

R Textbook Companion for  
Introductory Business Statistics  
by Alexander Holmes, Barbara Illowsky, Susan  
Dean<sup>1</sup>

Created by  
Radha R  
B.Sc.

Computer Science and Engineering

Shrimathi Devkunvar Nanalal Bhatt Vaishnav College for Women, Chennai

Cross-Checked by  
R TBC Team

April 28, 2022

<sup>1</sup>Funded by a grant from the National Mission on Education through ICT - <http://spoken-tutorial.org/NMEICT-Intro>. This Textbook Companion and R codes written in it can be downloaded from the "Textbook Companion Project" section at the website - <https://r.fossee.in>.

# Book Description

**Title:** Introductory Business Statistics

**Author:** Alexander Holmes, Barbara Illowsky, Susan Dean

**Publisher:** OpenStax

**Edition:** 2

**Year:** 2018

**ISBN:** 1-947172-47-6

R numbering policy used in this document and the relation to the above book.

**Exa** Example (Solved example)

**Eqn** Equation (Particular equation of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means an R code whose theory is explained in Section 2.3 of the book.

# Contents

<b>List of R Codes</b>	<b>4</b>
<b>1 Sampling and Data</b>	<b>5</b>
<b>2 Descriptive Statistics</b>	<b>10</b>
<b>3 Probability Topics</b>	<b>34</b>
<b>4 Discrete Random Variables</b>	<b>62</b>
<b>5 Continuous Random Variables</b>	<b>69</b>
<b>6 The Normal Distribution</b>	<b>77</b>
<b>7 The Central Limit Theorem</b>	<b>85</b>
<b>8 Confidence Intervals</b>	<b>87</b>
<b>9 Hypothesis Testing with One Sample</b>	<b>95</b>
<b>10 Hypothesis Testing with Two Samples</b>	<b>107</b>
<b>11 The Chi Square Distribution</b>	<b>122</b>
<b>12 F Distribution and one way ANOVA</b>	<b>134</b>
<b>13 Linear Regression and Correlation</b>	<b>142</b>

# List of R Codes

Exa 1.14	Finding percentage of heights . . . . .	5
Exa 1.15	Finding percentage of heights within a range . . . . .	6
Exa 1.16	Finding percentage of heights within a range . . . . .	6
Exa 1.17	Frequency table generation . . . . .	7
Exa 1.18	Frequency table . . . . .	8
Exa 2.1	Stem and leaf graph example1 . . . . .	10
Exa 2.2	Stem and leaf graph example2 . . . . .	10
Exa 2.3	Stem and Leaf plot . . . . .	11
Exa 2.4	Frequency curve example1 . . . . .	11
Exa 2.5	Bar graph example1 . . . . .	12
Exa 2.6	bar graph example2 . . . . .	12
Exa 2.7	Two way table . . . . .	13
Exa 2.8	Histogram graph example1 . . . . .	13
Exa 2.9	Histogram graph example2 . . . . .	14
Exa 2.10	Histogram graph example3 . . . . .	15
Exa 2.11	Frequency curve example2 . . . . .	16
Exa 2.12	Frequency curve example3 . . . . .	16
Exa 2.13	Time series graph . . . . .	17
Exa 2.14	Measures of Location of Data Example1 . . . . .	19
Exa 2.15	Measures of Location of Data example2 . . . . .	20
Exa 2.16	Measures of Location of Data example3 . . . . .	22
Exa 2.17	Measures of Location of Data example4 . . . . .	23
Exa 2.18	Measures of Location of Data example5 . . . . .	24
Exa 2.19	Measures of Location of Data example6 . . . . .	25
Exa 2.23	survey for buying gym . . . . .	26
Exa 2.24	Measure of Centre . . . . .	28
Exa 2.25	Measures of the Center of the Data example2 . . . . .	28
Exa 2.26	Measures of the Center of the Data example3 . . . . .	28

Exa 2.28	Calculating the Arithmetic Mean of Grouped Frequency Tables example1 . . . . .	29
Exa 2.29	Measures of the Spread of the Data Example1 . . . . .	30
Exa 2.30	Measures of the Spread of the Data example2 . . . . .	30
Exa 2.31	Standard deviation of grouped frequency tables . . . . .	32
Exa 2.32	Comparing values from different data sets . . . . .	33
Exa 3.1	Finding probabilities example1 . . . . .	34
Exa 3.2	Finding probabilities example2 . . . . .	35
Exa 3.3	Finding probabilities example3 . . . . .	36
Exa 3.6	Mutually Exclusive Events of coins . . . . .	37
Exa 3.7	Fliping of two coins and finding the probability . . . . .	38
Exa 3.8	Rolling of six sided dice . . . . .	39
Exa 3.9	Mutually Exclusive Events example1 . . . . .	40
Exa 3.10	Mutually Exclusive Events example2 . . . . .	41
Exa 3.11	Drawing of red and blue cards from a box . . . . .	42
Exa 3.12	Mutually Exclusive Events example3 . . . . .	43
Exa 3.13	Tossing of fair coin . . . . .	44
Exa 3.14	Two basic rules of Probability example1 . . . . .	45
Exa 3.15	Two basic rules of Probability example2 . . . . .	46
Exa 3.16	Two basic rules of Probability example3 . . . . .	46
Exa 3.17	Finding probabilities example4 . . . . .	47
Exa 3.18	Finding probabilities example5 . . . . .	48
Exa 3.19	Finding probabilities example6 . . . . .	49
Exa 3.20	Contingency tables example1 . . . . .	49
Exa 3.21	Contingency tables example2 . . . . .	50
Exa 3.22	Contingency tables example4 . . . . .	51
Exa 3.23	Contingency tables example3 . . . . .	52
Exa 3.24	drawing of three colored balls from urn . . . . .	53
Exa 3.25	drawing of marbles without replacement . . . . .	54
Exa 3.26	adoptiong of Tabby kittens and black kittens . . . . .	55
Exa 3.28	drawing venn diagram for flipping of two fair coins . . . . .	56
Exa 3.30	Venn diagram for selection of dogs . . . . .	57
Exa 3.31	venn diagram for selection of dogs2 . . . . .	58
Exa 3.32	probability of selecting student as fresher or earning B grade . . . . .	59
Exa 3.33	Two basic rules of Probability example4 . . . . .	60
Exa 4.1	hypergeometric Distribution . . . . .	62
Exa 4.8	Geometric probability distribution function example1 .	63

Exa 4.9	Geometric probability distribution function example2 . . . . .	63
Exa 4.10	Geometric probability distribution function example3 . . . . .	64
Exa 4.11	Geometric probability distribution function example4 . . . . .	64
Exa 4.14	Poisson Probability distribution example1 . . . . .	65
Exa 4.15	Poisson Probability distribution example2 . . . . .	65
Exa 4.16	Poisson Probability distribution example3 . . . . .	66
Exa 4.17	Poisson Probability distribution example4 . . . . .	67
Exa 4.18	Poisson Probability distribution example5 . . . . .	68
Exa 5.1	Continuous Probability Density functions example1 . . . . .	69
Exa 5.2	Uniform Distribution example1 . . . . .	70
Exa 5.3	The Exponential Distribution example1 . . . . .	70
Exa 5.4	The Exponential Distribution example2 . . . . .	71
Exa 5.5	The Exponential Distribution example3 . . . . .	72
Exa 5.6	The Exponential Distribution example4 . . . . .	73
Exa 5.7	The Exponential Distribution example5 . . . . .	74
Exa 5.8	Exponential probability . . . . .	75
Exa 6.1	The Standard Normal Distribution example1 . . . . .	77
Exa 6.2	Finding z scores for given mean and standard deviation	78
Exa 6.3	Using the Normal Distribution example1 . . . . .	79
Exa 6.4	Using the Normal Distribution example2 . . . . .	80
Exa 6.5	Using the Normal Distribution example3 . . . . .	81
Exa 6.6	Using the Normal Distribution example4 . . . . .	82
Exa 6.7	Finding binomial and normal distribution . . . . .	83
Exa 7.1	Finite Population Correction Factor example1 . . . . .	85
Exa 7.2	Finite Population Correction Factor example2 . . . . .	85
Exa 8.1	Calculating the Confidence Intervals example1 . . . . .	87
Exa 8.2	Calculating the Confidence Intervals example2 . . . . .	87
Exa 8.3	Calculating the Confidence Intervals example3 . . . . .	89
Exa 8.4	Calculating the Confidence Intervals example4 . . . . .	90
Exa 8.5	Confidence interval for a small sample example1 . . . . .	91
Exa 8.6	Confidence interval for a population proportion example1	92
Exa 8.7	Confidence interval for a population proportion example2	93
Exa 8.8	Confidence interval for a population proportion example3	93
Exa 8.9	Calculating the sample size n continuous and binary random variables . . . . .	94
Exa 9.8	Full Hypothesis test example1 . . . . .	95
Exa 9.9	Full Hypothesis test example2 . . . . .	96
Exa 9.10	Full Hypothesis test example3 . . . . .	98

Exa 9.11	Hypothesis test for proportions example1 . . . . .	99
Exa 9.12	Hypothesis test for proportions example2 . . . . .	101
Exa 9.13	Hypothesis test for proportions example3 . . . . .	103
Exa 9.14	Hypothesis test for proportions example4 . . . . .	104
Exa 10.1	Comparing two independent population means example1	107
Exa 10.2	Comparing two independent population means example2	109
Exa 10.3	Comparing two independent population means example3	110
Exa 10.4	Cohens standards for small medium and large effect sizes	111
Exa 10.5	Test for differences in means . . . . .	112
Exa 10.6	Comparing two independent population proportions ex- ample1 . . . . .	113
Exa 10.7	Two population means with known standard deviations example1 . . . . .	114
Exa 10.8	Two population means with known standard deviations example2 . . . . .	116
Exa 10.9	Matched or Paired Samples . . . . .	117
Exa 10.10	Matched or Paired Samples example2 . . . . .	118
Exa 10.11	Matched or Paired Samples example3 . . . . .	119
Exa 11.2	Test of single variance example1 . . . . .	122
Exa 11.3	Test of single variance example2 . . . . .	123
Exa 11.4	Goodness of Fit test example1 . . . . .	124
Exa 11.5	Goodness of Fit test example2 . . . . .	125
Exa 11.6	Goodness of Fit test example3 . . . . .	126
Exa 11.7	Goodness of Fit test example4 . . . . .	127
Exa 11.8	Goodness of Fit test example5 . . . . .	128
Exa 11.9	Test of Independence example1 . . . . .	129
Exa 11.10	Test of Independence example2 . . . . .	130
Exa 11.11	Test of Homogeneity . . . . .	132
Exa 12.1	Test of two variances . . . . .	134
Exa 12.2	The F distribution and the F Ratio example1 . . . . .	135
Exa 12.3	The F distribution and the F Ratio example2 . . . . .	136
Exa 12.4	The F distribution and the F Ratio example3 . . . . .	138
Exa 12.5	The F distribution and the F Ratio example4 . . . . .	140
Exa 13.2	Linear Equations example1 . . . . .	142
Exa 13.5	The Regression Equations example1 . . . . .	142
Exa 13.6	The Regression Equations example2 . . . . .	142

# Chapter 1

## Sampling and Data

R code Exa 1.14 Finding percentage of heights

```
1 #page 24
2 library(dplyr)
3 s_h<-data.frame(
4           lbound=c
5           (59.95,61.95,63.95,65.95,67.95,69.95,71.95,73.95)
6           ,
7           ubound=c
8           (61.95,63.95,65.95,67.95,69.95,71.95,73.95,75.95)
9           ,
10          freq=c(5,3,15,40,17,12,7,1))
11 View(s_h)
12 total=sum(s_h$freq)
13 print(total)
14 s_h$r_freq=s_h$freq/total
15 View(s_h)
16 s_h$cum_freq=cumsum(s_h$r_freq)
17 percent=s_h %>%
18   select(lbound,ubound,freq)%>%
19   filter(ubound<=65.95)
20 p_6595=(sum(percent$freq)/total)*100
21 print(paste("the solution is =",p_6595,"%"))
```

---

**R code Exa 1.15** Finding percentage of heights within a range

```
1 #page 25
2 library(dplyr)
3 s_h<-data.frame(
4   lbound=c
5   (59.95,61.95,63.95,65.95,67.95,69.95,71.95,73.95)
6   ,
7   ubound=c
8   (61.95,63.95,65.95,67.95,69.95,71.95,73.95,75.95)
9   ,
10  freq=c(5,3,15,40,17,12,7,1))
11 View(s_h)
12 total=sum(s_h$freq)
13 print(total)
14 s_h$r_freq=s_h$freq/total
15 View(s_h)
16 s_h$cum_freq=cumsum(s_h$r_freq)
17 percent=s_h %>%
18   select(lbound,ubound,freq,r_freq)%>%
19   filter(lbound>=61.95 & ubound<=65.95)
20 p_6165=sum(percent$r_freq)
21 print(paste("the solution is =",p_6165))
```

---

**R code Exa 1.16** Finding percentage of heights within a range

```
1 #page 25–26
2 library(dplyr)
3 s_h<-data.frame(
4   lbound=c
5   (59.95,61.95,63.95,65.95,67.95,69.95,71.95,73.95)
6   ,
```

```

5           ubound=c
              (61.95,63.95,65.95,67.95,69.95,71.95,73.95,75.95)
              ,
6           freq=c(5,3,15,40,17,12,7,1))
7 View(s_h)
8 total=sum(s_h$freq)
9 print(total)
10 s_h$r_freq=s_h$freq/total
11 View(s_h)
12 s_h$cum_freq=cumsum(s_h$r_freq)
13 percent=s_h %>%
14   dplyr::select(lbound,ubound,freq,r_freq)%>%
15   filter(lbound>=67.95 & ubound<=71.95)
16 p_6771=(sum(percent$r_freq))*100
17 print(paste("solution of a is =",p_6771,"%"))
18 percent=s_h %>%
19   dplyr::select(lbound,ubound,freq,r_freq)%>%
20   filter(lbound>=67.95 & ubound<=73.95)
21 p_6773=(sum(percent$r_freq))*100
22 print(paste("solution of b is =",p_6773,"%"))
23 percent=s_h %>%
24   dplyr::select(lbound,ubound,freq,r_freq)%>%
25   filter(lbound>=65.95)
26 p_65=(sum(percent$r_freq))*100
27 print(paste("solution of c is =",p_65,"%"))
28 percent=s_h %>%
29   dplyr::select(lbound,ubound,freq,r_freq)%>%
30   filter(lbound>=61.95 & ubound<=71.95)
31 n_p=sum(percent$freq)
32 print(paste("solution of d is =",n_p))

```

---

### R code Exa 1.17 Frequency table generation

```

1 #page 26-27
2 library(dplyr)

```

```

3 library(MASS)
4 miles<-data.frame(data=c
  (2,3,4,5,7,10,12,13,15,18,20),
  freq=c(2,1,1,3,2,3,2,1,1,2,1))
5 View(miles)
6 total=sum(miles$freq)
7 print(total)
8 miles$r_freq=miles$freq/total
9 View(miles)
10 miles$cum_freq=cumsum(miles$r_freq)
11 filterdata<-filter(miles,data>=5 & data<=7)
12 ans1=sum(filterdata$freq)/total
13 print(paste("the answer c=",fractions(ans1)))
14 filterdata<-filter(miles,data>=12)
15 ans2=sum(filterdata$freq)/total
16 print(paste("the answer d is=",fractions(ans2)))
17 filterdata<-filter(miles,data<12)
18 ans3=sum(filterdata$freq)/total
19 print(paste("the answer d=",fractions(ans3)))
20 filterdata<-filter(miles,data>5 & data<13)
21 ans4=sum(filterdata$freq)/total
22 print(paste("the answer d=",fractions(ans4)))

```

---

### R code Exa 1.18 Frequency table

```

1 #page 28
2 library(dplyr)
3 earthquake<-data.frame(year=c
  (2000,2001,2002,2003,2004,2005,2006,2007,2008,2009,2010,2011,2012,
   ,
 4           deaths=c
  (231,21357,11685,33819,228802,88003,6605,712,88
  )
5 View(earthquake)
6 total=sum(earthquake$deaths)

```

```

7 earthquake$r_freq=earthquake$deaths/total
8 View(earthquake)
9 earthquake$cum_freq=cumsum(earthquake$r_freq)
10 q_a=earthquake %>%
11   dplyr::select(year,r_freq) %>%
12   filter(year>=2006 & year<=2009)
13 View(q_a)
14 freq6_9=sum(q_a$r_freq)
15 p_6_9=freq6_9*100
16 cat("the answer (a) is = ",round(p_6_9,1),"%" )
17 q_b=earthquake %>%
18   dplyr::select(year,r_freq) %>%
19   filter(year>2009)
20 View(q_b)
21 freq_9=sum(q_b$r_freq)
22 p_9=freq_9*100
23 cat("the answer % (b) is= ",round(p_9,1),"%" )
24 q_c=earthquake %>%
25   dplyr::select(year,r_freq) %>%
26   filter(year<=2003)
27 View(q_c)
28 freq_3=sum(q_c$r_freq)
29 p_3=freq_3*100
30 cat("the answer (c) is=",round(p_3,1),"%" )
31 q_d=earthquake %>%
32   dplyr::select(year,r_freq) %>%
33   filter(year==2004)
34 View(q_d)
35 freq_4=sum(q_d$r_freq)
36 p_4=freq_4*100
37 cat("the % (d) is= ",round(p_4,1),"%" )

```

---

# Chapter 2

## Descriptive Statistics

**R code Exa 2.1** Stem and leaf graph example1

```
1 # Page NO : 46
2 df<-data.frame(scores=c
3   (33,42,49,49,53,55,55,61,63,67,68,68,69,69,72,
4     73,74,78,80,83,88,88,88,
5     90,92,94,94,94,94,94,96,100))
6 View(df)
7 stem(df$scores)
```

---

**R code Exa 2.2** Stem and leaf graph example2

```
1 # Page NO : 47
2 df<-data.frame(dist=c
3   (1.1,1.5,2.3,2.5,2.7,3.2,3.3,3.3,3.5,3.8,4.0,4.2,4.5,4.5,4.5,4.7,4.8,
4   6.5,6.7,12.3))
5 View(df)
6 stem(df$dist, scale=3)
```

---

### R code Exa 2.3 Stem and Leaf plot

```
1 # Page NO : 47–49
2 library("aplypack")
3 df<-data.frame(a_I=c
57,61,57,57,58,57,61,54,68,51,49,64,50,48,65,
52,56,46,54,49,51,47,55,55,54,42,51,56,55,51,
54,51,60,62,43,55,56,61,52,69,64,47,54,47)
)
6 df1<-data.frame(a_D=c
67,90,83,85,73,80,78,79,68,71,53,65,74,64,77,
56,66,63,70,49,56,71,67,71,58,60,72,67,57,60,
90,63,88,78,46,64,81,93,93))
7 View(df)
8 View(df1)
9 stem.leaf.backback(df$a_I,df1$a_D,m=1)
10 #The answer provided in the textbook is wrong.
```

---

### R code Exa 2.4 Frequency curve example1

```
1 #page 49–50
2 library(dplyr)
3 remainder<-data.frame(no_times=c(0,1,2,3,4,5),
4 frequency=c(2,5,8,14,7,4))
5 View(remainder)
6 plot(remainder$no_times,remainder$frequency,xlab="no
of times",
7 ylab="frequency ",type=
"o",col="blue")
```

---

### R code Exa 2.5 Bar graph example1

```
1 #page 51
2 library(dplyr)
3 library(ggplot2)
4 dtabl<-data.frame(
5     agegroups=c("13-25","26-44","45-64"),
6     no_of_users=c(66082280, 53300200, 27885100)
7     ,
8     proportion=c(45,36, 19))
9 View(dtabl)
10 ggplot(dtabl,aes(x=agegroups,y=proportion,color=cut) +
11     geom_bar(color="blue",stat="identity",width=0.5) +
11     labs(x="agegroups",y="%")
```

---

### R code Exa 2.6 bar graph example2

```
1 #page 52-53
2 library(dplyr)
3 library(ggplot2)
4 dtabl<-data.frame(
5     race=c("1","2","3","4","5","6"),
6     examinee=c(10.3,9.0,17.0,0.6,57.1,6.0),
7     overall=c(5.7,14.7, 17.6,1.1,59.2,1.7))
8 View(dtabl)
9 ggplot(dtabl,aes(x=race,y=examinee),fill=race) +
10     geom_bar(color="blue",stat="identity",width=0.5) +
11     theme(legend.position="bottom") +
12     theme(legend.direction="vertical") +
13     theme(axis.text.x=element_text(angle=0)) +
14     geom_text(aes(label=examinee))
```

---

### R code Exa 2.7 Two way table

```
1 #page 54
2 library(dplyr)
3 pets<-data.frame(dogs=c(4,4,8),
4                     cats=c(2,6,8),
5                     fish=c(2,2,4),
6                     total=c(8,12,20))
7 rownames(pets)<-c("men","women","total")
8 last=ncol(pets)
9 total=0
10 for(c in 1:(last-1)){
11   x=(pets[1,c]/pets[1,last])
12   print(paste("number owning ", colnames(pets)[c],x))
13   total=total+x
14 }
15 print(paste("sum = ", total))
```

---

### R code Exa 2.8 Histogram graph example1

```
1 #page 55-56
2 library(ggplot2)
3 dtabl<-data.frame(height=c
4                     (59.95,60,60.5,61,61,61.5,63.5,63.5,63.5,64,64,64,64,64,64,
5
6                     64.5,64.5,64.5,64.5,64.5,64.5,64.5,64.5,64.5,64.5,
7
8                     66,66,66,66,66,66,66,66,66,66,
```

66.5,66.5,66.5,66.5,66.5,66.5,66.5,66.5,66.5,66.5,

67,67,67,67,67,67,67,67,67,67,

67.5,67.5,67.5,67.5,67.5,67.5,67.5,

```

9      68,68,
10     69,69,69,69,69,69,69,69,69,69,69,
11     69.5,69.5,69.5,69.5,69.5,69.5,
12     70,70,70,70,70,70,
13     70.5,70.5,70.5,
14     71,71,71,
15     72,72,72,
16     72.5,72.5,
17     73,
18     73.5,
19     74,75.95))
20 View(dtbl)
21 breaks=seq(59.95,75.95,by=2)
22 dcut=cut(dtbl$height,breaks,right=FALSE)
23 dout=as.data.frame(table(dcut))
24 dout<-transform(dout,cumFreq=cumsum(Freq),relative=
25   round(prop.table(Freq),2))
26 ggplot(dout,aes(dcut,relative))+geom_col(fill="purple")+
27   geom_text(aes(label=relative))+xlab("height")+ylab("r.freq")
28 #The answer may slightly vary due to rounding off values.

