

# Time Series Forecasting

**Objective:** To perform time series forecasting on monthly sunspot dataset as part of Lab Migration Project.

## Methods:

- (i) Import and load the dataset and check for any missing values.
- (ii) Display the summary statistics and plot the data year-wise and month-wise.
- (iii) Decompose the data as multiplicative and plot it.
- (iv) Visualize the decompose data for trend, seasonal and random patterns.
- (v) Stationarize the dataset using ADF test.
- (vi) Plot ACF and PACF.
- (vii) Build ARIMA model.
- (viii) Conclusion

```
library(forecast)

## Registered S3 method overwritten by 'quantmod':
##   method      from
## as.zoo.data.frame zoo

library(tseries)
library("anytime")
data <- read.csv('monthly-sunspots.csv')

#Display head of dataset
head(data)

##      Month Sunspots
## 1 1749-01      58.0
## 2 1749-02      62.6
## 3 1749-03      70.0
## 4 1749-04      55.7
## 5 1749-05      85.0
## 6 1749-06      83.5

#Convert data type into Date type
data$Month <- anydate(data$Month)
data$Month <- as.Date(data$Month)

#Check for unfilled data
sum(is.na(data))
```

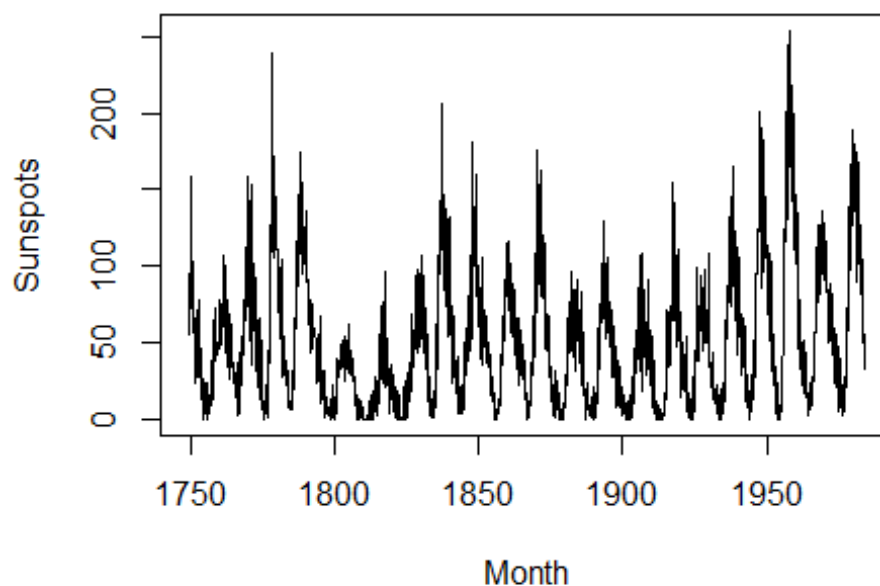
Inference: Here 0 denotes that there are no missing values in the given dataset. So, no data cleaning is required.

```
## [1] 0

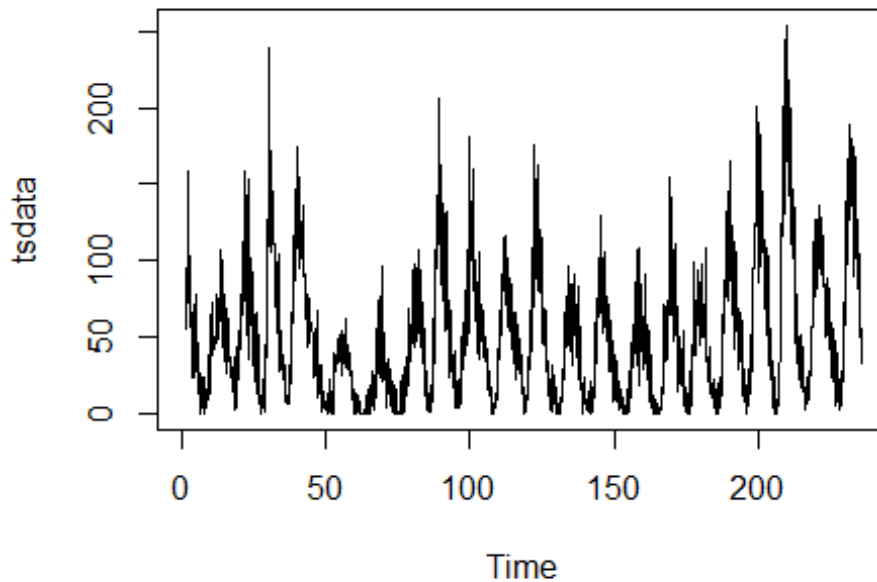
#Statistical info
summary(data)

##      Month              Sunspots
##  Min.   :1749-01-01   Min.    :  0.00
## 1st Qu.:1807-09-23   1st Qu.: 15.70
##  Median :1866-06-16   Median : 42.00
##   Mean  :1866-06-16   Mean    : 51.27
## 3rd Qu.:1925-03-08   3rd Qu.: 74.92
##   Max.  :1983-12-01   Max.    :253.80

plot(data,type="l")
```



```
#Plot as timeseries data
tsdata <- ts(data$Sunspots,frequency=12)
plot(tsdata)
```



