) / n)
58
59 UCL3 <- p + 3 * sigma
60 LCL3 <- p - 3 * sigma
61
62 cat("UCL is ",UCL3)
63 cat("LCL is",LCL3)
64
65 # Data for P chart is not available in Book
66
67 UCL4 <- n * p + 3 * sqrt(n * p * (1 - p))
68 LCL4 <- n * p - 3 * sqrt(n * p * (1 - p))
69
70 cat("UCL is ",UCL4)
71 cat("LCL is",LCL4)

```

---

# Chapter 21

## Decision Analysis

R code Exa 21.1a Problem Formulation

```
1 # Page no. :  
2 # 940 - 941  
3 # Problem Formulation  
4  
5 decision <- factor(c("Small Complex, d1", "Medium  
Complex, d2", "Large Complex, d3"))  
6 demand1 <- c(8, 14, 20)  
7 demand2 <- c(7, 5, -9)  
8  
9 DF <- data.frame(decision, demand1, demand2)  
10  
11 # Install Library if not install  
12  
13 install.packages("rpart")  
14 install.packages("rpart.plot")  
15  
16 # Import Library  
17  
18 library(rpart)  
19 library(rpart.plot)
```

```
20
21 ans <- rpart(decision ~ ., data = DF, method = "
22   class")
23 rpart.plot(ans)
24 # Decision Tree is Different from Book
```

---