```

---

### R code Exa 2.9 Histogram graph example2

```

1 #page 56–57
2 library(ggplot2)
3 dtabl<-data.frame(height=c(1,1,1,1,1,1,1,1,1,1,1,
4                           2,2,2,2,2,2,2,2,2,2,2,
5                           3,3,3,3,3,3,3,3,3,3,3,3,3,3,3,3,3,3,3,3,
6                           4,4,4,4,4,4,
7                           5,5,5,5,5,
8                           6,6))

```

```

9 View(dtbl)
10 breaks=seq(0.5,6.5,by=1)
11 dcut=cut(dtbl$height,breaks,right=FALSE)
12 dout=as.data.frame(table(dcut))
13 dout<-transform(dout,cumFreq=cumsum(Freq),relative=
    round(prop.table(Freq),2))
14 nobars=(6.5-0.5)/1
15 print(paste("the number of bars =",nobars))
16 ggplot(dout,aes(dcut,Freq))+
    geom_col(fill="purple")+
    geom_text(aes(label=Freq))+
    xlab("no. of books")+ylab("freq")

```

---

### R code Exa 2.10 Histogram graph example3

```

1 #page 57–58
2 library(dplyr)
3 library(ggplot2)
4 dtbl<-data.frame(hours=c(9.95,10,2.25,16.75,0,
5                     19.5,22.5,7.5,15,12.75,
6                     5.5,11,10,20.75,17.5,
7                     23,21.9,24,23.75,18,
8                     20,15,22.9,18.8,20.5))
9 bins=seq(-0.01,25,by=5)
10 scores=cut(dtbl$hours,bins)
11 table(scores)
12 View(dtbl)
13 View(scores)
14 freq_table=transform(table(scores))
15 xx=transform(freq_table,Rel_freq=prop.table(Freq),
   cumfreq=cumsum(Freq))
16 View(xx)
17 ggplot(data=xx,
18         aes(x=scores,y=Freq))+ 
19         geom_col(color="red",fill="blue")+

```

```
20     labs(y="no. of students",x="hours spent")+
21     scale_y_continuous(breaks=seq(0,10,1))
```

---

### R code Exa 2.11 Frequency curve example2

```
1 #page no 59
2 library(ggplot2)
3 df<-data.frame(lbound=c
4                   (39.5,49.5,59.5,69.5,79.5,89.5,99.5),
5                   ubound=c
6                   (49.5,59.5,69.5,79.5,89.5,99.5,109.5),
7                   ,
8                   freq=c(0,5,10,30,40,15,0),
9                   cfreq=c(0,5,15,45,85,100,0))
10 View(df)
11 df$mid=(df$lbound+df$ubound)/2
12
13 ggplot(df,aes(x=mid,y=freq))+geom_line(aes(x=mid,y=freq),size=1)+geom_point(aes(mid,size=0.5),shape=18,show.legend=
14   FALSE)+scale_x_continuous(breaks=seq(from=44.5,to=104.5,
15   by=10))+xlab("result")+ylab("number of students")
```

---

### R code Exa 2.12 Frequency curve example3

```
1 #page no: 60–61
2 library(ggplot2)
3 df<-data.frame(lbound=c
4                   (39.5,49.5,59.5,69.5,79.5,89.5,99.5),
```

```

4         ubound=c
5             (49.5,59.5,69.5,79.5,89.5,99.5,109.5)
6             ,
7             freq=c(0,5,10,30,40,15,0),
8             cfreq=c(0,5,15,45,85,100,0))
9 View(df)
10 df$mid=(df$lbound+df$ubound)/2
11 df2=data.frame(lbound=c
12     (39.5,49.5,59.5,69.5,79.5,89.5,99.5),
13     ubound=c
14         (49.5,59.5,69.5,79.5,89.5,99.5,109.5)
15         ,
16         freq=c(0,10,10,30,45,5,0),
17         cfreq=c(0,10,20,50,95,100,0))
18 df2$mid=(df2$lbound+df2$ubound)/2
19 View(df2)
20 ggplot(df,aes(x=mid,y=freq))+geom_line(aes(x=mid,y=freq),color="pink",size=1,
21   show.legend=FALSE)+geom_point(aes(mid,size=0.5),shape=18,show.legend=
22   FALSE)+geom_line(data=df2,aes(x=mid,y=freq),color="blue",
23   size=1,show.legend=FALSE)+geom_point(aes(mid,size=0.5),shape=18,show.legend=
24   FALSE)+scale_x_continuous(breaks=seq(44.5,104.5,10))+scale_y_continuous(breaks=seq(0,50,5))+xlab("result")+ylab("number of students")

```

---

### R code Exa 2.13 Time series graph

```

1 #page 62–63
2 library(ggplot2)
3 consumer<-data.frame(year=c
4   (2003,2004,2005,2006,2007,2008,2009,2010,2011,2012)

```

```

4      ,
5      jan=c
6          (181.7,185.2,190.7,198.3,202.416,211.080,211.143,216.687
7          ,
8      feb=c
9          (183.1,186.2,191.8,198.7,203.499,211.693,212.193,216.741
10         ,
11     mar=c
12         (184.2,187.4,193.3,199.8,205.352,213.528,212.709,217.631
13         ,
14     apr=c
15         (183.8,188,194.6,201.5,206.686,214.823,213.24,218.009,22
16         ,
17     may=c
18         (183.5,189.1,194.4,202.5,207.949,216.632,213.856,218.178
19         ,
20     jun=c
21         (183.7,189.7,194.5,202.9,208.352,218.815,215.693,217.965
22         ,
23     jul=c
24         (183.9,189.4,195.4,203.5,208.299,219.964,215.351,218.011
25         ,
26     aug=c
27         (184.6,189.5,196.4,203.9,207.917,219.086,215.834,218.312
28         ,
29     sep=c
30         (185.2,189.9,198.8,202.9,208.49,218.783,215.969,218.439,
31         ,
32     oct=c
33         (185,190.9,199.2,201.8,208.936,216.573,216.177,218.711,2
34         ,
35     nov=c
36         (184.5,191,197.6,201.5,210.177,212.425,216.33,218.803,22
37         ,
38     dec=c
39         (184.3,190.3,196.8,201.8,210.036,210.228,215.949,219.179
40         ,
41     annual=c

```

```

(184,188.9,195.3,201.6,207.342,215.303,214.537,218.056,2
)
17 View(consumer)
18 min<-as.Date("2003-1-1")
19 max<-as.Date("2012-12-30")
20 yrs<-as.Date(ISOdate(consumer$year,1,1))
21 ggplot(data=consumer,aes(x=yrs,y=annual))+ 
22   geom_line(size=1)+ 
23   scale_x_date(limits=c(min,max))+ 
24   xlab("year")+ylab("annual price")

```

---

### R code Exa 2.14 Measures of Location of Data Example1

```

1 #page no : 65–66
2 library(base)
3 library(dplyr)
4 price<-data.frame(
5   dollars=c
      (389950,230500,158000,479000,639000,114950,5500000,387000
6
      575000,488800,1095000))
7 View(price)
8 M=median(price$dollars)
9 print(paste("median = ",M))
10 price1=price %>%
11   select(dollars) %>%
12   arrange(dollars)
13 View(price1)
14 rowcount=nrow(price1)
15 midindex=(rowcount+1)/2
16 if(floor(midindex)!=midindex)
17 {
18   l<-(midindex-1)/2
19   u<-(midindex+1)/2
20 } else

```

```

21 {
22   l<- (midindex-1)
23   u<- (midindex+1)
24 }
25 q1=median(price1$dollars[1:l])
26 print(paste("Q1 = ",q1))
27 q3=median(price1$dollars[u:rowcount])
28 print(paste("Q3 = ",q3))
29 IQR1=q3-q1
30 print(paste("IQR = ",IQR1))
31 o_IQR1=(1.5)*IQR1
32 loutlier=q1-o_IQR1
33 print(paste("lower outlier =",loutlier))
34 uoutlier=q3+o_IQR1
35 print(paste("upper outlier =",uoutlier))
36 if(min(price1$dollars)>loutlier)
37 {
38   print("No outliers in the lower end of price")
39 } else
40 {
41   print("Outliers in the lower end of price")
42   print(paste("the outlier value is =",min(price1$ 
43 dollars)))
44 }
45 if(max(price1$dollars)<uoutlier)
46 {
47   print("No outliers in the upper end of price")
48 } else
49 {
50   print("Outliers in the upper end of price")
51   print(paste("the outlier value is =",max(price1$ 
      dollars)))
52 }
```

---

**R code Exa 2.15** Measures of Location of Data example2

```

1 #page no : 66
2 library(dplyr)
3 t_s<-data.frame(
4     minimum=c(32,25.5),
5     q1=c(56,78),
6     median=c(74.5,81),
7     q3=c(82.5,89),
8     maximum=c(99,98)
9 )
10 rownames(t_s)<-c("day","night")
11 View(t_s)
12 t_s$IQR=t_s$q3-t_s$q1
13 t_s$outlierq1=t_s$q1-(t_s$IQR)*1.5
14 t_s$outlierq3=t_s$q3+(t_s$IQR)*1.5
15 result1=t_s %>% select(q1,q3,minimum,maximum,
16     outlierq1,outlierq3) %>%
17         filter(row.names(t_s)=="day")
18 if(result1$minimum>result1$outlierq1)
19 {
20 } else
21 {
22     print("No outliers in the lower end of day")
23 } else
24 {
25     print("Outliers in the lower end of day")
26     print(paste("any value < than", result1$outlierq1,
27         " is outlier"))
28     print(paste("the value=", result1$minimum, "is
29         outlier"))
30 }
31 if(result1$maximum<result1$outlierq3)
32 {
33     print("No outliers in the upper end of day")
34 } else
35 {
36     print("Outliers in the upper end of day")
37     print(paste("any value > than", result1$outlierq3,
38         " is outlier"))
39     print(paste("the value=", result1$maximum, "is
40         outlier"))

```

```

34 }
35 result2=t_s %>% select(q1,q3,minimum,maximum,
  outlierq1,outlierq3) %>%
36   filter(row.names(t_s)=="night")
37 if(result2$minimum>result2$outlierq1)
38 {
39   print("No outliers in the lower end of night")
40 } else
41 {
42   print("Outliers in the lower end of night")
43   print(paste("any value < than", result2$outlierq1,
44     " is outlier"))
45   print(paste("the value=",result2$minimum," is
46     outlier"))
47 }
48 if(result2$maximum<result2$outlierq3)
49 {
50   print("No outliers in the upper end of night")
51 } else
52 {
53   print("Outliers in the upper end of night")
54   print(paste("any value > than", result2$outlierq3,
55     " is outlier"))
56   print(paste("the value=",result2$maximum," is
57     outlier"))
58 }

```

## R code Exa 2.16 Measures of Location of Data example3

```
5 dtabl1<-data.frame(  
6             hours=c(4,5,6,7,8,9,10),  
7             freq=c(2,5,7,12,14,7,3))  
8 total=sum(dtabl1$freq)  
9 dtabl1$rfreq=dtabl1$freq/total  
10 dtabl1$cum_freq=cumsum(dtabl1$rfreq)  
11 View(dtabl1)  
12 print(paste("28% is",quantile(dtbl,0.28)))  
13 print(paste("median is",quantile(dtbl,0.50)))  
14 print(paste("75% is",quantile(dtbl,0.75)))  
15 #The answer may slightly vary due to rounding off  
   values.
```

## R code Exa 2.17 Measures of Location of Data example4

```

19     return(x)
20 }
21 test1=find_percentile(80,dtabl_len)
22 per_80=(dtabl[test1[1]]+dtabl[test1[2]])/2
23 test2=find_percentile(90,dtabl_len)
24 per_90=(dtabl[test2[1]]+dtabl[test2[2]])/2
25 test3=find_percentile(25,dtabl_len)
26 per_25=(dtabl[test3[1]]+dtabl[test3[2]])/2
27 print(paste("80th percentile is",per_80))
28 print(paste("90th percentile is",per_90))
29 print(paste("first quartile is",per_25))

```

---

### R code Exa 2.18 Measures of Location of Data example5

```

1 #page no : 68–69
2 library(base)
3 dtabl=c
4             (18,21,22,25,26,27,29,30,31,33,36,37,41,42,47,52,55,57,58,62,64,67,
5               71,72,73,74,76,77)
6 dtabl_len=length(dtabl)
7 find_percentile<-function(val,dtabl_len)
8 {
9     i=(val/100)*(dtabl_len+1)
10    lvalue=floor(i)
11    uvalue=ceiling(i)
12    x=c(lvalue,uvalue)
13    return(x)
14 }
15 test1=find_percentile(70,dtabl_len)
16 per_70=(dtabl[test1[1]]+dtabl[test1[2]])/2
17 test2=find_percentile(83,dtabl_len)
18 per_83=(dtabl[test2[1]]+dtabl[test2[2]])/2
19 print(paste("70th percentile is",per_70))
20 print(paste("83rd percentile is",per_83))

```

---

### R code Exa 2.19 Measures of Location of Data example6

```
1 #page no : 69
2 library(base)
3 dtabl=c
4 (18,21,22,25,26,27,29,30,31,33,36,37,41,42,47,52,55,57,58,62,64,67
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
```

```
71,72,73,74,76,77)
dtabl_len=length(dtabl)
find_range<-function(val)
{
  count=0
  for(i in 1:dtabl_len)
  {
    if(dtabl[i]<val)
    {
      count=count+1
    }
    else
    {
      break
    }
  }
  return(count)
}
find_percentile<-function(val)
{
  x=find_range(val)
  y=1
  i=((x+0.5*y)/(dtabl_len))*100
  return(round(i))
}
per_58=find_percentile(58)
per_25=find_percentile(25)
```

```
31 print(paste("58 is",per_58,"th percentile"))
32 print(paste("25 is",per_25,"th percentile"))
```

---

### R code Exa 2.23 survey for buying gym

```
1 #page no : 71
2 library(dplyr)
3 minutes<-data.frame(
4   x=c
5   (0,40,60,30,60,10,45,30,300,90,30,120,60,0,20)
6 )
5 View(minutes)
6 M=median(minutes$x)
7 minutes1=minutes %>%
8   select(x) %>%
9   arrange(x)
10 View(minutes1)
11 rowcount=nrow(minutes1)
12 midindex=(rowcount+1)/2
13 if(floor(midindex)!=midindex)
14 {
15   l<-(midindex-1)/2
16   u<-(midindex+1)/2
17 } else
18 {
19   l<-(midindex-1)
20   u<-(midindex+1)
21 }
22 q1=median(minutes1$x[1:l])
23 print(paste("minimum=",min(minutes)))
24 print(paste(" (Q1) = ",q1," minutes"))
25 print(paste(" median = ",M))
26 q3=median(minutes1$x[u:rowcount])
27 print(paste(" (Q3) = ",q3, " minutes"))
28 IQR1=q3-q1
```

```

29 print(paste("maximum=", max(minutes)))
30 o_IQR1=(1.5)*IQR1
31 loutlier=q1-o_IQR1
32 uoutlier=q3+o_IQR1
33 minutes3<-data.frame(
34   x=c(0,40,60,30,60,10,45,30,90,30,120,60,0,20))
35 View(minutes3)
36 M=median(minutes3$x)
37 minutes4=minutes3 %>%
38   select(x) %>%
39   arrange(x)
40 View(minutes4)
41 rowcount=nrow(minutes4)
42 if(rowcount%%2==0)
43 {
44   midindex=rowcount/2
45 } else
46 {
47   midindex=(rowcount+1)/2
48 }
49 if(floor(midindex) != midindex)
50 {
51   l<-(midindex-1)/2
52   u<-(midindex+1)/2
53 } else
54 {
55   l<-(midindex-1)
56   u<-(midindex+1)
57 }
58 q1=median(minutes4$x[1:l])
59 print(paste("minimum=", min(minutes3)))
60 print(paste(" (Q1) = ", q1, " minutes"))
61 q3=median(minutes4$x[u:rowcount])
62 print(paste(" (Q3) = ", q3, " minutes"))
63 IQR1=q3-q1
64 print(paste("maximum=", max(minutes3)))
65 #The answer provided in the textbook is wrong.