Inference: The graphs denote that the monthly count of the number of observed sunspots increases and decreases over time with each year.

```
#Decompose the data as multiplicative
ddata <- decompose(tsdata, "multiplicative")
```

We will decompose the time series for estimates of trend, seasonal, and random components using moving average method.

The multiplicative model is:

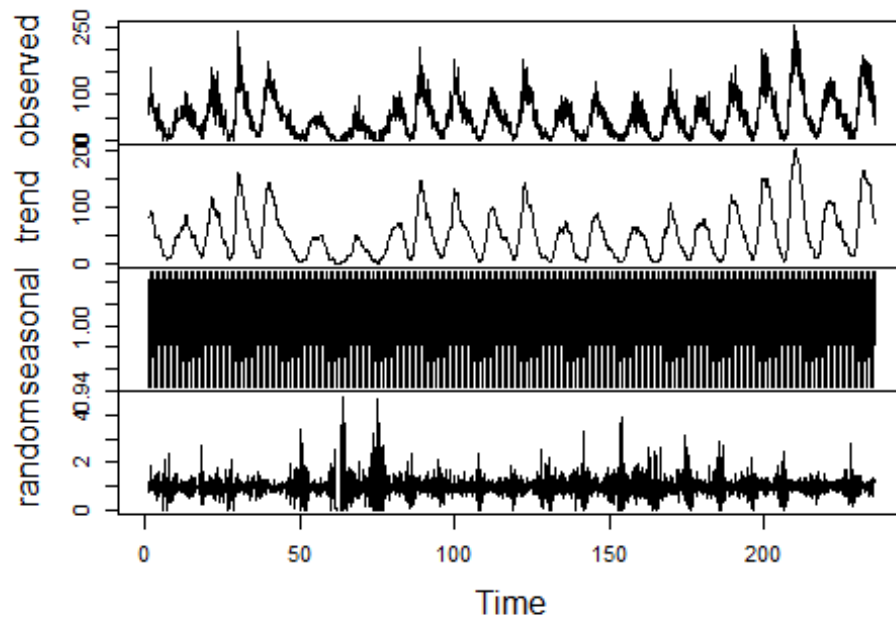
$$Y[t] = T[t] * S[t] * e[t]$$

where

- $Y(t)$  is the number of passengers at time  $t$ ,
- $T(t)$  is the trend component at time  $t$ ,
- $S(t)$  is the seasonal component at time  $t$ ,
- $e(t)$  is the random error component at time  $t$ .