```

---

**R code Exa 2.24** Measure of Centre

```
1 #page no : 72–73
2 library(dplyr)
3 aids<-c
   (3,4,8,8,10,11,12,13,14,15,15,16,16,17,17,18,21,22,22,24,24,25,26
4
   27,27,29,29,31,32,33,33,34,34,35,37,40,44,44,47)
5 aids_mean=mean(aids)
6 aids_median=median(aids)
7 print(paste("mean = ",round(aids_mean,1)))
8 print(paste("median = ",aids_median))
```

---

**R code Exa 2.25** Measures of the Center of the Data example2

```
1 #page no : 73
2 earning<-c()
3 for(i in 1:49)
4 {
5   earning[i]=30000
6 }
7 earning[50]=5000000
8 earning_mean=mean(earning)
9 earning_median=median(earning)
10 print(paste("the mean is ",earning_mean))
11 print(paste("the median is ",earning_median))
```

---

**R code Exa 2.26** Measures of the Center of the Data example3

```

1 #page no : 73
2 library(dplyr)
3 student<-c
    (50,53,59,59,63,63,72,72,72,72,7276,78,81,83,84,84,84,90,93)

4 mode<-function(x)
5 {
6   ux<-unique(x)
7   tab<-tabulate(match(x,ux))
8   return(ux[tab==max(tab)])
9 }
10 s_mode=mode(student)
11 print(paste("the MODE is ",s_mode))

```

---

**R code Exa 2.28** Calculating the Arithmetic Mean of Grouped Frequency Tables example1

```

1 #page no : 74–75
2 s_test<-data.frame(
3   grade_l=c
        (50,56.5,62.5,68.5,74.5,80.5,86.5,92.5)
        ,
4   grade_u=c
        (56.5,62.5,68.5,74.5,80.5,86.5,92.5,98.5)
        ,
5   s_no=c(1,0,4,4,2,3,4,1))
6 s_test$midpoint=(s_test$grade_u+s_test$grade_l)/2
7 s_test$fm=s_test$midpoint*s_test$s_no
8 sum_fm=sum(s_test$fm)
9 sum_s_no=sum(s_test$s_no)
10 mean_value=sum_fm/sum_s_no
11 print(paste("the sum of product is ",round(sum_fm,2)))
12 print(paste("the mean is ",round(mean_value,2)))

```

---

**R code Exa 2.29** Measures of the Spread of the Data Example1

```
1 #page no : 81–82
2 library(dplyr)
3 avg_ages<-data.frame(ages=c
4                         (9,9.5,9.5,10,10,10,10,10.5,10.5,10.5,10.5,
5                          11,11,11,11,11,11,11,11.5,11.5,11.5))
6 View(avg_ages)
7 ages1=avg_ages %>%
8     group_by(ages)%>%
9     mutate(frequency=n())%>%
10    select(ages,frequency)%>%
11    distinct()
12 View(ages1)
13 total=sum(ages1$frequency)
14 ages1$val1=ages1$ages*ages1$frequency
15 xbar=sum(ages1$val1)/total
16 View(ages1)
17 ages1$dev1=ages1$ages-xbar
18 ages1$devsq=ages1$dev1*ages1$dev1
19 ages1$fd=ages1$frequency*ages1$devsq
20 View(ages1)
21 sv=sum(ages1$fd)/(total-1)
22 sd=sqrt(sv)
23 print(paste("the sample mean is =",round(xbar,3)))
24 print(paste("the sample variance is =",round(sv,4)))
25 print(paste("the sample sd is =",round(sd,2)))
```

---

**R code Exa 2.30** Measures of the Spread of the Data example2

```
1 #page no : 83–84
```

```

2 library(dplyr)
3 calculus<-data.frame(marks=c
(33,42,49,49,53,55,55,61,63,67,68,68,69,69,72,73,74,78,
4 80,83,88,88,88,90,92,94,94,94,94,96,100)
)
5 View(calculus)
6 calc1=calculus %>%
7   group_by(marks)%>%
8   mutate(frequency=n())%>%
9   select(marks,frequency)%>%
10  distinct()
11 View(calc1)
12 total=sum(calc1$frequency)
13 calc1$r_freq=round((calc1$frequency/total),3)
14 calc1$c_freq=round((cumsum(calc1$r_freq)),3)
15 View(calc1)
16 calc1$val1=calc1$marks*calc1$frequency
17 xbar=sum(calc1$val1)/total
18 View(calc1)
19 calc1$dev1=calc1$marks-xbar
20 calc1$devsq=calc1$dev1*calc1$dev1
21 calc1$fd=calc1$frequency*calc1$devsq
22 View(calc1)
23 sv=sum(calc1$fd)/(total-1)
24 sd=sqrt(sv)
25 rowcount=nrow(calculus)
26 midindex=(rowcount+1)/2
27 if(floor(midindex) != midindex)
28 {
29   l<-(midindex-1)/2
30   u<-(midindex+1)/2
31 } else
32 {
33   l<-(midindex-1)
34   u<-(midindex+1)
35 }
36 q1=median(calculus$marks[1:l])

```

```

37 q3=median(calculus$marks[u:rowcount])
38 IQR1=q3-q1
39 mean1=mean(calculus$marks)
40 median1=median(calculus$marks)
41 print(paste("the sample mean is =",round(mean1,1)))
42 print(paste("the sample sd is =",round(sd,1)))
43 print(paste("the median is =",median1))
44 print(paste("the 1st quartile is =",q1))
45 print(paste("the 3rd quartile is =",q3))
46 print(paste("the IQR is =",IQR1))

```

---

**R code Exa 2.31** Standard deviation of grouped frequency tables

```

1 #page no : 84–85
2 dtabl<-data.frame(lvalue=c(0,3,6,9,12),
3                     uvalue=c(2,5,8,11,14),
4                     f=c(1,6,10,7,0))
5
6 dtabl$m=(dtabl$lvalue+dtabl$uvalue)/2
7 total=sum(dtabl$f)
8 dtabl$fm=dtabl$f*dtabl$m
9 xbar=sum(dtabl$fm)/total
10 View(dtabl)
11 dtabl$dev1=dtabl$m-xbar
12 dtabl$devsq=dtabl$dev1*dtabl$dev1
13 dtabl$fmxbar=dtabl$f*dtabl$devsq
14 View(dtabl)
15 sv=sum(dtabl$fmxbar)/(total-1)
16 sd=sqrt(sv)
17 print(paste("the variance is =",round(sv,2)))
18 print(paste("the sample sd is =",round(sd,2)))
19 #The answer provided in the textbook is wrong.

```

---

**R code Exa 2.32** Comparing values from different data sets

```
1 #page no : 85
2 dtabl<-data.frame(name=c("John","Ali"),
3                      GPA=c(2.85,77),
4                      meangpa=c(3.0,80),
5                      schoolsd=c(0.7,10))
6 dtabl$z1=(dtabl$GPA-dtabl$meangpa)/dtabl$schoolsd
7 View(dtabl)
8 no=nrow(dtabl)
9 for(i in 1:no)
10 {
11   print(paste("sd of = ",dtabl$name[i]," is ",round(
12     dtabl$z1[i],2)))
13   if(dtabl$z1[1]>dtabl$z1[2])
14   {
15     print(paste(dtabl$name[1]," has more GPA"))
16   } else
17   {
18     print(paste(dtabl$name[2]," has more GPA"))
19 }
```

---

# Chapter 3

## Probability Topics

R code Exa 3.1 Finding probabilities example1

```
1 #page no :135
2 library(MASS)
3 S=c(1:19)
4 A=c(2,4,6,8,10,12,14,16,18)
5 B=c(14,15,16,17,18,19)
6 cat("a. S= ",S)
7 cat("b. A= ",A)
8 cat("b. B= ",B)
9 P_A=length(A)/length(S)
10 print(paste(" c. P(A) =",fractions(P_A)))
11 P_B=length(B)/length(S)
12 print(paste("c. P(B) =",fractions(P_B)))
13 ABint=intersect(A,B)
14 ABunion=union(A,B)
15 cat("d. AintB =",ABint)
16 cat("d. AUB=",ABunion)
17 P_AintB=length(ABint)/length(S)
18 print(paste("e. P(AintB) =",fractions(P_AintB)))
19 P_AUB=length(ABunion)/length(S)
20 print(paste("e. P(AUB) =",fractions(P_AUB)))
21 Acomp=setdiff(S,A)
```

```

22 cat("f. A' =", Acomp)
23 P_Acomp=length(Acomp)/length(S)
24 print(paste("f. P(A') =", fractions(P_Acomp)))
25 print(paste("g. P(A)+P(A') =", P_A+P_Acomp))
26 P_A_B=P_AintB/P_B
27 P_B_A=P_AintB/P_A
28 print(paste("h. P(A|B) = ", fractions(P_A_B)))
29 print(paste("h. P(B|A) = ", fractions(P_B_A)))
30 if(P_A_B==P_B_A){
31   print("h. P(A|B) is equal to P(B|A)")
32 }else {
33   print("h. P(A|B) not equal to P(B|A)")
34 }

```

---

### R code Exa 3.2 Finding probabilities example2

```

1 #page no :136–137
2 library(MASS)
3 S=c(1:6)
4 T=c(2)
5 A=c(2,4,6)
6 B=c(1,2,3)
7 P_T=length(T)/length(S)
8 cat("a. T =", T)
9 print(paste("a. P(T) =", fractions(P_T)))
10 P_A=length(A)/length(S)
11 cat("b. A =", A)
12 print(paste("b. P(A) =", fractions(P_A)))
13 P_B=length(B)/length(S)
14 cat("c. B =", B)
15 print(paste("c. P(B) =", fractions(P_B)))
16 Acomp=setdiff(S,A)
17 cat("d. A' =", Acomp)
18 P_Acomp=length(Acomp)/length(S)
19 print(paste("d. P(A') =", fractions(P_Acomp)))

```

```

20 ABint=intersect(A,B)
21 ABunion=union(A,B)
22 P_AintB=length(ABint)/length(S)
23 P_A_B=P_AintB/P_B
24 P_B_A=P_AintB/P_A
25 print(paste("e. P(A|B) =", fractions(P_A_B)))
26 print(paste("f. P(B|A) =", fractions(P_B_A)))
27 cat("g. AintB =", ABint)
28 print(paste("g. P(AintB) =", fractions(P_AintB)))
29 P_AUB=length(ABunion)/length(S)
30 cat("h. AUB =", ABunion)
31 print(paste("h. P(AUB) =", fractions(P_AUB)))
32 Bcomp=setdiff(S,B)
33 ABunion=union(A,Bcomp)
34 cat("i. AUB' =", ABunion)
35 PABunion=length(ABunion)/length(S)
36 print(paste("i. P(AUB') =", fractions(PABunion)))
37 N=c(2,3,5)
38 PN=length(N)/length(S)
39 cat("j. N =", N)
40 print(paste("j. P(N) =", fractions(PN)))
41 print("k. P(7)=0")

```

---

### R code Exa 3.3 Finding probabilities example3

```

1 #page no :137–138
2 library(MASS)
3 S=data.frame(sex=c('M', 'F'),
4               RH=c(43,44),
5               LH=c(9,4))
6 S$total=S$RH+S$LH
7 View(S)
8 total=sum(S$total)
9 P_M=S$total[1]/total
10 P_F=S$total[2]/total

```

```

11 P_R=sum(S$RH)/total
12 P_L=sum(S$LH)/total
13 table=round(prop.table(S[,2:3]),2)
14 table=as.matrix(table)
15 table
16 RintM=table[1]
17 FintL=table[4]
18 LintF=table[4]
19 MunionF=sum(table)
20 MunionR=table[1]+table[2]+table[3]
21 FunionL=table[3]+table[4]+table[2]
22 csum=apply(table[,1:2],2,sum)
23 rsum=apply(table[,1:2],1,sum)
24 P_Mdash=sum(table)-rsum[1]
25 PRintM=round(RintM/P_M,4)
26 PFintL=round(FintL/P_L,4)
27 PLintF=round(LintF/P_F,4)
28 print(paste(" a. P(M) =",P_M))
29 print(paste(" b. P(F) =",P_F))
30 print(paste(" c. P(R) =",P_R))
31 print(paste(" d. P(L) =",P_L))
32 print(paste(" e. P(M int R) =",RintM))
33 print(paste(" f. P(F int L) =",FintL))
34 print(paste(" g. P(M U F) =",MunionF))
35 print(paste(" h. P(M U R) =",MunionR))
36 print(paste(" i. P(F U L) =",FunionL))
37 print(paste(" j. P(M') =",P_Mdash))
38 print(paste(" k. P(R|M) =",PRintM))
39 print(paste(" l. P(F|L) =",PFintL))
40 print(paste(" m. P(L|F) =",PLintF))

```

---

### R code Exa 3.6 Mutually Exclusive Events of coins

```

1 # page no : 140
2 library(prob)

```

```

3 library(MASS)
4 coin=tosscoin(2)
5 A=subset(coin,toss1=="H" | toss2=="H")
6 P_A=nrow(A)/nrow(coin)
7 print(paste(" one tail =",fractions(P_A)))
8 B=subset(coin,toss1=="T" & toss2=="T")
9 P_B=1-P_A
10 print(paste(" all tail =",fractions(P_B)))
11 C=subset(coin,toss1=="H" & toss2=="H")
12 P_C=nrow(C)/nrow(coin)
13 print(paste(" all heads =",fractions(P_C)))
14 BintC=intersect(B,C)
15 P_BintC=nrow(BintC)/nrow(coin)
16 D=subset(coin,toss1=="T" & toss2=="T")
17 P_D=nrow(D)/nrow(coin)
18 print(paste("more than one tail =",fractions(P_D)))
19 E=subset(coin,toss1=="H" & (toss1=="H" | toss2=="T"))
20 P_E=nrow(E)/nrow(coin)
21 print(paste("head-first roll =",fractions(P_E)))
22 F=subset(coin,toss1=="T" | toss2=="T")
23 P_F=nrow(F)/nrow(coin)
24 print(paste("one tail-two filps =",fractions(P_F)))

```

---

**R code Exa 3.7** Fliping of two coins and finding the probability

```

1 # page no : 141
2 library(prob)
3 library(MASS)
4 coin=tosscoin(2)
5 F=subset(coin,toss1=="T" | toss2=="T")
6 P_F=nrow(F)/nrow(coin)
7 print(paste("a. P(F)=",fractions(P_F)))
8 G=subset(coin,(toss1=="T" & toss2=="T") | (toss1=="H"
    & toss2=="H"))
9 P_G=nrow(G)/nrow(coin)

```

```

10 print(paste("b. P(G) =", fractions(P_G)))
11 H=subset(coin,toss1=="H" & (toss1=="H" | toss2=="T"))
12 P_H=nrow(H)/nrow(coin)
13 print(paste("c.P(H) =", fractions(P_H)))
14 FintG=intersect(F,G)
15 P_FintG=nrow(FintG)/nrow(coin)
16 if(P_FintG==0)
17 {
18   print("d. F,G-mutually exclusive")
19 }else
20 {
21   print("d. F,G-not mutually exclusive")
22 }
23 J=subset(coin,toss1=="T" & toss2=="T")
24 JintH=intersect(J,H)
25 P_JintH=nrow(JintH)/nrow(coin)
26 if(P_JintH==0)
27 {
28   print("e.J,H-mutually exclusive")
29 }else
30 {
31   print("e.J,H-not mutually exclusive")
32 }

```

---

### R code Exa 3.8 Rolling of six sided dice

```

1 # page no : 141–142
2 library(prob)
3 library(MASS)
4 library(sets)
5 S=rolldie(1)
6 A=subset(S,(X1 %% 2 !=0))
7 B=subset(S,(X1 %% 2 ==0))
8 P_A=nrow(A)/nrow(S)
9 print(paste("P(A) =", fractions(P_A)))

```

```

10 P_B=nrow(B)/nrow(S)
11 print(paste("P(B) =", fractions(P_B)))
12 C=subset(S,(X1 %% 2!=0) & (X1>2))
13 D=subset(S,(X1 %% 2==0) & (X1<5))
14 CintD=intersect(C,D)
15 P_CintD=length(CintD)/nrow(S)
16 if(P_CintD==0)
17 {
18   print("C,D-mutually exclusive")
19 }else
20 {
21   print("C,D-not mutually exclusive")
22 }
23 E=subset(S,(X1 < 5))
24 CintE=intersect(C,E)
25 P_CintE=length(CintE)/nrow(S)
26 if(P_CintE==0)
27 {
28   print("C,E-mutually exclusive")
29 }else
30 {
31   print("C,E-not mutually exclusive")
32 }
33 CintA=intersect(C,A)
34 P_CintA=length(CintA)/nrow(S)
35 P_C_A=P_CintA/P_B
36 print(paste(" P(C|A) = ", fractions(P_C_A)))

```

---

### R code Exa 3.9 Mutually Exclusive Events example1

```

1 #page no:142–143
2 P_G=0.6
3 P_H=0.5
4 PGintH=0.3
5 P_G_H=PGintH/P_H

```

```

6 if(P_G_H==P_G)
7 {
8   print(paste("a. P(G|H) = P(G)"))
9 }else
10 {
11   print(paste("a. P(G|H) != P(G)"))
12 }
13 PGH=P_G*P_H
14 if(PGintH==PGH)
15 {
16   print(paste("b. P(G int H) = P(G)P(H)"))
17 }else
18 {
19   print(paste("b. P(G int H) != P(G)P(H)"))
20 }

```

---

### R code Exa 3.10 Mutually Exclusive Events example2

```

1 #page no:143
2 P_C=0.75
3 P_D=0.3
4 P_C_D=0.75
5 PCintD=0.225
6 if(P_C_D==P_C)
7 {
8   print(paste('independent ,P(C|D)=P(C)'))
9 }else
10 {
11   print(paste('dependent P(C|D) !=P(C)'))
12 }
13 if(PCintD==0)
14 {
15   print(paste('mutually exclusive P(C int D)=0'))
16 }else
17 {

```

```

18   print(paste('not mutually exclusive P(C int D) !=0 '
19   ))
20 P_D_C=PCintD/P_C
21 print(paste("c. P(D|C) =", P_D_C))

```

---

**R code Exa 3.11** Drawing of red and blue cards from a box

```

1 # page no : 144
2 library(prob)
3 library(MASS)
4 S<-c('R1', 'R2', 'R3', 'B1', 'B2', 'B3', 'B4', 'B5')
5 R1<-c('R1', 'R2', 'R3')
6 B1<-c('B1', 'B2', 'B3', 'B4', 'B5')
7 E1<-c('R2', 'B2', 'B4')
8 G1<-c('B4', 'B5')
9 H1<-c('B1', 'B2', 'B3', 'B4')
10 P_R=length(R1)/length(S)
11 print(paste("P(R) =", fractions(P_R)))
12 P_B=length(B1)/length(S)
13 print(paste("P(B) =", fractions(P_B)))
14 P_E=length(E1)/length(S)
15 print(paste("P(E) =", fractions(P_E)))
16 EintB=intersect(E1,B1)
17 P_EintB=length(EintB)/length(S)
18 P_E_B=P_EintB/P_B
19 print(paste("The P(E|B) =", fractions(P_E_B)))
20 BintE=intersect(B1,E1)
21 P_BintE=length(BintE)/length(S)
22 P_B_E=P_BintE/P_E
23 print(paste("The P(B|E) =", fractions(P_B_E)))
24 RintB=intersect(R1,B1)
25 P_RintB=length(RintB)/length(S)
26 if(P_RintB==0)
27 {

```

```

28     print("R,B-mutually exclusive")
29 }else
30 {
31     print("R,B-not mutually exclusive")
32 }
33 P_G=length(G1)/length(S)
34 print(paste("P(G)=",fractions(P_G)))
35 P_H=length(H1)/length(S)
36 print(paste("P(H)=",fractions(P_H)))
37 GintH=intersect(G1,H1)
38 P_GintH=length(GintH)/length(S)
39 P_G_H=P_GintH/P_H
40 print(paste("The P(G|H) =",fractions(P_G_H)))
41 if(P_G==P_G_H)
42 {
43     print("G,H-independent")
44 }else
45 { print(" G,H-not independent")
46 }
```

---

### R code Exa 3.12 Mutually Exclusive Events example3

```

1 #page no:145
2 P_F=0.60
3 P_L=0.5
4 PFintL=0.45
5 P_L_F=0.75
6 PFL=P_F*P_L
7 if(PFintL==PFL)
8 {
9     print(paste("a. female ,long hair-independent"))
10 }else
11 {
12     print(paste("a. female ,long hair-dependent"))
13 }
```

```

14 if(P_L_F==P_L)
15 {
16   print(paste("b. female ,long hair-independent"))
17 }else
18 {
19   print(paste("b. female ,long hair-dependent"))
20 }

```

---

### R code Exa 3.13 Tossing of fair coin

```

1 # page no : 145–146
2 library(prob)
3 library(MASS)
4 S=tosscoin(1)
5 cat(paste("a. solution =",S$toss1[1] , "and " ,S$toss1
      [2] ,";" ,nrow(S)))
6 S1=rolldie(1)
7 writeLines("\n b.")
8 print(S1$X1)
9 print(paste("b." ,nrow(S1)))
10 print(paste("c." , nrow(S1)*2))
11 cat(paste("d. ="))
12 count=0
13 for(val1 in 1:nrow(S1))
14 {
15   for(val in 1:nrow(S))
16   {
17     count=count+1
18     cat(paste(S$toss1[val] ,S1$X1[val1]) , " ")
19   }
20 }
21 A=c('H2' , 'H4' , 'H6')
22 P_A=length(A)/count
23 writeLines("\n")
24 print(paste("e. P(A) =" , fractions(P_A)))

```

```

25 B=c( 'H3 ')
26 P_B=length(B)/count
27 print(paste(" f . P(B) =", fractions(P_B)))
28 AintB=intersect(A,B)
29 P_AintB=length(AintB)/count
30 if(P_AintB==0)
31 {
32   print("g . A,B-mutually exclusive")
33 }else
34 {
35   print("g . A,B-not mutually exclusive")
36 }
37 righteq=P_A*P_B
38 lefteq=P_AintB
39
40 if(lefteq==righteq)
41 {
42   print("h . A,B-independent")
43 }else
44 { print("h . A,B-dependent")
45 }

```

---

**R code Exa 3.14** Two basic rules of Probability example1

```

1 #page no:147
2 P_A=0.60
3 P_B=0.35
4 PAintB=0
5 PUB=P_A+P_B
6 PUBcomp=1-PUB
7 print(paste("PUB=",PUB))
8 print(paste("1-PUB =", PUBcomp))

```

---

**R code Exa 3.15** Two basic rules of Probability example2

```
1 #page no:147–148
2 P_A=0.65
3 P_B=0.65
4 P_B_A=0.90
5 PAintB=P_B_A*P_A
6 print(paste("a. solution =",PAintB))
7 PUB=P_A+P_B-PAintB
8 print(paste("b. solution = ",PUB))
9 PBA=P_A*P_B
10 if(PAintB==PBA)
11 {
12   print(paste("c. A,B-independent"))
13 }else
14 {
15   print(paste("c. A,B-not independent"))
16 }
17 if(PAintB==0)
18 {
19   print(paste("d. A,B-mutually exclusive"))
20 }else
21 {
22   print(paste("d. A,B-not mutually exclusive"))
23 }
```

---

**R code Exa 3.16** Two basic rules of Probability example3

```
1 #page no:148–149
2 library(MASS)
3 N=150
4 A_swim=75
5 A_swim1=40
6 I_swim=47
7 I_swim1=30
```

```

8 N_swim=N-(A_swim+I_swim)
9 N_swim1=10
10 P_N_swim=N_swim/N
11 print(paste("a. solution = ",N_swim,"/",N))
12 P_swim_4=(A_swim1+I_swim1+N_swim1)/N
13 print(paste("b. solution = ",A_swim1+I_swim1+N_swim1,
14 ,"/",N))
15 P_A_swim1=A_swim1/N
16 print(paste("c. solution = ",A_swim1,"/",N))
17 PAintI=0
18 PNint4=0.0667
19 if(PAintI==0)
20 {
21   print(paste("d. A and B are mutually exclusive"))
22 }else
23 {
24   print(paste("d. A and B are not mutually exclusive
25 "))
26 if(PNint4==P)
27 {
28   print(paste("e. A And B are independent"))
29 }else
30 {
31   print(paste("e.A And B are not independent"))
32 }

```

---

### R code Exa 3.17 Finding probabilities example4

```

1 #page no: 149
2 P_M=0.2
3 P_S=0.65
4 P_M_S=0.25
5 PMintS=P_M_S*P_S

```

```

6 print(paste("a. solution=",PMintS))
7 PMunionS=P_M+P_S-PMintS
8 print(paste("b. solution=",PMunionS))
9 if(P_M_S==P_M){
10   print("c. M and S are independent")
11 }else
12 {
13   print("c. M and S are not independent")
14 }
15 if(PMintS==0){
16   print("d. M and S are mutually exclusive")
17 }else
18 {
19   print("d. M and S are not mutually exclusive")
20 }

```

---

### R code Exa 3.18 Finding probabilities example5

```

1 #page no:150
2 P_B=14.3/100
3 P_N=85/100
4 P_N_B=2/100
5 PBintN=P_B*P_N_B
6 PBunionN=P_B+P_N-PBintN
7 print(paste(" a. P(B) =",P_B))
8 print(paste(" a. P(N) =",P_N))
9 print(paste(" b. P(N|B) =",P_N_B))
10 print(paste(" c. P(B int N) =",round(PBintN,4)))
11 print(paste(" d. P(B U N) =",round(PBunionN,4)))
12 if(P_N==P_N_B){
13   print("e. B and N are independent")
14 }else
15 {
16   print("e. B and N are not independent")
17 }

```

```

18 if(PBintN==0){
19   print("f. B and N are mutually exclusive")
20 }else{
21 {
22   print("f. B and N are not mutually exclusive")
23 }

```

---

### R code Exa 3.19 Finding probabilities example6

```

1 #page no:151
2 P_B=14.3/100
3 P_N=85/100
4 P_N_B=2/100
5 PBintN=P_B*P_N_B
6 PBunionN=P_B+P_N-PBintN
7 P_P_B=1-P_N_B
8 PBintP=P_P_B*P_B
9 P_Bcomp=1-P_B
10 P_P=1-P_N
11 print(paste(" a. P(P|B) =",P_P_B))
12 print(paste(" b. P(B int P) =",round(PBintP,4)))
13 print(paste(" c. P(B') =",P_Bcomp))
14 print(paste(" d. P(P) =",P_P))

```

---

### R code Exa 3.20 Contingency tables example1

```

1 #page no:152 – 153
2 library(MASS)
3 df=data.frame(violation=c(25,45,70),
4                 noviolation=c(280,405,685),
5                 rtotal=c(305,450,755))
6 rownames(df)=c("cell","nocell","ctotal")
7 View(df)

```

```

8 P_D_C=df$rtotal[1]/df$rtotal[3]
9 P_D_NV=df$noviolation[3]/df$rtotal[3]
10 PNVintC=df$noviolation[1]/df$rtotal[3]
11 e=df$violation[1]/df$violation[3]
12 f=df$noviolation[2]/df$noviolation[3]
13 term1=(df$rtotal[1]/df$rtotal[3])+(df$noviolation[3]
   /df$rtotal[3])
14 term2=(df$noviolation[1]/df$rtotal[3])
15 PC_U_NV=term1-term2
16 print(paste("a.solution=",df$rtotal[1],"/",df$rtotal
   [3]))
17 print(paste("b.solution=",df$noviolation[3],"/",df$rtotal[3]))
18 print(paste("c.solution=",df$noviolation[1],"/",df$rtotal[3]))
19 print(paste("d.solution=",fractions(PC_U_NV)))
20 print(paste("e.solution=",df$violation[1],"/",df$violation[3]))
21 print(paste("f.solution=",df$noviolation[2],"/",df$rtotal[2]))
22 #The answer may vary due to difference in representation.

```

---

### R code Exa 3.21 Contingency tables example2

```

1 #page no:153–155
2 library(MASS)
3 df=data.frame(coast=c(18,16,34),
4               lakes=c(16,25,41),
5               peaks=c(11,14,25),
6               rtotal=c(45,55,100))
7 rownames(df)=c("F","M","ctotal")
8 View(df)
9 PFintC=df$coast[1]/df$rtotal[3]
10 P_F=df$rtotal[1]/df$rtotal[3]

```

```

11 P_C=df$coast [3] /df$rtotal [3]
12 PFC=P_F*P_C
13 print(paste("b.1 P(FintC) =",PFintC))
14 print(paste("b.2 P(F)P(C) =",PFC))
15 if(PFintC==PFC){
16   print("b. F,C-independent")
17 }else
18 {
19   print("b. F,C-not independent")
20 }
21 P_M_L=df[[2]][2]/df$lakes[3]
22 print(paste("c.2 P(M|L)= ",fractions(P_M_L)))
23 P_P=df[[3]][[3]]/df$rtotal[3]
24 print(paste("d.1 P(F)= ",fractions(P_F)))
25 print(paste("d.2 P(P)= ",fractions(P_P)))
26 PFintP=df$peaks[1]/df$rtotal[3]
27 print(paste("d.3 P(F int P)= ",fractions(PFintP)))
28 FUP=(P_F+P_P)-PFintP
29 print(paste("d.4 P(FUP)= ",fractions(FUP)))
30 #The answer may vary due to difference in
   representation.

```

---

### R code Exa 3.22 Contingency tables example4

```

1 #page no:155–156
2 library(MASS)
3 df=data.frame(D1=c(1/15,4/15),
4                 D2=c(1/12,3/12),
5                 D3=c(1/6,1/6))
6 rs <- rowSums(df)
7 df <- cbind(df,rs)
8 cs <- colSums(df)
9 df_s <- sum(df)
10 df <- rbind(df,c(cs,df_s))
11 rownames(df)=c("caught","Ncought","ctotal")

```

```

12 View(df)
13 b=fractions(df$rtotal[2])
14 print(paste("b. solution= ",fractions(b)))
15 P_CD1=df$D1[1]
16 P_CD2=df$D2[1]
17 c = P_CD1 + P_CD2
18 print(paste("c. solution= ",fractions(c)))
19 #The answer provided in the textbook is wrong.

```

---

### R code Exa 3.23 Contingency tables example3

```

1 #page no:156–157
2 library(MASS)
3 df=data.frame(robbery=c(145.7,133.1,119.3,113.7),
4                 burg=c(732.1,717.7,701,702.2),
5                 rape=c(29.7,29.1,27.7,26.8),
6                 vehicle=c(314.7,259.2,239.1,229.6))
7 rownames(df)=c("2008","2009","2010","2011")
8 View(df)
9 df$rtotal=rowSums(df)
10 ctotal<-c(colSums(df[]))
11 total=ctotal[5]
12 P_8=df$rtotal[1]/total
13 P_9=df$rtotal[2]/total
14 P_10=df$rtotal[3]/total
15 P_11=df$rtotal[4]/total
16 P_R=ctotal[1]/total
17 P_B=ctotal[2]/total
18 P_Ra=ctotal[3]/total
19 P_V=ctotal[4]/total
20 P9intR=df$robbery[2]/total
21 P10intB=df$burg[3]/total
22 P11intRa=df$rape[4]/total
23 P8intV=df$vehicle[1]/total
24 P10UB=(P_10+P_B)-P10intB

```

```

25 P11_Ra=P11intRa/P_Ra
26 PV_8=P8intV/P_8
27 print(paste("a.solution=",round(P9intR,4)))
28 print(paste("b.solution=",round(P10intB,4)))
29 print(paste("c.solution=",round(P10UB,4)))
30 print(paste("d.solution=",round(P11_Ra,4)))
31 print(paste("e.solution=",round(PV_8,4)))

```

---

**R code Exa 3.24** drawing of three colored balls from urn

```

1 #page no:157–159
2 library("DiagrammeR")
3 library(data.tree)
4 library("prob")
5 library("dplyr")
6 library("MASS")
7 x<-Node$new(" ")
8     firstdraw_blue<-x$AddChild("8B")
9         seconddraw_blue<-firstdraw_blue$AddChild("8B"
10             )
11             seconddraw_red<-firstdraw_blue$AddChild("3R")
12                 thirddraw_blue<-seconddraw_blue$AddChild(
13                     "64BB")
14                     thirddraw_red<-seconddraw_red$AddChild("24BR")
15                     firstdraw_red<-x$AddChild("3R")
16                         seconddraw_blue<-firstdraw_red$AddChild("8B")
17                             seconddraw_red<-firstdraw_red$AddChild("3R")
18                                 thirddraw_blue<-seconddraw_blue$AddChild(
19                                     "24RB")
20                                     thirddraw_red<-seconddraw_red$AddChild("9RR")
21
22 print(x)
23 plot(x)
24 balls_R <- c(rep("R1",1),rep("R2",1),rep("R3",1))

```

```

21 balls_B <- c(rep("B1",1),rep("B2",1),rep("B3",1),rep(
22   ("B4",1),rep("B5",1),rep("B6",1),rep("B7",1),rep(
23     "B8",1)))
24 apply(as.data.frame(expand.grid(balls_B,balls_R)),1,
25   function(x){paste(x,collapse = "")})
26 M<-unique(urnsamples(balls,size=2,replace=TRUE,
27   ordered=TRUE))
28 N<-probspace(M)
29 P_RR=(3/11)*(3/11)
30 print(paste("b. P(RR)=" ,fractions(P_RR)))
31 P_RB_U_BR=((3/11)*(8/11))+((8/11)*(3/11))
32 print(paste("c. P(RR U BR)=" ,fractions(P_RB_U_BR)))
33 P_R1_int_B2=((3/11)*(8/11))
34 print(paste("d. P(R1 int B2)=" ,fractions(P_R1_int_B2
35   )))
36 P_R2_int_B1=(24/(24+64))
37 print(paste("e. P(R2| B1)=" ,fractions(P_R2_int_B1)))
38 P_BB=64/(64+24+24+9)
39 print(paste("f. P(BB)=" ,fractions(P_BB)))
40 P_B2_int_R1=(24/(9+24))
41 print(paste("g.( B2 | R1)=" ,fractions(P_B2_int_R1)))

```

---

**R code Exa 3.25** drawing of marbles without replacement

```

1 #page no:160–161
2 library(data.tree)
3 library("prob")
4 library("dplyr")
5 library("MASS")
6 x<-Node$new(" ")
7   firstdraw_blue<-x$AddChild("B \n 8/11")
8   seconddraw_blue<-firstdraw_blue$AddChild("B \
9     n 7/10")
10  seconddraw_red<-firstdraw_blue$AddChild("R \n
11    3/10")

```

```

10      thirddraw_blue<-seconddraw_blue$AddChild(
11          "56/110 \n BB")
12      thirddraw_red<-seconddraw_red$AddChild(
13          "24/110 \n BR")
14      firstdraw_red<-x$AddChild("R \n 3/11")
15      seconddraw_blue<-firstdraw_red$AddChild("B \n
16          8/10")
17      seconddraw_red<-firstdraw_red$AddChild("R \n
18          2/10")
19      thirddraw_blue<-seconddraw_blue$AddChild(
20          ("24/110 \n RB"))
21      thirddraw_red<-seconddraw_red$AddChild(
22          "6/110 \n RR")
23
24
25
26
27
28
29
30
31

```

---

**R code Exa 3.26** adoptiong of Tabby kittens and black kittens

```

1 #pageno 162–163
2 library(data.tree)

```

```

3 library("prob")
4 library("dplyr")
5 library("MASS")
6 x<-Node$new(" ")
7     firstdraw_blue<-x$AddChild("T \n 4/9")
8         seconddraw_blue<-firstdraw_blue$AddChild("T \
9             n 3/8")
10        seconddraw_red<-firstdraw_blue$AddChild("B \n
11            5/8")
12            thirddraw_blue<-seconddraw_blue$AddChild(
13                "TT")
14                thirddraw_red<-seconddraw_red$AddChild(
15                    "TB")
16                    firstdraw_red<-x$AddChild("B \n 5/9")
17                     seconddraw_blue<-firstdraw_red$AddChild("T \n
18                         4/8")
19                         seconddraw_red<-firstdraw_red$AddChild("B \n
20                             4/8")
21                             thirddraw_blue<-seconddraw_blue$AddChild(
22                                 ("BT"))
23                                 thirddraw_red<-seconddraw_red$AddChild(
24                                     "BB")

17 print(x)
18 plot(x)
19 P_TT=(4/9)*(3/8)
20 print(paste("a. =",fractions(P_TT)))
21 P_TB=((4/9)*(5/8))+((5/9)*(4/8))
22 print(paste("b. =",fractions(P_TB)))
23 P_BT=(4/8)
24 print(paste("c. =",fractions(P_BT)))
25 P_TT_BB=((4/9)*(3/8))+((5/9)*(4/8))
26 print(paste("d. =",fractions(P_TT_BB)))

```

---

**R code Exa 3.28** drawing venn diagram for flipping of two fair coins

```

1 #page number : 164–165
2 library(RAM)
3 library(VennDiagram)
4 A=c("TT","TH")
5 B=c("TT","HT")
6 AintB=c("TT")
7 AUB=c("TH","TT","HT")
8 X=c("HH","HT","TH","TT")
9 v<-venn.diagram(list(A=A,B=B),
10                  fill=c("orange","blue"),
11                  alpha=c(0.5,0.5),cat.cex=1.5,cex
12                  =1.5,
13                  filename=NULL)
14 grid.newpage()
15 grid.draw(v)
16 lapply(v,names)
17 lapply(v,function(i) i$label)
18 v[[5]]$label<-paste(setdiff(A,B),collapse="\n")
19 v[[6]]$label<-paste(setdiff(B,A),collapse="\n")
20 v[[7]]$label<-paste(intersect(A,B),collapse="\n")
21 grid.newpage()
22 grid.text(x=c(0.5,0),y=c(0.1,0),label=paste(setdiff(
23   X,c(A,B)),collapse=""))
24 grid.draw(v)

```

---

**R code Exa 3.30** Venn diagram for selection of dogs

```

1 #page no:166_167
2 library(eulerr)
3 library(grid)
4 VennDiag <- euler(c("C" = 0.40, "PT" = .50, "C&PT" =
0.05))
5 p1<-plot(VennDiag, counts = TRUE, font=1, cex=1,
alpha=0.5,
6 fill=c("grey","blue","red"))

```

```

7 grid.text("C int PT", x=0.5, y=0.9)
8 gridExtra::grid.arrange(p1)
9 P_C=0.40
10 P_PT=0.50
11 print(paste(" P(C)=",P_C))
12 print(paste(" P(PT)=",P_PT))
13 CintPT=0.05
14 print(paste(" P(C\U2229PT)=",CintPT))
15 C_PT=CintPT/P_PT
16 print(paste("P(C|PT)=",C_PT))
17 CUPT=P_C+P_PT-CintPT
18 print(paste("P(C U PT)=",CUPT))

```

---

**R code Exa 3.31** venn diagram for selection of dogs2

```

1 #page no:168_169
2 library(eulerr)
3 library(grid)
4 VennDiag <- euler(c("Male" = 12, "Female" = 8, "Male
  &Female" = 0.00))
5 p1<-plot(VennDiag, counts = TRUE, font=1, cex=1,
  alpha=0.5,
  fill=c("grey", "blue", "red"))
6 VennDiag <- euler(c("Male" = 12, "Brown" = 10, "Male
  &Brown" = 0.83))
7 p2<-plot(VennDiag, counts = TRUE, font=1, cex=1,
  alpha=0.5,
  fill=c("grey", "blue", "red"))
8 grid.text("10", x=0.5, y=0.5)
9 VennDiag <- euler(c("Female" = 8, "White Fur" = 5, "
  Female&White Fur" = 0.625))
10 p3<-plot(VennDiag, counts = TRUE, font=1, cex=1,
  alpha=0.5,
  fill=c("blue", "white"))
11 gridExtra::grid.arrange(p1,p2,p3)

```

---

**R code Exa 3.32** probability of selecting student as fresher or earning B grade

```
1 #page no:170_172
2 library(eulerr)
3 library(grid)
4 library(multipanelfigure)
5 S=50
6 A=20
7 B=15
8 sopho=30
9 P_A=A/S
10 P_B=B/S
11 P_AintB=(5/S)
12 P_AUB=P_A+P_B-P_AintB
13 VennDiag <- euler(c("A" = A, "B" = B, "A&B" = 0.10))
14 p1<-plot(VennDiag, counts = TRUE, font=1, cex=1,
           alpha=0.5,
           fill=c("grey", "lightgray", "red"))
15 VennDiag <- euler(c("A" = A, "B" = B, "A&B" = 0.10))
16 p2<-plot(VennDiag, counts = TRUE, font=1, cex=1,
           alpha=0.5,
           fill=c("blue", "lightgray", "blue"))
17 VennDiag <- euler(c("A" = A, "B" = B, "A&B" = 0.10))
18 p3<-plot(VennDiag, counts = TRUE, font=1, cex=1,
           alpha=0.5,
           fill=c("lightgray", "blue", "blue"))
19 VennDiag <- euler(c("A" = A, "B" = B, "A&B" = 0.10))
20 p4<-plot(VennDiag, counts = TRUE, font=1, cex=1,
           alpha=0.5,
           fill=c("lightgray", "lightgray", "blue"))
21
22 gridExtra::grid.arrange(p1,p2,p3,p4, nrow=2)
23 grid.text("P(AUB)", x=0.25, y=.95)
```

```

28 grid.text("=", x=0.50, y=.75)
29 grid.text("P(A)", x=0.56, y=.95)
30 grid.text("+", x=0.99, y=.75)
31 grid.text("P(B)", x=0.35, y=.50)
32 grid.text("-", x=0.50, y=.25)
33 grid.text("P(A\u2229B)", x=0.75, y=.50)