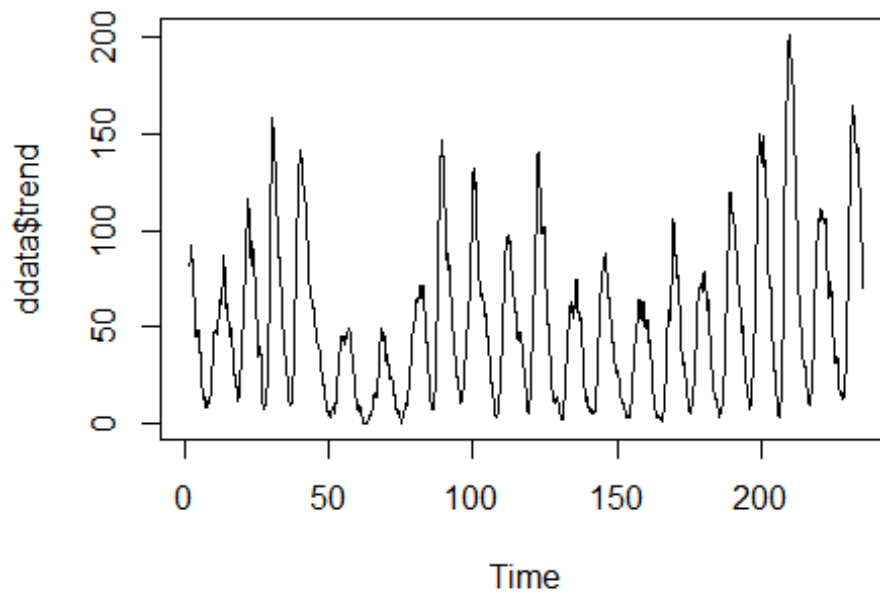
```
plot(ddata)
```

## Decomposition of multiplicative time series

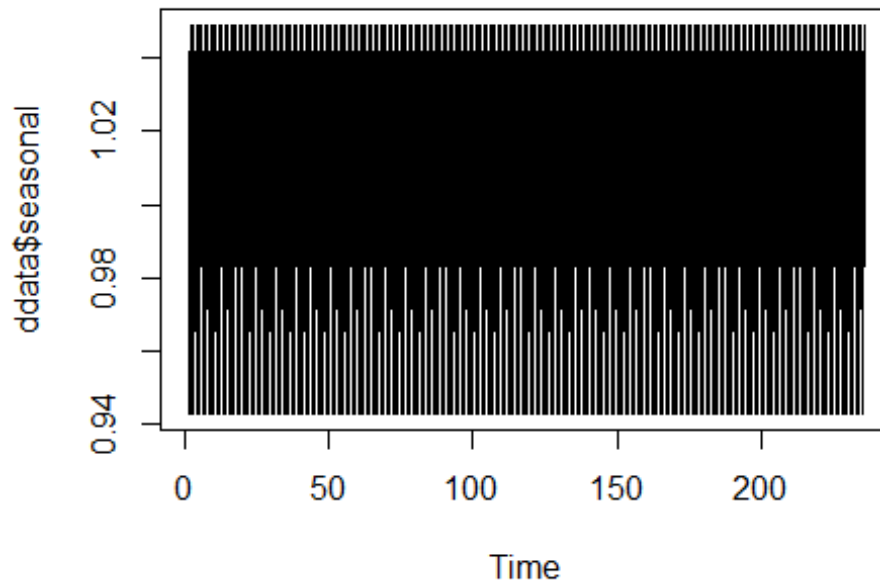


Inference: The decomposed plots show the trend and seasonality.