```

---

### R code Exa 3.33 Two basic rules of Probability example4

```

1 #page no:172–173
2 library(MASS)
3 df=data.frame(LHG=c(5,8),
4                 HG=c(15,12),
5                 C=c(40,30),
6                 CG=c(60,30))
7 rownames(df)=c("M","F")
8 View(df)
9 df$rtotal=rowSums(df)
10 ctotal<-c(colSums(df[]))
11 total=ctotal[5]
12 PCGintF=df$CG[2]/total
13 P_F=df$rtotal[2]/total
14 P(CG=ctotal[4]/total
15 PCGUf=(P_F+P_CG)-PCGintF
16 PHGintM=df$HG[1]/total
17 P_M=df$rtotal[1]/total
18 P_HG_M=PHGintM/P_M
19 P_HG=ctotal[2]/total
20 LHS1=PCGintF
21 RHS1=P_CG*P_F
22 print(paste("a.solution=", round(PCGintF,2)))
23 print(paste("b.solution=", round(PCGUf,2)))
24 print(paste("c.solution=", round(P_HG_M,3)))
25 if(LHS1!=RHS1)
26 {

```

```
27     print("d. gender and education are not independent  
          ")  
28 }else  
29 {  
30     print("d. gender and education are independent")  
31 }  
32 LHS2=P_HG_M  
33 RHS2=P_HG  
34 if(LHS2 !=RHS2)  
35 {  
36     print("d. gender and education are not independent  
          ")  
37 }else  
38 {  
39     print("d. gender and education are independent")  
40 }
```

---

# Chapter 4

## Discrete Random Variables

R code Exa 4.1 hypergeometric Distribution

```
1 #page no: 206
2 A=30
3 gd=20
4 x=5
5 k=10
6 factorial=function(x)
7 {
8   fact=1
9   for(i in 1:x)
10  {
11    fact=fact*i
12  }
13 return(fact)
14 }
15 binomial=function(a,x)
16 {
17   b=factorial(a)/(factorial(x)*factorial(a-x))
18   return(b)
19 }
20 term1=binomial(A,x)
21 term2=binomial(gd,k-x)
```

```

22 term3=binomial(A+gd,k)
23 num=term1*term2
24 P=num/term3
25 print(paste("1. solution =",round(P,3)))
26 P1=dhyper(x,A,gd,k)
27 print(paste("2. solution(built-in function) =",round(
    P1,3)))

```

---

**R code Exa 4.8** Geometric probability distribution function example1

```

1 #page no: 211–212
2 library(ggplot2)
3 p=0.02
4 x=7
5 P_7=((1-p)^(x-1))*p
6 print(paste("a. P(x=7)=", round(P_7,4)))
7 m=1/p
8 print(paste("mean =", round(m,4)))
9 pp<-0
10 for(i in 1:51)
11 {
12   pp[i]=((1-p)^(i-1))*p
13 }
14 variance=(1/p)*((1/p)-1)
15 sd=sqrt(variance)
16 print(paste("the variance=",variance))
17 print(paste("the sd=",round(sd,1)))
18 x1=seq(1,51,by=1)
19 barplot(pp,names.arg=x1,xlab="x",ylab="P(X=x)")

```

---

**R code Exa 4.9** Geometric probability distribution function example2

```
1 #page no: 212–213
```

```
2 p=1.28/100
3 x=9
4 P_9=((1-p)^x)*p
5 print(paste("a. P(x=9)= ", round(P_9,4)))
6 x=20
7 P_20=((1-p)^(x-1))*p
8 print(paste("b. P(x=20)= ", round(P_20,2)))
9 m=(1-p)/p
10 print(paste("c. mean= ", round(m,2)))
11 sd=sqrt((1-p)/(p^2))
12 print(paste("d sd= ", round(sd,2)))
```

---

**R code Exa 4.10** Geometric probability distribution function example3

```
1 #page no: 213
2 p=0.320
3 x=3
4 P_3=((1-p)^(x-1))*p
5 print(paste("a. P(x=3)= ", round(P_3,4)))
6 m=(1/p)
7 print(paste("c. mean= ", round(m,2)))
```

---

**R code Exa 4.11** Geometric probability distribution function example4

```
1 #page no: 213
2 p=0.80
3 x=3
4 P_3=((1-p)^(x))*p
5 print(paste("a. P(x=3)= ", round(P_3,4)))
```

---

### R code Exa 4.14 Poisson Probability distribution example1

```
1 #page no :215-216
2 library(ggplot2)
3 mu=(1/8)*6
4 x=c(0,1,2,3,4,5)
5 xtot=0
6 p=mu
7 for(i in 1:length(x))
8 {
9   xtot=xtot+ppois(x[i],lambda=mu,lower=FALSE)
10 }
11 y=ppois(1,lambda=mu,lower.tail=FALSE)
12 print(paste('P(x>1)',round(y,4)))
13 pp<-0
14 for(i in 1:6)
15 {
16   pp[i]=dpois(x[i],lambda=mu)
17 }
18 x1=c(0:5)
19 barplot(pp,names.arg=x1,beside=TRUE,xlab="x",ylab="P(X=x)",space=0,ylim=range(pretty(c(0,pp))))
```

---

### R code Exa 4.15 Poisson Probability distribution example2

```
1 #page no :216
2 mu=7
3 e=2.718
4 P_2=dpois(2,lambda=mu)
5 print(paste('P(x=2)',round(P_2,3)))
6 x<-c(0,1,2)
7 y=0
8 for(i in 1:length(x))
9 {
10   y=y+dpois(x[i],lambda=mu)
```

```

11 }
12 print(paste('P(x \u2264 2)', round(y,4)))
13 sd=sqrt(7)
14 print(paste('\u03c3 =', round(sd,2)))

```

---

### R code Exa 4.16 Poisson Probability distribution example3

```

1 #page no :216-217
2 muday=41.5
3 muhour=muday/24
4 e=2.718
5 print(paste('a. solution ',round(muhour,4)))
6 factorial=function(v)
7 {
8   fact=1
9   if(v==0)
10  {
11    return(1)
12  }else{
13    for(i in 1:v)
14    {
15      fact=fact*i
16    }
17    return(fact)
18  }
19 }
20 x=2
21 nu=((muhour^x)*(e^(-muhour)))
22 p2=nu/factorial(x)
23 print(paste('b. P(x=2)',round(p2,3)))
24 x=0
25 nu1=((muhour^x)*(e^(-muhour)))
26 p0=nu1/factorial(x)
27 x=1
28 nu2=((muhour^x)*(e^(-muhour)))

```

```

29 p1=nu2/factorial(x)
30 x=2
31 nu3=((muhour^x)*(e^(-muhour)))
32 p2=nu3/factorial(x)
33 px2=1-(p0+p1+p2)
34 print(paste('c. P(x > 2) ', round(px2,3)))

```

---

### R code Exa 4.17 Poisson Probability distribution example4

```

1 #page no :217
2 mu=200*0.0102
3 e=2.718
4 N=200
5 r=10
6 a=dbinom(10,size=200,prob=.0102)
7 sprintf("a. binomial distribution = %.6f",a)
8 factorial=function(v)
9 {
10   fact=1
11   if(v==0)
12   {
13     return(1)
14   }else{
15     for(i in 1:v)
16     {
17       fact=fact*i
18     }
19     return(fact)
20   }
21 }
22
23 x=10
24 nu=((mu^x)*(e^(-mu)))
25 p2=nu/factorial(x)
26 sprintf('b. poison distribution = %.6f',p2)

```

---

### R code Exa 4.18 Poisson Probability distribution example5

```
1 #page no :217-218
2 size=500
3 prob=0.01
4 mu=size*prob
5 x<-c(0,1,2)
6 binom1=0
7 for(i in 1:length(x))
8 {
9   v1=dbinom(x[i],size,prob)
10  binom1 = binom1 + v1
11  print(paste("binomial distribution P(x=",x[i]," )=",round(v1,5)))
12 }
13 print(paste("binomial distribution P(0,1,2)" ,round(
14   binom1,5)))
14 app1=1-binom1
15 print(paste("binomial solution =" ,round(app1,5)))
16 poisson1=0
17 for(i in 1:length(x))
18 {
19   v2=dpois(x[i],mu)
20   poisson1 = poisson1 +v2
21   print(paste("poisson approx P(x=",x[i]," )=",round(
22     v2,4)))
23   print(paste("poisson approx P(0,1,2)=",round(
24     poisson1,4)))
25 app2=1-poisson1
26 print(paste("poisson solution =" ,round(app2,4)))
```

---

# Chapter 5

## Continuous Random Variables

R code Exa 5.1 Continuous Probability Density functions example1

```
1 #page no: 243–246
2 library(visualize)
3 a=20
4 b=0
5 x<-seq(b,a,by=1)
6 fx1=dunif(x,min=0,max=20)
7 base=(2-0)
8 height=1/20
9 area=base*height
10 p_2=(2-0)*(1/20)
11 print(paste("a. p(0<x<2)=",round(p_2,4)))
12 par(mfcol=c(2,2))
13 visualize.unif(stat=c(0,2),a=0,b=20,section="bounded")
14 base2=15-4
15 area2=base2*height
16 p_15=base2*(1/20)
17 print(paste("b. p(4 < x < 15)=",round(p_15,4)))
18 visualize.unif(stat=c(4,15),a=0,b=20,section="bounded")
19 base3=(12.7-2.3)
```

```

20 p_23_127=base3*height
21 print(paste("b. p(2.3 < x < 12.7)=", round(p_23_
127,4)))
22 visualize.unif(stat=c(2.3,12.7),a=0,b=20,section="
bounded")

```

---

### R code Exa 5.2 Uniform Distribution example1

```

1 #page no: 247–248
2 library(visualize)
3 a=15
4 b=0
5 x<-seq(b,a,by=1)
6 fx1=dunif(x,min=0,max=12.5)
7 p_12=(12.5-0)*(1/15)
8 print(paste("a. p(x<12.5)=", round(p_12,4)))
9 mu=(a+b)/2
10 var=((b-a)^2)/12
11 sd=sqrt(((b-a)^2)/12)
12 print(paste("b. mean =",mu))
13 print(paste("b. sd =",round(sd,1)))
14 k=quantile(x,.90)
15 print(paste("c. 90th percentile =",k))
16 visualize.unif(stat=c(0,12.5),a=0,b=15,section="
bounded")

```

---

### R code Exa 5.3 The Exponential Distribution example1

```

1 #page no:250
2 library(ggplot2)
3 x<-seq(0,20,length.out=100)
4 mu=4
5 e=2.718

```

```

6 m=1/mu
7 px=dexp(x,rate=m)
8 df<-data.frame(x=x,y=px)
9 x=5
10 p_5=(m*(e^(-m*x)))
11 print(paste("a.P>5 =",round(p_5,3)))
12 qplot(x,y,data=df,geom="line")+
13   geom_ribbon(data=subset(df,x>=5),aes(ymax=y),ymin
14     =0,
15       fill="red",colour=NA,alpha=0.5)+
16       scale_x_continuous(labels=as.character(seq(0:20)),
17         breaks=seq(0:20))+  

18       annotate(geom="text",x=4,y=0.25,label=paste("m
19         =0.25"))+
20       labs(x="mu=4", y="f(x)")

```

---

### R code Exa 5.4 The Exponential Distribution example2

```

1 #page no: 251
2 library(ggplot2)
3 e=2.718
4 mu=0.25
5 x<-seq(0,20,length.out=100)
6 px=dexp(x,rate=mu)
7 df<-data.frame(x=x,y=px)
8 x1=5
9 p_5=(1-(e^(-mu*x1)))
10 x2=4
11 p_4=(1-(e^(-mu*x2)))
12 p_4_5=p_5-p_4
13 qplot(x,y,data=df,geom="line")+
14   geom_ribbon(data=subset(df,x>=4 & x<5),aes(ymax=y)
15     ,ymin=0,
16       fill="red",colour=NA,alpha=0.5)+
17       scale_x_continuous("x",labels=as.character(seq

```

```

(0:20)),breaks=seq(0:20))+  

17   annotate(geom="text",x=10,y=0.05,label=paste("P(4<  

      x<5)"))+  

18   labs(y="f(x)")  

19   print(paste("P(x<5) =",round(p_5,4)))  

20   print(paste("P(x<4) =",round(p_4,4)))  

21   print(paste("P(4<x<5) =",round(p_4_5,4)))

```

---

### R code Exa 5.5 The Exponential Distribution example3

```

1 #page no: 251–253  

2 library(ggplot2)  

3 require(gridExtra)  

4 e=2.718  

5 mu=10  

6 m=1/10  

7 x<-seq(0,15,length.out=200)  

8 px=dexp(x,rate=m)  

9 df<-data.frame(x=x,y=px)  

10 x1=7  

11 p_7=(1-(e^(-m*x1)))  

12 p10=(1-p_7)  

13 p1<-qplot(x,y,data=df,geom="line") +  

14   geom_ribbon(data=subset(df,x>=7),aes(ymax=y),ymin  

     =0.02,  

           fill="blue",colour=NA,alpha=0.5)+  

15   scale_x_continuous("x",labels=as.character(seq  

     (0:20)),breaks=seq(0:20))+  

16   annotate(geom="text",x=7,y=0.06,label=paste("P(x  

     >7)"))+  

17   labs(x="mu=10", y="f(x)")  

18   print(paste("P(x<7) =",round(p_7,4)))  

19   print(paste("a. P(x > 7) =",round(p10,4)))  

20   print(paste("b. solution =",5*mu," years"))
21 x2=9

```

```

23 p_9=(1-(e^(-m*x2)))
24 x3=11
25 p_11=(1-(e^(-m*x3)))
26 p_9_11=p_11-p_9
27 print(paste("d. P(9 < x < 11)=", round(p_9_11,4)))
28 p2<-qplot(x,y,data=df,geom="line")+
29   geom_ribbon(data=subset(df,x>=9 & x<=11),aes(ymax=
30     y),ymin=0.02,
31     fill="blue",colour=NA,alpha=0.5)+ 
32   scale_x_continuous("x",labels=as.character(seq
33     (0:20)),breaks=seq(0:20))+ 
34   annotate(geom="text",x=10,y=0.05,label= paste("P(9<
35     x<11)")+
36   labs(x="mu=10", y="f(x)") 
37 grid.arrange(p1,p2,ncol=2)

```

---

### R code Exa 5.6 The Exponential Distribution example4

```

1 #page no : 253
2 library(MASS)
3 m=1/12
4 e=2.718
5 mu=1/m
6 sd=12
7 x=5
8 p_5=(1-(e^(-m*x)))
9 p_gt_5=1-p_5
10 print(paste("a. m =",fractions(m)))
11 print(paste("b. mu =",fractions(mu)))
12 print(paste("c. sigma =",fractions(sd)))
13 print(paste("a. prob. more than 5=",round(p_gt_5,4)))
14 #The answer may slightly vary due to rounding off
values .

```

---

### R code Exa 5.7 The Exponential Distribution example5

```
1 #page no: 253–254
2 library(ggplot2)
3 require(gridExtra)
4 e=2.718
5 avg=30
6 hour=60
7 a=hour/avg
8 print(paste("a. solution=",a," minutes"))
9 b=a*3
10 print(paste("b. solution=",b," minutes"))
11 mu=2
12 m=1/mu
13 x<-seq(0,20,length.out=200)
14 px=dexp(x,rate=m)
15 df<-data.frame(x=x,y=px)
16 x1=1
17 p_1=(1-(e^(-m*x1)))
18 print(paste("c. P(x<1) =",round(p_1,4)))
19 p1<-qplot(x,y,data=df,geom="line")+
20   geom_ribbon(data=subset(df,x<1),aes(ymax=y),ymin
21               =0,
22               fill="red",colour=NA,alpha=0.5)+
22     scale_x_continuous("x",labels=as.character(seq
23       (0:20)),breaks=seq(0:20))+ 
23     annotate(geom="text",x=7,y=0.4,label=paste("P
24       =0.3935"))+
24     labs(y="f(x)") 
25 x2=5
26 p_5=(1-(e^(-m*x2)))
27 p_gt_5=1-p_5
28 print(paste("d. P(x>5)=",round(p_gt_5,4)))
29 p2<-qplot(x,y,data=df,geom="line")+
```

```

30     geom_ribbon(data=subset(df ,x>=5) ,aes(ymax=y) ,ymin
31             =0 ,
32             fill="red" ,colour=NA ,alpha=0.5) +
33             scale_x_continuous("x" ,labels=as.character(seq
34             (0:20)) ,breaks=seq(0:20))+ 
35             annotate(geom="text" ,x=10 ,y=0.1 ,label=paste("P(x
36             >5)=1-P(x<5)") )+
37             labs( y="f(x)" )
38     grid.arrange(p1 ,p2 ,ncol=2)

```

---

### R code Exa 5.8 Exponential probability

```

1 #page no:255
2 library(ggplot2)
3 require(gridExtra)
4 x<-seq(0,20,length.out=100)
5 e=2.718
6 mu=4
7 m=1/mu
8 px=dexp(x,rate=m)
9 df<-data.frame(x=x,y=px)
10 x1=3
11 p_3=1-(e ^(-m*x1))
12 print(paste("P(x<3)=",round(p_3,4)))
13 p_gt_3=1-p_3
14 print(paste("Answer P(x>3)=",round(p_gt_3,4)))
15 p1<-qplot(x,y,data=df,geom="line")+
16     geom_ribbon(data=subset(df ,x>3) ,aes(ymax=y) ,ymin
17             =0 ,
18             fill="red" ,colour=NA ,alpha=0.5) +
19             scale_x_continuous("x" ,labels=as.character(seq
20             (0:20)) ,breaks=seq(0:20))+ 
21             annotate(geom="text" ,x=12 ,y=0.05 ,label=paste("(P
22             >3)=0.4724") )+
23             labs( y="f(x)" )

```

```
21 grid.arrange(p1, ncol=1)
```

---

# Chapter 6

## The Normal Distribution

R code Exa 6.1 The Standard Normal Distribution example1

```
1 #page no: 280–281
2 mu=5
3 sd=6
4 x=17
5 z=(x-mu)/sd
6 if(z>0)
7 {
8 print(paste("x=",x," is to right of mean"))
9 }else{
10   print(paste("x=",x," is to left of mean"))
11 }
12 x=1
13 z=(x-mu)/sd
14 if(z>0)
15 {
16   print(paste("x=",x," is to right of mean"))
17 }else{
18   print(paste("x=",x," is to left of mean"))
19 }
```

---

### R code Exa 6.2 Finding z scores for given mean and standard deviation

```
1 #page no: 281
2 mu=50
3 sd=6
4 x=68
5 x1=mu-sd
6 x2=mu+sd
7 z=(x-mu)/sd
8 z1=(x1-mu)/sd
9 z2=(x2-mu)/sd
10 print(paste("for the x value =",x1, "the z score is
               =",z1))
11 print(paste("for the x value =",x2, "the z score is
               =",z2))
12 sd1=2*sd
13 x3=mu-sd1
14 x4=mu+sd1
15 z3=(x3-mu)/sd
16 z4=(x4-mu)/sd
17 print(paste("for the x value =",x3, "the z score is
               =",z3))
18 print(paste("for the x value =",x4, "the z score is
               =",z4))
19 sd2=3*sd
20 x5=mu-sd2
21 x6=mu+sd2
22 z5=(x5-mu)/sd
23 z6=(x6-mu)/sd
24 print(paste("for the x value =",x5, "the z score is
               =",z5))
25 print(paste("for the x value =",x6, "the z score is
               =",z6))
```

---

### R code Exa 6.3 Using the Normal Distribution example1

```
1 #page no:284–285
2 library(ggplot2)
3 require(gridExtra)
4 x=65
5 mu=63
6 sd=5
7 p65<-pnorm(x,mean=mu,sd=sd)
8 pgt65=1-p65
9 z=(x-mu)/sd
10 p0=pnorm(63,mean=mu,sd=5)
11 p63_65=p65-p0
12 print(paste("a. z1 left area=",round(p63_65,4)))
13 print(paste("a. P(x>65) area=",round(pgt65,4)))
14 xx=seq(0,100,length.out=1000)
15 px=dnorm(xx,mean=mu,sd=sd)
16 df<-data.frame(x=xx,y=px)
17 p1<-qplot(x,y,data=df,geom="line")+
18   geom_ribbon(data=subset(df, x>=65),aes(ymax=y),
19               ymin=0,
20               fill="blue",colour=NA,alpha=0.5)+
21   scale_x_continuous("x",labels=as.character(seq
22     (0:100)),breaks=seq(0:100))+  
23   geom_vline(aes(xintercept=mu),color="blue",
24   linetype="dashed")+
25   annotate("text",x=64,y=0.01,size=3,label="0.1554")+
26   annotate("text",x=80,y=0.01,size=3,label="0.3446")+
27   annotate("text",x=63,y=0.00,size=3,label="mu=63")+
28   annotate("text",x=65,y=0.00,size=3,label="x=65")
29 grid.arrange(p1,ncol=1)
30 x1=85
```

```

28 z1=(x1-mu)/sd
29 if(z1>4.0)
30 {
31   print("b. solution = 1")
32 }

```

---

### R code Exa 6.4 Using the Normal Distribution example2

```

1 #page no:285–287
2 library(ggplot2)
3 require(gridExtra)
4 mu=2
5 sd=0.5
6 x=1.8
7 p18<-pnorm(x,mean=mu,sd=sd)
8 x1=2.75
9 p275<-pnorm(x1,mean=mu,sd=sd)
10 p=p275-p18
11 print(paste("a. P(1.8<=x<=2.75)=",round(p,4)))
12 fz=sd-0.25
13 z=qnorm(0.25)
14 print(paste("a. z score =",round(z,3)))
15 xvalue=(z*sd)+mu
16 print(paste("b. max =",round(xvalue,2)," hours"))
17 xx=seq(0,10,length.out=100)
18 px=dnorm(xx,mean=mu,sd=sd)
19 df<-data.frame(x=xx,y=px)
20 z1=1.8
21 z2=2.75
22 p1<-qplot(x,y,data=df,geom="line")+
23   geom_ribbon(data=subset(df, x>=z1 & x<=z2),aes(
24     ymax=y, ymin=0,
25       fill="blue", colour=NA, alpha=0.5)+
26   scale_x_continuous("x",labels=as.character(seq
27   (0:10)),breaks=seq(0:10))+
```

```

26   geom_vline(aes(xintercept=mu),color="blue",
27   linetype="dashed")+
28   annotate("text",x=2,y=0.00,size=3,label="mu=2")+
29   annotate("text",x=1.8,y=-0.005,size=3,label="1.8")+
30   annotate("text",x=2.75,y=0.00,size=3,label="2.75")+
31 p2<-qplot(x,y,data=df,geom="line")+
32   geom_ribbon(data=subset(df, x<1.66),aes(ymax=y),
33   ymin=0,
34   fill="blue",colour=NA,alpha=0.5)+
35   scale_x_continuous("x",labels=as.character(seq
36   (0:10)),breaks=seq(0:10))+  

37   geom_vline(aes(xintercept=mu),color="blue",
38   linetype="dashed")+
39   annotate("text",x=0.5,y=0.4,size=3,label="P(x<k)
40   =0.25")+
41   annotate("text",x=4,y=0.2,size=3,label="P(x>k)
42   =0.75")
43 grid.arrange(p1,p2,nrow=2)

```

---

### R code Exa 6.5 Using the Normal Distribution example3

```

1 #page no:287
2 library(ggplot2)
3 mu=36.9
4 sd=13.9
5 x1=23
6 p23<-pnorm(x1,mean=mu,sd=sd)
7 x2=64.7
8 p64<-pnorm(x2,mean=mu,sd=sd)
9 p=p64-p23
10 print(paste("a. solution =",round(p,4)))
11 x3=50.8

```

```
12 p508=pnorm(x3,mean=mu,sd=sd)
13 print(paste("b. solution =",round(p508,4)))
```

---

### R code Exa 6.6 Using the Normal Distribution example4

```
1 #page no:288
2 library(ggplot2)
3 mu=5.85
4 sd=0.24
5 x1=6.0
6 p6<-round(pnorm(x1,mean=mu,sd=sd),4)
7 pgt6=1-p6
8 z1=(x1-mu)/sd
9 print(paste("a. P(>=6.0)=",round(pgt6,4)))
10 print(paste("a. Z1=",round(z1,4)))
11 fz_z=0.20/2
12 fz1=0.25
13 fz2=-0.25
14 x2=(fz1*sd)+mu
15 x3=(fz2*sd)+mu
16 print(paste("b. solution = ",x3," and ",x2))
17 xx=seq(0,7,length.out=100)
18 px=dnorm(xx,mean=mu,sd=sd)
19 df<-data.frame(x=xx,y=px)
20 p1<-qplot(x,y,data=df,geom="line")+
21   geom_ribbon(data=subset(df, x>=6.0 & x<=7),aes(
22     ymax=y),ymin=0,
23     fill="blue",colour=NA,alpha=0.5)+
24   scale_x_continuous("x",labels=as.character(seq
25   (0:7)),breaks=seq(0:7))+ 
26   geom_vline(aes(xintercept=mu),color="blue",
27   linetype="dashed")+
28   geom_text(x=7,y=0.5,size=3.5,
29             label=paste0("sd= ",sd))+ 
30   annotate("text",x=5.85,y=-0.05,size=3,label="mu")
```

```

=5.85")+
28   annotate("text",x=6.0,y=-0.05,size=3,label="6.0")
29 grid.arrange(p1,ncol=1)

```

---

### R code Exa 6.7 Finding binomial and normal distribution

```

1 #page no:290-291
2 library(ggplot2)
3 library(gridExtra)
4 mu=10
5 sd=3
6 x=16
7 z=(x-mu)/sd
8 xx=0:100
9 n=100
10 px=dbinom(xx, size=n, prob=0.0228)
11 df<-data.frame(x=xx, y=px)
12 z1=15
13 z2=100
14 p1<-plot(df$x, df$y, type='h', lty=1, lwd=5, xlab="number
    of successes", ylab="P(X)", col=ifelse(df$x<15,
    'grey', 'blue'))
15 x_norm=seq(0:100)
16 p_norm=dnorm(x_norm, mean=mu, sd=sd)
17 df_norm<-data.frame(x=x_norm, y=p_norm)
18 p2<-qplot(x, y, data=df_norm, geom="line")+
19   geom_ribbon(data=subset(df_norm, x>=15), aes(ymax=
    y), ymin=0,
    fill="blue", colour=NA, alpha=0.5)+
20   scale_x_continuous("x", labels=as.character(seq
    (0:100)), breaks=seq(0:100))+ 
21   geom_vline(aes(xintercept=mu), color="blue",
    linetype="dashed")
22 p2
23 x1=16.0

```

```
25 p16<-round(pnorm(x1, mean=mu, sd=sd), 4)
26 pgt16=1-p16
27 print(paste("P(X>16) =", pgt16))
```

---

# Chapter 7

## The Central Limit Theorem

**R code Exa 7.1** Finite Population Correction Factor example1

```
1 #page no: 320–321
2 N=4000
3 n=100
4 sd=10.37
5 mu=75.45
6 differ1=2
7 differ2=-2
8 term1=sd/sqrt(n)
9 term2=sqrt((N-n)/(N-1))
10 denom=term1*term2
11 z=differ1/denom
12 Z1=differ2/denom
13 zscore_r=0.4744
14 fz=zscore_r*differ1
15 print(paste("f(Z) = ", fz))
```

---

**R code Exa 7.2** Finite Population Correction Factor example2

```

1 #page no: 321
2 N=3000
3 n=360
4 p=0.06
5 term1=sqrt((p*(1-p))/n)
6 term2=sqrt((N-n)/(N-1))
7 sdp1=term1*term2
8 p10=10/n
9 p20=20/n
10 znum1=(p10-p)
11 znum2=(p20-p)
12 z10=znum1/sdp1
13 z20=znum2/sdp1
14 zscore10=0.4969
15 zscore20=0.1480
16 ans=zscore10-zscore20
17 print(paste("sigma p' =",round(sdp1,4)))
18 print(paste("P1' =",round(p10,4)))
19 print(paste("P2' =",round(p20,4)))
20 print(paste("Z1' =",round(z10,2)))
21 print(paste("Z2' =",round(z20,2)))
22 print(paste("the solution=",round(ans,4)))

```

---

# Chapter 8

## Confidence Intervals

**R code Exa 8.1** Calculating the Confidence Intervals example1

```
1 #page no:338
2 xbar=68
3 sd=3
4 n=36
5 conf_l=0.90
6 alpha=1-conf_l
7 zalpha=alpha/2
8 arearight=zalpha
9 arealeft=1-zalpha
10 zscore=round(qnorm(arealeft),3)
11 al=(1+conf_l)/2
12 EBM=zscore*(sd/sqrt(n))
13 interval1=xbar-EBM
14 interval2=xbar+EBM
15 print(paste("z score is=",zscore))
16 print(paste("90% confidence interval= (",interval1,
, " ,interval2 ,)" ))
```

---

**R code Exa 8.2** Calculating the Confidence Intervals example2

```

1 #page no:339-340
2 library(ggplot2)
3 xbar=68
4 sd=3
5 n=36
6 conf_l=0.95
7 alpha=1-conf_l
8 x=seq(67,69,length=n)
9 y=dnorm(x,xbar,sd)
10 df=data.frame(x,y)
11 zalpha=alpha/2
12 arearight=zalpha
13 arealeft=1-zalpha
14 zscore=round(qnorm(arealeft),3)
15 al=(1+conf_l)/2
16 EBM=zscore*(sd/sqrt(n))
17 mu1=xbar-EBM
18 mu2=xbar+EBM
19 print(paste("z =",zscore))
20 print(paste("90% interval= (",mu1," , ",mu2,")"))
21 par(mfcol=c(2,1))
22 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
23 abline(v=xbar)
24 abline(v=mu1,lwd=2,col='red')
25 abline(v=mu2,lwd=2,col='red')
26 polygon(c(x[x<=mu1],mu1),c(y[x<=mu1],0),col="red")
27 polygon(c(x[x>=mu2],mu2),c(y[x>=mu2],0),col="red")
28 text(mu1,0.126,"67.02")
29 text(mu2,0.126,"68.98")
30 text(68,0.126,"68")
31 x=seq(-3,3,length=100)
32 y <- dt(x,df=Inf)
33 df=data.frame(x,y)
34 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
35 abline(v=0)
36 abline(v=-1.96,lwd=2,col='red')
37 abline(v=1.96,lwd=2,col='red')
38 polygon(c(x[x<=-1.96],-1.96),c(y[x<=-1.96],0),col="

```

```
    red")
39 polygon(c(x[x>=abs(1.96)],abs(1.96) ),c(y[x>=abs
    (1.96)],0),col="red")
40 text(-1.96,0,-1.96)
41 text(1.96,0,1.96)
42 text(0,0,0)
```

---

### R code Exa 8.3 Calculating the Confidence Intervals example3

```
1 #page no:340-341
2 xbar=68
3 sd=3
4 n=100
5 conf_l=0.90
6 alpha=1-conf_l
7 zalpha=alpha/2
8 arearight=zalpha
9 arealeft=1-zalpha
10 zscore=round(qnorm(arealeft),3)
11 al=(1+conf_l)/2
12 EBM=zscore*(sd/sqrt(n))
13 interval1=xbar-EBM
14 interval2=xbar+EBM
15 print(paste("z score is=",zscore))
16 print(paste("solution A (",interval1," , ",interval2
    ," )"))
17 n=25
18 EBM=zscore*(sd/sqrt(n))
19 interval1=xbar-EBM
20 interval2=xbar+EBM
21 print(paste("Solution B (",interval1," , ",interval2
    ," )"))
```

---

### R code Exa 8.4 Calculating the Confidence Intervals example4

```
1 #page no: 341–342
2 n=80
3 sd=369.34
4 xbar=593.84
5 conf_l=0.92
6 alpha=1-conf_l
7 zalpha=alpha/2
8 arearight=zalpha
9 arealeft=1-zalpha
10 zscore=round(qnorm(arealeft),2)
11 v1=round((zscore*(sd/sqrt(n))),2)
12 mu1=xbar-v1
13 mu2=xbar+v1
14 print(paste("z score =",zscore))
15 print(paste("Answer :(", round(mu1,2), ", ", round(mu2,2), ")"))
16 xseq=seq(mu1,mu2,length=n)
17 d=dnorm(xseq,xbar,sd)
18 par(mfcol=c(2,1))
19 plot(xseq,d,type='l',lwd=3,col='blue',xlab='x')
20 abline(v=xbar)
21 abline(v=mu1,lwd=2,col='red')
22 abline(v=mu2,lwd=2,col='red')
23 text(mu1,0.001060,"521.58")
24 text(mu2,0.001060,"666.10")
25 text(xbar,0.001060,"593.84")
26 x=seq(-3,3,length=100)
27 y <- dt(x,df=Inf)
28 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
29 abline(v=0)
30 abline(v=-1.75,lwd=2,col='red')
31 abline(v=1.75,lwd=2,col='red')
32 polygon(c(x[x<=-1.75],-1.75),c(y[x<=-1.75],0),col="red")
33 polygon(c(x[x>=abs(1.75)],abs(1.75)),c(y[x>=abs(1.75)],0),col="red")
```

```

34 text(-1.75,0,-1.75)
35 text(1.75,0,1.75)
36 text(0,0,0)
37 text(-2.7,0.2,expression(frac(alpha,2)))
38 text(-2.5,0.2,zalpha)
39 text(2.3,0.2,expression(frac(alpha,2)))
40 text(2.5,0.2,zalpha)

```

---

### R code Exa 8.5 Confidence interval for a small sample example1

```

1 #page no: 345–346
2 n=10
3 sd=0.395
4 xbar=1.851
5 conf_l=0.99
6 alpha=1-conf_l
7 zalpha=alpha/2
8 arearight=zalpha
9 arealeft=1-zalpha
10 zscore=round(qnorm(arealeft),2)
11 tscore=round(qt(arealeft,df=9),4)
12 v1=round((tscore*(sd/sqrt(n))),3)
13 mu1=xbar-v1
14 mu2=xbar+v1
15 print(paste("t score is=",tscore))
16 print(paste("Answer : ",round(mu1,3)," \u2264 \u00B5
    \u2264 ", round(mu2,3)))
17 x=seq(-4,4,length=100)
18 y <- dt(x,df=9)
19 prob1=-3.2498
20 par(mfcol=c(1,2))
21 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
22 abline(v=0)
23 abline(v=prob1,lwd=2,col='red')
24 abline(v=abs(prob1),lwd=2,col='red')

```

```

25 polygon(c(x[x<=prob1],prob1),c(y[x<=prob1],0),col="red")
26 polygon(c(x[x>=abs(prob1)],abs(prob1)),c(y[x>=abs(prob1)],0),col="red")
27 text(prob1,0,prob1)
28 text(abs(prob1),0,abs(prob1))
29 text(0,0,round(0,2))
30 x=seq(mu1-2,mu2+2,length=100)
31 y=dnorm(x,xbar,sd)
32 df=data.frame(x,y)
33 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
34 abline(v=xbar)
35 abline(v=mu1,lwd=2,col='red')
36 abline(v=mu2,lwd=2,col='red')
37 polygon(c(x[x<=abs(mu1)],abs(mu1)),c(y[x<=abs(mu1)],0),col="red")
38 polygon(c(x[x>=mu2],mu2),c(y[x>=mu2],0),col="red")
39 text(mu1,0,round(mu1,2))
40 text(mu2,0,round(mu2,2))
41 text(xbar,0,round(xbar,2))

```

---

### R code Exa 8.6 Confidence interval for a population proportion example1

```

1 #page no: 347–348
2 n=500
3 sample_x=421
4 p_dash=sample_x/n
5 q_dash=1-p_dash
6 conf_l=0.95
7 alpha=1-conf_l
8 zalpha=alpha/2
9 arearight=zalpha
10 arealeft=1-zalpha
11 zscore=round(qnorm(arealeft),2)
12 tscore=round(qt(arealeft,df=Inf),4)

```

```

13 v1=(zscore*(sqrt((p_dash*q_dash)/n)))
14 p1=p_dash-v1
15 p2=p_dash+v1
16 print(paste("p' =",p_dash))
17 print(paste("q' =",q_dash))
18 print(paste("z' =",zscore))
19 print(paste(round(p1,3)," \u2264 p \u2264 ",round(p2,3)))
20 print(paste("people -cell phone ", round(p1,3)*100,"%",
    "%," to ", round(p2,3)*100,"%"))

```

---

**R code Exa 8.7** Confidence interval for a population proportion example2

```

1 #page no: 348-349
2 n=150
3 l_limit=0.08
4 u_limit=0.16
5 p_dash=(l_limit+u_limit)/2
6 p=1-p_dash
7 c_interval=u_limit-p_dash
8 v1=sqrt((p_dash*(1-p_dash))/n)
9 zscore=round(c_interval*(1/v1),2)
10 p_zvalue=0.4345
11 p_zvalue1=2*p_zvalue
12 print(paste("p' is=",p_dash))
13 print(paste("z score is=",zscore))
14 print(paste("confidence is ", round(p_zvalue1,3)*
    100,"%"))

```

---

**R code Exa 8.8** Confidence interval for a population proportion example3

```

1 #page no: 349
2 n=500

```

```

3 x=300
4 p_dash=(x/n)
5 q_dash=1-p_dash
6 cl=0.90
7 alpha=1-cl
8 zalpha=alpha/2
9 arearight=zalpha
10 arealeft=1-zalpha
11 zscore=round(qnorm(arealeft),3)
12 v1=round((zscore*(sqrt((p_dash*q_dash)/n))),3)
13 p1=p_dash-v1
14 p2=p_dash+v1
15 print(paste("z score is=",zscore))
16 print(paste("90% confidence :",round(p1,3)," , ",
               round(p2,3)))
17 print(paste("solution : ", round(p1,3)*100,"%"," to "
               , round(p2,3)*100,"%"))

```

---

**R code Exa 8.9** Calculating the sample size n continuous and binary random variables

```

1 #page no 351
2 aer=0.03
3 cl=0.90
4 alpha=1-cl
5 zalpha=alpha/2
6 arearight=zalpha
7 arealeft=1-zalpha
8 zscore=round(qnorm(arealeft),3)
9 p_dash=0.5
10 q_dash=1-p_dash
11 n=((zscore^2)*p_dash*q_dash)/(aer^2)
12 print(paste(" the sample size is = ",round(n,0)))

```

---

# Chapter 9

## Hypothesis Testing with One Sample

**R code Exa 9.8** Full Hypothesis test example1

```
1 #page no 392–394
2 mu0=16.43
3 xbar=16
4 sd=0.8
5 n=15
6 t_stat=(xbar-mu0)/(sd/sqrt(n))
7 alpha=0.05
8 t_c_left=qnorm(alpha)
9 p_value=pnorm(t_stat)
10 print(paste('t static =',round(t_stat,4)))
11 if(t_stat <= t_c_left)
12 {
13   print(paste("left tail : Reject H0"))
14 }else
15 {
16   print(paste("Left tail : Accept H0"))
17 }
18 t_c_right=qnorm(1-alpha)
19 p_value=1-pnorm(t_stat)
```

```

20 if(t_stat >= t_c_right)
21 {
22   print(paste(" right tail : Reject H0"))
23 }else
24 {
25   print(paste(" right tail : Accept H0"))
26 }
27 two_t_stat=abs((xbar-mu0))/(sd/sqrt(n))
28 two_t_critical=qnorm(1-alpha/2)
29 p_value=2*(1-pnorm(two_t_stat))
30 if(two_t_stat>=two_t_critical)
31 {
32   print("reject H0")
33 }else
34 {
35   print("accept H0")
36 }
37 dfs<-n-1
38 x<-seq(-3,3,0.1)
39 y<-dt(x,dfs)
40 t.val<-qt(0.95,df=dfs)
41 p1<-plot(x,y,type='l',lwd=3,col='blue',xlab='x')+
42   abline(v=0)+
43   abline(v=t.val,lwd=2,col="green")+
44   polygon(c(x[x<=-1.76],-2.08),c(y[x
45     <=-1.76],-2.08),col="white")+
46   polygon(c(x[x<=-2.08],-2.08),c(y[x<=-2.08],0),
47     col="blue")+
48   text(t_stat,0,round(t_stat,2))+
49   text(-t.val,0,"-1.76")+
50   text(-2.3,0.1,"alpha=")+
```