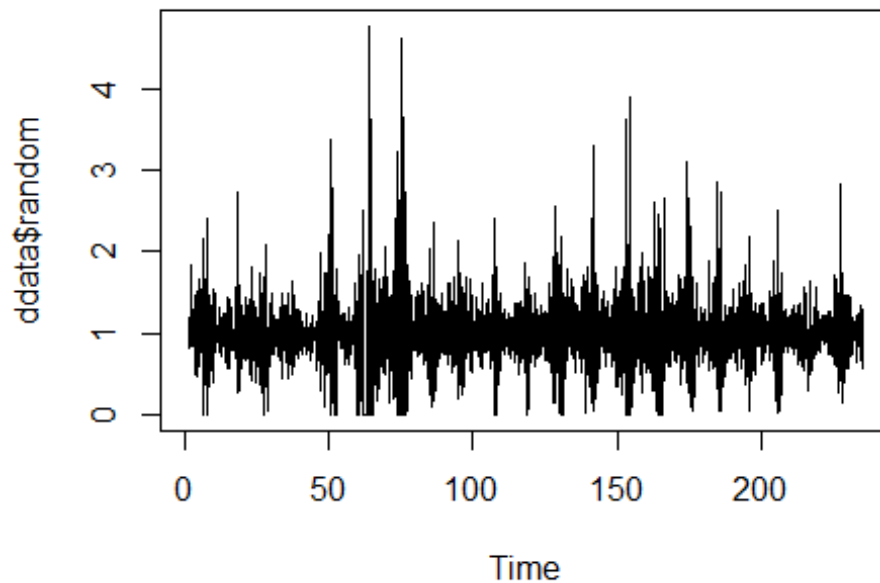
```
plot(ddata$trend)
```



```
plot(ddata$seasonal)
```



```
plot(ddata$random)
```



```
#ADF test for stationarity
```

```
adf.test(data$Sunspots)
```

```
## Warning in adf.test(data$Sunspots): p-value smaller than printed p-value
```

```
##
```

```
## Augmented Dickey-Fuller Test
```

```
##
```

```
## data: data$Sunspots
```

```
## Dickey-Fuller = -6.494, Lag order = 14, p-value = 0.01
## alternative hypothesis: stationary
```

To test the stationarity of the time series, we run the Augmented Dickey-Fuller Test using the `adf.test()` function from the `tseries` package.

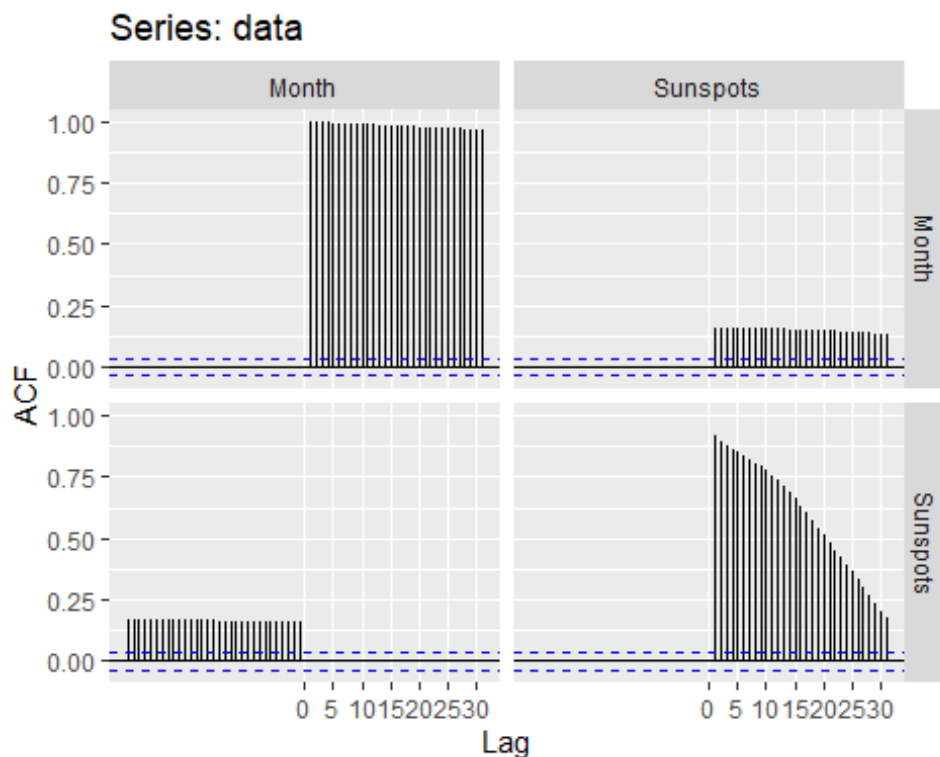
First set the hypothesis test:

The null hypothesis  $H_0$ : that the time series is non stationary

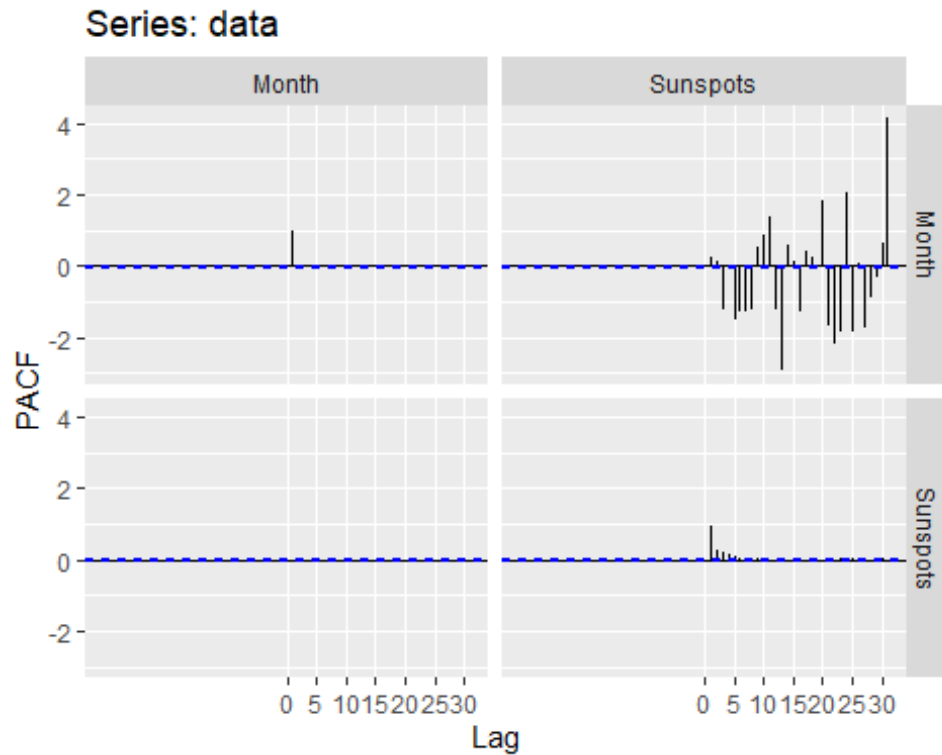
The alternative hypothesis  $H_A$ : that the time series is stationary

Inference: Here, the p-value is 0.01 which is less than 0.05, so we reject the null hypothesis, and go with the alternative hypothesis that the time series is stationary.

```
autoplot(acf(data, plot=FALSE))
```



```
autoplot(pacf(data, plot=FALSE))
```



```
#Model using ARIMA
auto.arima(data$Sunspots)

## Series: data$Sunspots
## ARIMA(2,1,2)
##
## Coefficients:
##          ar1          ar2          ma1          ma2
##          1.3467   -0.3963   -1.7710    0.8103
## s.e.    0.0303    0.0287    0.0205    0.0194
##
## sigma^2 = 243.8: log likelihood = -11745.5
## AIC=23500.99   AICc=23501.01   BIC=23530.71
```

Inference: The ARIMA(2,1,2) model parameters are lag 1 differencing (d), an autoregressive term of second lag (p) and a moving average model of order 2 (q).

## Conclusion:

The sunspot numbers increase and decrease over time with each year. The monthly sunspot data shows the pattern of seasonality with large differences between seasons.