---

### R code Exa 9.9 Full Hypothesis test example2

```

1 #page no 395
2 library(ggplot2)
3 mu0=100
4 xbar=108
5 sd=12
6 n=16
7 dfs=n-1
8 t_stat=(xbar-mu0)/(sd/sqrt(n))
9 alpha=0.05
10 t_c_right=abs(qt(1-alpha,df=dfs))
11 p_value=1-pt(t_stat,df=dfs)
12 print(paste("critical value= ",round(t_c_right,3)))
13 print(paste("t-static =",round(t_stat,2)))
14 if(t_stat >= t_c_right)
15 {
16   print(paste("right tail : Reject H0"))
17 }else
18 {
19   print(paste("right tail : Accept H0"))
20 }
21 two_t_stat=abs((xbar-mu0))/(sd/sqrt(n))
22 two_t_critical=qnorm(1-alpha/2)
23 p_value=2*(1-pnorm(two_t_stat))
24 if(two_t_stat>=two_t_critical)
25 {
26   print("reject H0")
27 }else
28 {
29   print("accept H0")
30 }
31 dfs <- n-1
32 x <- seq(-4,4,0.1)
33 y <- dt(x,dfs)
34 t.val <- qt(0.95,df=dfs)
35 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
36 abline(v=0)
37 abline(v=t.val,lwd=2,col='red')
38 abline(v=t_stat,lwd=2,col='green')

```

```

39 polygon(c(x[x>=1.75], 1.75), c(y[x>=1.75], 0), col="red")
40 text(t_stat, 0, round(t_stat, 2))
41 text(t.val, 0, round(t.val, 2))
42 text(3.0, 0.1, "alpha=")
43 text(3.6, 0.1, alpha)

```

---

### R code Exa 9.10 Full Hypothesis test example3

```

1 #page no 396–397
2 library(ggplot2)
3 mu0=8
4 xbar=7.91
5 sv=.03
6 sd=sqrt(sv)
7 n=35
8 df=n-1
9 t_stat=(xbar-mu0)/(sd/sqrt(n))
10 alpha=(1-0.99)/2
11 t_c_left=qt(alpha, df=Inf)
12 p_value=pt(t_stat, df=Inf)
13 print(paste("critical value= ", round(t_c_left, 3)))
14 print(paste("t-static =", round(t_stat, 2)))
15 if(t_stat <= t_c_left)
16 {
17   print(paste("left tail : Reject H0"))
18 }else
19 {
20   print(paste("left tail : Accept H0"))
21 }
22 two_t_stat=abs((xbar-mu0)/(sd/sqrt(n)))
23 two_t_critical=qnorm(1-alpha/2)
24 p_value=2*(1-pnorm(two_t_stat))
25 if(two_t_stat>=two_t_critical)
26 {

```

```

27   print("reject H0")
28 }else
29 {
30   print("accept H0")
31 }
32 x <- seq(-4,4,0.1)
33 y <- dt(x,df=Inf)
34 t.val <- qt(0.95,df=Inf)
35 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
36 abline(v=0)
37 abline(v=t_c_left,lwd=2,col='red')
38 abline(v=t_stat,lwd=2,col='green')
39 abline(v=abs(t_c_left),lwd=2,col='green')
40 polygon(c(x[x>=abs(t_c_left)],abs(t_c_left)),c(y[x
    >=abs(t_c_left)],0),col="red")
41 polygon(c(x[x<=t_c_left],t_c_left),c(y[x<=t_c_left
    ],0),col="red")
42 text(t_c_left,0,round(t_c_left,3))
43 text(t_stat,0,round(t_stat,2))
44 text(abs(t_c_left),0,round(abs(t_c_left),3))
45 text(3.0,0.1,"alpha/2=")
46 text(3.6,0.1,alpha)
47 text(-3.6,0.1,"alpha/2=")
48 text(-3.0,0.1,alpha)

```

---

### R code Exa 9.11 Hypothesis test for proportions example1

```

1 #page no 398–399
2 library(ggplot2)
3 n=100
4 p_dash=53/n
5 p0=50/n
6 q0=1-p0
7 n=100
8 t_stat=(p_dash-p0)/(sqrt((p0*q0)/n))

```

```

9 alpha=((5/n))/2
10 t_c_left=qt(alpha,df=Inf)
11 p_value=pt(t_stat,df=Inf)
12 print(paste("critical value= ",round(t_c_left,2)))
13 print(paste("t-static =",round(t_stat,2)))
14 if(t_stat <= t_c_left)
15 {
16   print(paste("left tail : Reject H0"))
17 }else
18 {
19   print(paste("left tail :Accept H0"))
20 }
21 t_c_right=qnorm(1-alpha)
22 p_value=1-pnorm(t_stat)
23 if(t_stat >= t_c_right)
24 {
25   print(paste("right tail : Reject H0"))
26 }else
27 {
28   print(paste("right tail :Accept H0"))
29 }
30
31 two_t_stat=abs((p_dash-p0))/(sqrt((p0*q0)/n))
32 two_t_critical=qnorm(1-alpha/2)
33 p_value=2*(1-pnorm(two_t_stat))
34 if(two_t_stat>=two_t_critical)
35 {
36   print("reject H0")
37 }else
38 {
39   print("accept H0")
40 }
41 x <- seq(-4,4,0.1)
42 y <- dt(x,df=Inf)
43 t.val <- qt(0.95,df=Inf)
44 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
45 abline(v=0)
46 abline(v=t_c_left,lwd=2,col='red')

```

```

47 abline(v=t_stat, lwd=2, col='green')
48 abline(v=abs(t_c_left), lwd=2, col='green')
49 polygon(c(x[x>=abs(t_c_left)], abs(t_c_left) ), c(y[x
    >=abs(t_c_left)], 0), col="red")
50 polygon(c(x[x<=t_c_left], t_c_left ), c(y[x<=t_c_left
    ], 0), col="red")
51 text(t_c_left, 0, round(t_c_left, 2))
52 text(t_stat, 0, round(t_stat, 2))
53 text(abs(t_c_left), 0, round(abs(t_c_left), 2))
54 text(3.0, 0.1, "alpha/2=")
55 text(3.6, 0.1, alpha)
56 text(-3.6, 0.1, "alpha/2=")
57 text(-3.0, 0.1, alpha)

```

---

### R code Exa 9.12 Hypothesis test for proportions example2

```

1 #page no 400
2 library(ggplot2)
3 n=150
4 x=43
5 p_dash=round(x/n, 3)
6 p0=30/100
7 q0=1-p0
8 t_stat=abs((p_dash-p0)/(sqrt((p0*q0)/n)))
9 alpha=(1-0.90)/2
10 t_c_left=qt(alpha, df=Inf)
11 p_value=pt(t_stat, df=Inf)
12 print(paste("critical value= ", round(t_c_left, 2)))
13 print(paste("t-static =", round(t_stat, 3)))
14 if(t_stat <= t_c_left)
15 {
16   print(paste("left tail : Reject H0"))
17 }else
18 {
19   print(paste("left tail : Accept H0"))

```

```

20  }
21 t_c_right=qnorm(1-alpha)
22 p_value=1-pnorm(t_stat)
23 if(t_stat >= t_c_right)
24 {
25   print(paste("right tail : Reject H0"))
26 }else
27 {
28   print(paste("right tail :Accept H0"))
29 }
30 two_t_stat=abs((p_dash-p0))/(sqrt((p0*q0)/n))
31 two_t_critical=qnorm(1-alpha/2)
32 p_value=2*(1-pnorm(two_t_stat))
33 if(two_t_stat>=two_t_critical)
34 {
35   print("reject H0")
36 }else
37 {
38   print("accept H0")
39 }
40 x <- seq(-4,4,0.1)
41 y <- dt(x,df=Inf)
42 t.val <- qt(0.95,df=Inf)
43 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
44 abline(v=0)
45 abline(v=t_c_left,lwd=2,col='red')
46 abline(v=t_stat,lwd=2,col='green')
47 abline(v=abs(t_c_left),lwd=2,col='green')
48 Polygon(c(x[x>=abs(t_c_left)],abs(t_c_left)),c(y[x>=abs(t_c_left)],0),col="red")
49 Polygon(c(x[x<=t_c_left],t_c_left),c(y[x<=t_c_left],0),col="red")
50 text(t_c_left,0,round(t_c_left,2))
51 text(t_stat,0,round(t_stat,3))
52 text(abs(t_c_left),0,round(abs(t_c_left),2))
53 text(3.0,0.1,"alpha/2=")
54 text(3.6,0.1,alpha)
55 text(-3.6,0.1,"alpha/2=")

```

```
56 text(-3.0,0.1, alpha)
```

---

### R code Exa 9.13 Hypothesis test for proportions example3

```
1 #page no 400–401
2 library(ggplot2)
3 glass=c
  (1.11,1.07,1.11,1.07,1.12,1.08,0.98,0.98,1.02,0.95,0.95)

4 n=length(glass)
5 xbar=mean(glass)
6 sd=sd(glass)
7 mu0=1
8 t_stat=abs((xbar-mu0)/(sd/sqrt(n)))
9 alpha=(1-0.90)/2
10 t_c_left=qt(alpha,df=Inf)
11 p_value=pt(t_stat,df=Inf)
12 print(paste("critical value= ",round(t_c_left,2)))
13 print(paste("t-static =",round(t_stat,2)))
14 t_c_right=qnorm(1-alpha)
15 p_value=1-pnorm(t_stat)
16 if(t_stat >= t_c_right)
17 {
18   print(paste("right tail : Reject H0"))
19 }else
20 {
21   print(paste("right tail : Accept H0"))
22 }
23 two_t_stat=abs((xbar-mu0)/(sd/sqrt(n)))
24 two_t_critical=qnorm(1-alpha/2)
25 p_value=2*(1-pnorm(two_t_stat))
26 if(two_t_stat>=two_t_critical)
27 {
28   print("reject H0")
29 }else
```

```

30  {
31    print(" accept H0")
32  }
33 x <- seq(-4,4,0.1)
34 y <- dt(x,df=Inf)
35 t.val <- qt(0.95,df=Inf)
36 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
37 abline(v=0)
38 abline(v=t_c_left,lwd=2,col='red')
39 abline(v=t_stat,lwd=2,col='green')
40 abline(v=abs(t_c_left),lwd=2,col='green')
41 polygon(c(x[x>=abs(t_c_left)],abs(t_c_left)),c(y[x
        >=abs(t_c_left)],0),col="red")
42 polygon(c(x[x<=t_c_left],t_c_left),c(y[x<=t_c_left
        ],0),col="red")
43 text(t_c_left,0,round(t_c_left,2))
44 text(t_stat,-0.01,round(t_stat,3))
45 text(abs(t_c_left),0,round(abs(t_c_left),2))
46 text(3.0,0.1,"alpha/2=")
47 text(3.6,0.1,alpha)
48 text(-3.6,0.1,"alpha/2=")
49 text(-3.0,0.1,alpha)

```

---

### R code Exa 9.14 Hypothesis test for proportions example4

```

1 #page no 401
2 library(ggplot2)
3 n=420019
4 x=172
5 p_dash=round(x/n,6)
6 p0=.0340/100
7 q0=1-p0
8 t_stat=abs((p_dash-p0)/(sqrt((p0*q0)/n)))
9 alpha=.005
10 t_c_left=(qt(alpha,df=Inf))

```

```

11 p_value=pt(t_stat,df=Inf)
12 print(paste("critical value= ",round(t_c_left,2)))
13 print(paste("t-static =",round(t_stat,2)))
14 if(t_stat <= t_c_left)
15 {
16   print(paste("left tail : Reject H0"))
17 }else
18 {
19   print(paste("left tail :Accept H0"))
20 }
21 t_c_right=qnorm(1-alpha)
22 p_value=1-pnorm(t_stat)
23 if(t_stat >= t_c_right)
24 {
25   print(paste("right tail : Reject H0"))
26 }else
27 {
28   print(paste("right tail :Accept H0"))
29 }
30 two_t_stat=abs((p_dash-p0))/(sqrt((p0*q0)/n))
31 two_t_critical=qnorm(1-alpha/2)
32 p_value=2*(1-pnorm(two_t_stat))
33 if(two_t_stat>=two_t_critical)
34 {
35   print("reject H0")
36 }else
37 {
38   print("accept H0")
39 }
40 x <- seq(-3,3,0.1)
41 y <- dt(x,df=Inf)
42 t.val <- qt(0.95,df=Inf)
43 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
44 abline(v=0)
45 abline(v=t_c_left,lwd=2,col='red')
46 abline(v=t_stat,lwd=2,col='green')
47 abline(v=abs(t_c_left),lwd=2,col='green')
48 polygon(c(x[x>=abs(t_c_left)]),abs(t_c_left)),c(y[x

```

```
>=abs(t_c_left)] ,0) ,col="red")  
49 polygon(c(x[x<=t_c_left],t_c_left) ,c(y[x<=t_c_left]  
] ,0) ,col="red")  
50 text(t_c_left,0,round(t_c_left,2))  
51 text(t_stat,0.05,round(t_stat,3))  
52 text(abs(t_c_left),0,round(abs(t_c_left),2))  
53 text(-3.0,0.1,"alpha/2=")  
54 text(-2.8,0.1,alpha)  
55 text(2.6,0.1,"alpha/2=")  
56 text(2.8,0.1,alpha)
```

---

# Chapter 10

## Hypothesis Testing with Two Samples

**R code Exa 10.1** Comparing two independent population means example1

```
1 #page no 422–424
2 library(ggplot2)
3 library(MASS)
4 s1=0.866
5 s2=1.00
6 n1=9
7 n2=16
8 numerator=((s1)^2/n1)+((s2)^2/n2))^2
9 deno1=(1/(n1-1))*(((s1^2)/n1))^2
10 deno2=(1/(n2-1))*(((s2^2)/n2))^2
11 df=round(numerator/(deno1+deno2),0)
12 xbar1=2
13 xbar2=3.2
14 diffmu=0
15 num3=round((xbar1-xbar2)-diffmu,3)
16 term1=round((s1^2)/n1,3)
17 term2=round((s2^2)/n2,3)
18 deno3=round(sqrt(term1+term2),3)
19 t_stat=num3/deno3
```

```

20 alpha=.05
21 twotail_alpha=alpha/2
22 t_c_left=qt(twotail_alpha,df=df)
23 p_value=pnorm(t_stat)
24 if(t_stat <= t_c_left)
25 {
26   print(paste(" left tail : Reject H0"))
27 }else
28 {
29   print(paste(" Left tail : Accept H0"))
30 }
31 two_t_stat=abs(t_stat)
32 two_t_critical=qt(twotail_alpha,df=df)
33 p_value=2*(1-pnorm(two_t_stat))
34 if(two_t_stat>=two_t_critical)
35 {
36   print(" reject H0")
37 }else
38 {
39   print(" accept H0")
40 }
41 dfs <- df
42 x <- seq(-4,4,0.1)
43 y <- dt(x,dfs)
44 t.val <- qt(0.025,df=dfs)
45 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
46 abline(v=0)
47 abline(v=t.val,lwd=2,col='red')
48 abline(v=t_stat,lwd=2,col='green')
49 polygon(c(x[x>=abs(t_c_left)],abs(t_c_left)),c(y[x
  >=abs(t_c_left)],0),col="red")
50 polygon(c(x[x<=t_c_left],t_c_left),c(y[x<=t_c_left
  ],0),col="red")
51 text(t_c_left,0,round(t_c_left,2))
52 text(t_stat,0,round(t_stat,2))
53 text(abs(t_c_left),0,round(abs(t_c_left),2))
54 text(3.0,0.1,expression(frac(alpha,2)))
55 text(3.6,0.1,alpha/2)

```

```

56 text(-3.6,0.1,expression(frac(alpha,2)))
57 text(-3.0,0.1,alpha/2)
58 #The answer may slightly vary due to rounding off
  values

```

---

**R code Exa 10.2** Comparing two independent population means example2

```

1 #page no 425–426
2 library(ggplot2)
3 s1=1.5
4 n1=11
5 xbar1=4
6 s2=1
7 n2=9
8 xbar2=3.5
9 diffmu=0
10 num3=round((xbar1-xbar2)-diffmu,3)
11 term1=round((s1^2)/n1,3)
12 term2=round((s2^2)/n2,3)
13 deno3=round(sqrt(term1+term2),3)
14 t_stat=num3/deno3
15 alpha=.01
16 df=10
17 t_c_right=qt(1-alpha,df=df)
18 p_value=1-pt(t_stat,df=df)
19 print(paste(" critical value= ",round(t_c_right,3)))
20 print(paste("g. t-static =",round(t_stat,2)))
21 if(t_stat >= t_c_right)
22 {
23   print(paste(" right tail : Reject H0"))
24 } else
25 {
26   print(paste(" right tail : Accept H0"))
27 }
28 dfs <- df

```

```

29 x <- seq(-4,4,0.1)
30 y <- dt(x,dfs)
31 t.val <- qt(1-alpha,df=dfs)
32 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
33 abline(v=0)
34 abline(v=t.val,lwd=2,col='red')
35 abline(v=t_stat,lwd=2,col='green')
36 polygon(c(x[x>=abs(t_c_right)],abs(t_c_right)),c(y[
  x>=abs(t_c_right)],0),col="red")
37 text(t_c_right,0,round(t_c_right,2))
38 text(t_stat,0,round(t_stat,2))
39 text(abs(t_c_right),0,round(abs(t_c_right),2))
40 text(3.0,0.1,expression(alpha))
41 text(3.6,0.1,alpha)
42 text(-3.6,0.1,expression(alpha))
43 text(-3.0,0.1,alpha)

```

---

### R code Exa 10.3 Comparing two independent population means example3

```

1 #page no 426–427
2 library(ggplot2)
3 s1=16
4 n1=35
5 xbar1=74
6 s2=9
7 n2=40
8 xbar2=76
9 diffmu=0
10 num3=round((xbar1-xbar2)-diffmu,3)
11 term1=round((s1^2)/n1,3)
12 term2=round((s2^2)/n2,3)
13 deno3=round(sqrt(term1+term2),3)
14 t_stat=num3/deno3
15 print(paste("t-static =",round(t_stat,2)))
16 alpha=0.05

```

```

17 twotail_alpha=alpha/2
18 df=n1+n2-2
19 two_t_stat=abs(num3)/deno3
20 two_t_critical=qnorm(1-twotail_alpha)
21 p_value=2*(1-pnorm(t_stat))
22 if(two_t_stat>=two_t_critical)
23 {
24   print("Reject H0")
25 }else
26 {
27   print("Accept H0")
28 }
29 dfs <- df
30 x <- seq(-4,4,0.1)
31 y <- dt(x,dfs)
32 t.val <- qt(1-alpha,df=dfs)
33 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
34 abline(v=0)
35 abline(v=t.val,lwd=2,col='red')
36 abline(v=t_stat,lwd=2,col='green')
37 abline(v=two_t_critical,lwd=2,col='green')
38 polygon(c(x[x>=abs(two_t_critical)]),abs(two_t_
    critical),c(y[x>=abs(two_t_critical)],0),col="
    red")
39 text(two_t_critical,0,round(two_t_critical,2))
40 text(t_stat,0,round(t_stat,2))
41 text(abs(two_t_critical),0,round(abs(two_t_critical)
    ,2))
42 text(3.0,0.1,expression(frac(alpha,2)))
43 text(3.6,0.1,twotail_alpha)
44 text(-3.6,0.1,expression(frac(alpha,2)))
45 text(-3.0,0.1,twotail_alpha)

```

---

**R code Exa 10.4** Cohens standards for small medium and large effect sizes

```

1 #page no : 428
2 xbar1=4
3 s1=1.5
4 n1=11
5 xbar2=3.5
6 s2=1
7 n2=9
8 small=0.2
9 medium=0.5
10 large=0.8
11 num1=xbar1-xbar2
12 s_pool=sqrt(((n1-1)*s1^2)+((n2-1)*s2^2))/(n1+n2-2)
13 cohend=(num1/s_pool)
14 if((cohend>=small) & (cohend<=medium))
15 {
16   print(paste("small-size =",round(cohend,3)))
17 }
18 if((cohend>=medium) & (cohend<=large))
19 {
20   print(paste("medium-size =",round(cohend,3)))
21 }
22 if(cohend>=large)
23 {
24   print(paste("large-size is =",round(cohend,3)))
25 }

```

---

### R code Exa 10.5 Test for differences in means

```

1 #page no : 428-429
2 xbar1=8
3 s1=5.4
4 n1=18
5 xbar2=4
6 s2=2.4
7 n2=11

```

```

8 alpha=0.05
9 num1=xbar1-xbar2
10 term1=((n1-1)*s1^2)+((n2-1)*s2^2)/(n1+n2-2)
11 term2=(1/n1)+(1/n2)
12 df=n1+n2-2
13 t_stat=num1/sqrt(term1*term2)
14 t_critical=qt(alpha,df)
15 print(paste("t-static =",round(t_stat,2)))
16 print(paste("t-alpha =",df))
17 if(t_stat>t_critical)
18 {
19     print("Reject H0")
20 }else
21 {
22     print("Accept H0")
23 }

```

---

**R code Exa 10.6** Comparing two independent population proportions example1

```

1 #page no : 431-432
2 xa=20
3 xb=12
4 na=200
5 nb=200
6 pc=round(((xa+xb)/(na+nb)),3)
7 p=1-pc
8 print(paste('1-pc =',p))
9 p_dash_a=xa/na
10 p_dash_b=xb/nb
11 ediff=p_dash_a-p_dash_b
12 print(paste('P\A =',p_dash_a))
13 print(paste('P\B =',p_dash_b))
14 print(paste('P\A - P\B =',ediff))
15 deno1=(pc*p*((1/na)+(1/nb)))

```

```

16 t_stat=(ediff/sqrt(deno1))
17 print(paste('Zc =', round(t_stat,3)))
18 alpha=.1/2
19 df=na+nb-2
20 t_critical=qnorm(1-alpha)
21 if(t_stat>t_critical)
22 {
23   print(" Reject H0")
24 }else
25 {
26   print(" Accept H0")
27 }
28 dfs <- na+nb-2
29 x <- seq(-4,4,0.1)
30 y <- dt(x,dfs)
31 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
32 abline(v=0)
33 abline(v=t_critical,lwd=2,col='red')
34 abline(v=t_stat,lwd=2,col='green')
35 polygon(c(x[x>=abs(t_critical)],abs(t_critical)),c(
36   y[x>=abs(t_critical)],0),col="red")
37 text(t_critical,0,round(t_critical,2))
38 text(t_stat,0,round(t_stat,2))
39 text(abs(t_critical),0,round(abs(t_critical),2))
40 text(3.0,0.1,expression(frac(alpha,2)))
41 text(3.6,0.1,alpha)
42 text(-3.6,0.1,expression(frac(alpha,2)))
43 text(-3.0,0.1,alpha)
44 #The answer provided in the textbook is wrong

```

---

**R code Exa 10.7** Two population means with known standard deviations  
example1

```

1 #page no : 433–434
2 x1=3

```

```

3 x2=2.9
4 psd1=0.33
5 psd2=0.36
6 n=20
7 mdiff=x1-x2
8 sd=sqrt((psd1^2/n)+(psd2^2/n))
9 t_stat=(mdiff/sd)
10 print(paste("mean diff= ",x1-x2))
11 print(paste("t stat= ",round(t_stat,1)))
12 alpha=.05
13 df=n+n-2
14 t_critical=round(qnorm(1-alpha),3)
15 print(paste("t critical= ",t_critical))
16 if(t_stat>t_critical)
17 {
18     print("Reject H0")
19 }else
20 {
21     print("Accept H0")
22 }
23 dfs <- n+n-2
24 x <- seq(-4,4,0.1)
25 y <- dt(x,dfs)
26 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
27 abline(v=0)
28 abline(v=t_critical,lwd=2,col='red')
29 abline(v=mdiff,lwd=2,col='green')
30 polygon(c(x[x>=abs(t_critical)],abs(t_critical)),c(
    y[x>=abs(t_critical)],0),col="red")
31 text(t_critical,0,round(t_critical,2))
32 text(mdiff,0,round(mdiff,2))
33 text(abs(t_critical),0,round(abs(t_critical),2))
34 text(3.0,0.1,expression(alpha))
35 text(3.6,0.1,alpha)
36 text(-3.6,0.1,expression(alpha))
37 text(-3.0,0.1,alpha)
38 #The answer provided in the textbook is wrong

```

---

**R code Exa 10.8** Two population means with known standard deviations  
example2

```
1 #page no : 434-435
2 x1=61.675
3 x2=61.704
4 psd1=10.17
5 psd2=9.55
6 n1=30
7 n2=30
8 mdiff=abs(x1-x2)
9 sd=sqrt((psd1^2/60)+(psd2^2/60))
10 t_stat=((mdiff/sd))
11 alpha=.05
12 t_critical=qnorm(1-alpha)
13 print(paste("t critical=",round(t_critical,2)))
14 p_value=pnorm(t_stat)
15 if(t_stat>t_critical)
16 {
17     print("Reject H0")
18 }else
19 {
20     print("Accept H0")
21 }
22 if(alpha>p_value)
23 {
24     print("Reject H0")
25 }else
26 {
27     print("Accept H0")
28 }
29 df s <- n1+n2-2
30 x <- seq(-3,3,0.01)
31 y <- dt(x,df s)
```

```

32 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
33 abline(v=0)
34 abline(v=round(t_stat,2),lwd=2,col='green')
35 polygon(c(x[x>=abs(t_critical)],abs(t_critical)),c(
36     y[x>=abs(t_critical)],0),col="red")
37 text(t_stat,0,round(t_stat,2))
38 text(2.0,0.1,expression(alpha))
39 text(2.3,0.1,alpha)
40 text(-2.6,0.1,expression(alpha))
41 text(-2.0,0.1,alpha)
41 #The answer may slightly vary due to rounding off
values.

```

---

### R code Exa 10.9 Matched or Paired Samples

```

1 #page no : 436–437
2 xd=23.9
3 mud=20.4
4 sd=3.8
5 n=20
6 t_stat=round(((xd-mud)-0)/(sd/sqrt(n)),2)
7 alpha=0.1
8 t_critical1=qt(alpha/2,df=n-2)
9 t_critical2=qt(1-alpha/2,df=n-2)
10 p_value=pnorm(t_stat)
11 print(paste("t_static=",t_stat))
12 print(paste("t_critical1=",round(t_critical1,3)))
13 print(paste("t_critical2=",round(t_critical2,3)))
14 if(t_stat>t_critical2)
15 {
16     print("Reject H0")
17 }else
18 {
19     print("Accept H0")
20 }

```

```

21  dfs <- n-2
22  x <- seq(-5,5,0.1)
23  y <- dt(x,dfs)
24  plot(x,y,type='l',lwd=3,col='blue',xlab='x')
25  abline(v=0)
26  abline(v=t_critical2,lwd=2,col='red')
27  abline(v=t_stat,lwd=2,col='green')
28  polygon(c(x[x>=abs(t_critical2)],abs(t_critical2)), 
29            c(y[x>=abs(t_critical2)],0),col="red"))
30  text(t_critical2,0,round(t_critical2,2))
31  text(t_stat,0,round(t_stat,2))
32  text(abs(t_critical2),0,round(abs(t_critical2),2))
33  text(3.0,0.1,expression(alpha))
34  text(3.6,0.1,alpha)
35  text(-3.6,0.1,expression(alpha))
36  text(-3.0,0.1,alpha)

```

---

### R code Exa 10.10 Matched or Paired Samples example2

```

1 #page no : 437-439
2 study<-data.frame(subject=c('A','B','C','D','E','F',
3                           'G','H'),
4                     before=c
5                           (6.6,6.5,9.0,10.3,11.3,8.1,6.3,11.6)
6                           ,
7                     after=c
8                           (6.8,2.4,7.4,8.5,8.1,6.1,3.4,2.0)
9                           )
10 study$diff=study$after-study$before
11 xbar=round(mean(study$diff),3)
12 study$dbarsq=(study$diff-xbar)^2
13 View(study)
14 n=8
15 sumxbar=round(sum(study$dbarsq),2)
16 s=round(sqrt(sumxbar/(n-1)),2)

```

```

12 SE=round(s/sqrt(n),2)
13 df=n-1
14 t_stat=round((xbar-0)/SE,2)
15 alpha=0.05
16 t_critical=qt(alpha,df=n-1)
17 p_value=pnorm(t_stat)
18 if(t_stat<t_critical)
19 {
20   print("Reject H0")
21 }else
22 {
23   print("Accept H0")
24 }
25 dfs <- n-1
26 x <- seq(-5,5,0.1)
27 y <- dt(x,dfs)
28 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
29 abline(v=0)
30 abline(v=t_critical,lwd=2,col='red')
31 abline(v=xbar,lwd=2,col='green')
32 polygon(c(x[x<=t_critical],t_critical),c(y[x<=t_
    critical],0),col="red")
33 text(t_critical,0,round(t_critical,2))
34 text(xbar,0,round(xbar,2))
35 text(3.0,0.1,expression(alpha))
36 text(3.6,0.1,alpha)
37 text(-3.6,0.1,expression(alpha))
38 text(-3.0,0.1,alpha)
39 #The answer may slightly vary due to rounding off
  values.

```

---

### R code Exa 10.11 Matched or Paired Samples example3

```

1 #page no : 439–440
2 w_lift<-data.frame(weight=c("play1","play2","play3",

```

```

" play4") ,
3                         before=c(205,241,338,368) ,
4                         after=c(295,252,330,360))
5 w_lift$diff=w_lift$after-w_lift$before
6 xbar=round(mean(w_lift$diff),3)
7 w_lift$dbarsq=(w_lift$diff-xbar)^2
8 View(w_lift)
9 n=4
10 sumxbar=round(sum(w_lift$dbarsq),2)
11 s=round(sqrt(sumxbar/(n-1)),2)
12 SE=round(s/sqrt(n),2)
13 df=n-1
14 t_stat=round((xbar-0)/SE,2)
15 alpha=0.05
16 t_critical=qt(1-alpha,df=n-1)
17 print(paste("t critical=",round(t_critical,3)))
18 print(paste("t static=",round(t_stat,3)))
19 p_value=pnorm(t_stat)
20 if(t_stat>t_critical)
21 {
22   print("Reject H0")
23 }else
24 {
25   print("Accept H0")
26 }
27 dfs <- n-1
28 x <- seq(-5,5,0.1)
29 y <- dt(x,dfs)
30 plot(x,y,type='l',lwd=3,col='blue',xlab='x')
31 abline(v=0)
32 abline(v=t_critical,lwd=2,col='red')
33 abline(v=t_stat,lwd=2,col='green')
34 polygon(c(x[x>=t_critical],t_critical),c(y[x>=t_
critical],0),col="red")
35 text(t_critical,0,round(t_critical,2))
36 text(t_stat,0,round(t_stat,2))
37 text(3.0,0.1,expression(alpha))
38 text(3.6,0.1,alpha)

```

```
39 text(-3.6,0.1,expression(alpha))  
40 text(-3.0,0.1,alpha)
```

---

# Chapter 11

## The Chi Square Distribution

R code Exa 11.2 Test of single variance example1

```
1 #page no : 467–468
2 library(ggplot2)
3 library(MASS)
4 options(scipen=999)
5 n=25
6 df=n-1
7 sigma=7.2
8 s_mean=3.5
9 t_stat=round(((n-1)*(s_mean)^2)/(sigma)^2,2)
10 alpha=0.05
11 p=round(pchisq(t_stat,df,lower.tail=TRUE),6)
12 print(paste0(" df=",df))
13 print(paste0(" tstatic=",t_stat))
14 if(alpha > p)
15 {
16   print(paste(" left tail : Reject H0"))
17 }else
18 {
19   print(paste(" Left tail : Accept H0"))
20 }
21 t_critical=13.85
```

```

22 curve(dchisq(x, df=df), from=0, to=100,
23         ylab=" density",
24         lwd=2,
25         col='steelblue')
26 x<-seq(0,100)
27 y<-dchisq(x, df=df)
28 abline(v=0)
29 abline(v=t_stat, lwd=2, col='green')
30 polygon(c(x[x<=abs(t_critical)], abs(t_critical) ), c(
31   y[x<=abs(t_critical)], 0), col="red")
32 text(t_stat, 0, round(t_stat, 2))
33 text(abs(t_critical), 0, round(abs(t_critical), 2))
34 text(60, 0.04, expression(alpha))
35 text(65, 0.04, alpha)
36 mtext(expression(chi^2), side=1, at=5.67, cex=1)

```

---

### R code Exa 11.3 Test of single variance example2

```

1 #page no : 469
2 library(ggplot2)
3 library(MASS)
4 options(scipen=999)
5 n=24
6 df=n-1
7 sigma=0.2
8 s_mean=.11
9 t_stat_num=(n-1)*(s_mean)^2
10 t_stat_deno=sigma*sigma
11 t_stat=round(t_stat_num/t_stat_deno ,2)
12 alpha=0.025
13 p=round(pchisq(t_stat ,df) ,6)
14 print(paste0(" t static=",t_stat))
15 print(paste0("P( t static)=",p))
16 if(alpha > p)
17 {

```

```

18   print(paste(" left tail : Reject H0"))
19 }else
20 {
21   print(paste(" Left tail : Accept H0"))
22 }
23 t_critical1=round(qchisq(alpha,df),2)
24 t_critical2=round(qchisq(1-alpha,df),2)
25 if((t_stat<=t_critical1) & (t_stat>=t_critical2))
26 {
27   print("Accept H0")
28 }else
29 {
30   print("Reject H0")
31 }
32 curve(dchisq(x,df=df),from=0,to=100,
33        ylab="density",
34        lwd=2,
35        col='steelblue')
36 x<-seq(0,100)
37 y<-dchisq(x,df=df)
38 abline(v=0)
39 abline(v=t_stat,lwd=2,col='red')
40 abline(v=t_stat,lwd=2,col='green')
41 polygon(c(x[x<=abs(t_critical1)],abs(t_critical1)),
42           c(y[x<=abs(t_critical1)],0),col="red")
42 polygon(c(x[x>=abs(t_critical2)],abs(t_critical2)),
43           c(y[x>=abs(t_critical2)],0),col="red")
43 text(t_stat,0,round(t_stat,2))
44 text(t_critical1,0,t_critical1)
45 text(t_critical2,0,t_critical2)
46 text(60,0.04,expression(frac(alpha, 2)))
47 text(65,0.04,alpha)
48 mtext(expression(chi^2),side=1,at=t_stat,cex=1)
49 #The answer provided in the textbook is wrong.

```

---

### R code Exa 11.4 Goodness of Fit test example1

```
1 #apge no: 470-471
2 students<-data.frame(lterm=c(0,3,6,9),
3                         uterm=c(2,5,8,12),
4                         E=c(50,30,12,8),
5                         O=c(35,40,20,5))
6 View(students)
7 no=nrow(students)
8 df=no-1
9 print(paste("b. df =",df))
```

---

### R code Exa 11.5 Goodness of Fit test example2

```
1 #apge no: 472-473
2 emp<-data.frame(E=c(12,12,12,12,12),
3                    O=c(15,12,9,9,15))
4 emp$OE=emp$O-emp$E
5 emp$OEsq=emp$OE^2
6 emp$OE2=emp$OEsq/emp$E
7 View(emp)
8 no=nrow(emp)
9 t_stat=sum(emp$OE2)
10 df=no-1
11 print(paste(" df =",df))
12 print(paste(" t stat =",t_stat))
13 alpha=0.05
14 t_critical=qchisq(1-alpha,df=no-1)
15 if(t_stat<=t_critical)
16 {
17   print("Accept H0")
18 }else
19 {
20   print("Reject H0")
21 }
```

```

22 curve(dchisq(x, df=df), from=0, to=15,
23         ylab=" density",
24         lwd=2,
25         col='steelblue')
26 x<-seq(0,15,0.1)
27 y<-dchisq(x, df=df)
28 abline(v=0)
29 abline(v=t_stat, lwd=2, col='green')
30 polygon(c(x[x>=t_critical], t_critical ), c(y[x>=t_
    critical], 0), col="red")
31 text(t_stat, 0, round(t_stat, 2))
32 text(t_critical, 0, round(t_critical, 2))
33 text(60, 0.04, expression(alpha))
34 text(65, 0.04, alpha)
35 mtext(expression(chi^2), side=1, at=3, cex=1)

```

---

### R code Exa 11.6 Goodness of Fit test example3

```

1 #apge no: 474-476
2 tv<-data.frame(no_TV=c(0,1,2,3,4),
3                   E=c(60,96,330,66,48),
4                   O=c(66,119,340,60,15))
5 tv$OE=tv$O-tv$E
6 tv$OEsq=tv$OE^2
7 tv$OE2=tv$OEsq/tv$E
8 View(tv)
9 no=nrow(tv)
10 t_stat=sum(tv$OE2)
11 df=no-1
12 print(paste("df =", df))
13 print(paste("t statistic =", round(t_stat, 2)))
14 alpha=0.01
15 t_critical=qchisq(1-alpha, df=no-1)
16 print(paste("critical value =", round(t_critical, 3)))
17 if(t_stat<=t_critical)

```

```

18 {
19   print("Accept H0")
20 }else
21 {
22   print("Reject H0")
23 }
24 curve(dchisq(x,df=df),from=0,to=35,
25        ylab="density",
26        lwd=2,
27        col='steelblue')
28 x<-seq(0,35,0.1)
29 y<-dchisq(x,df=df)
30 abline(v=0)
31 abline(v=t_critical,lwd=2,col='red')
32 abline(v=t_stat,lwd=2,col='green')
33 polygon(c(x[x>=t_critical],t_critical),c(y[x>=t_
critical],0),col="blue")
34 text(20,0.05,expression(alpha ==0.01))
35 mtext(expression(chi^2),side=1,at=t_stat,cex=1)
36 mtext(round(t_stat,2),side=1,at=t_stat+2,cex=1)
37 mtext(round(t_critical,2),side=1,at=t_critical,cex
=1)

```

---

### R code Exa 11.7 Goodness of Fit test example4

```

1 #apge no: 476-477
2 library(GetoptLong)
3 coin<-data.frame(no_coin=c(0,1,2),
4                    E=c(25,50,25),
5                    O=c(20,57,23))
6 coin$OE=coin$O-coin$E
7 coin$OEsq=coin$OE^2
8 coin$OE2=coin$OEsq/coin$E
9 View(coin)
10 no=nrow(coin)

```

```

11 t_stat=sum(coin$OE2)
12 chisquare=t_stat
13 df=no-1
14 print(paste("df =",df))
15 print(paste("chi square =",chisquare))
16 alpha=0.05
17 t_critical=qchisq(1-alpha,df=no-1)
18 if(t_stat<=t_critical)
19 {
20   print("Accept H0")
21 }else
22 {
23   print("Reject H0")
24 }
25 x<-seq(0,15,length=100)
26 curve(dchisq(x,df=df),from=0,to=15,n=10000,
27        ylab="density",
28        lwd=2,
29        col='steelblue')
30 y<-dchisq(x,df=df)
31 abline(v=0)
32 abline(v=t_critical,lwd=2,col='red')
33 abline(v=t_stat,lwd=2,col='green')
34 polygon(c(x[x>=t_critical],t_critical),c(y[x>=t_
critical],0),col="blue")
35 text(10,0.3,expression(alpha ==0.05))
36 mtext((expression(chi^2==2.14)),side=1,at=t_stat,cex
      =1)
37 mtext(round(t_critical,2),side=1,at=t_critical,cex
      =1)

```

---

### R code Exa 11.8 Goodness of Fit test example5

```

1 #page no: 478
2 library(GetoptLong)

```

```

3 A=70
4 B=305
5 total_pop=755
6 P_A=A/total_pop
7 P_B=B/total_pop
8 P_A_int_B=P_A*P_B
9 y=P_A_int_B*total_pop
10 print(paste("answer =", round(y,digits=1)))

```

---

### R code Exa 11.9 Test of Independence example1

```

1 #apge no: 479-480
2 library(MASS)
3 obs_matrix<-matrix(c(111,96,91,96,133,150,48,61,53),
4 ncol=3)
5 rownames(obs_matrix)<-c("comm_stud","four_y_stud",
6 "non_stud")
7 colnames(obs_matrix)<-c('hours13','hours46','hours79')
8 exp_matrix<-matrix(
9   (90.57,103.00,104.42,115.19,131.00,132.81,49.24,56.00,56.77),
10  ncol=3)
11 rownames(exp_matrix)<-c("comm_stud","four_y_stud",
12 "non_stud")
13 colnames(exp_matrix)<-c('hours13','hours46','hours79')
14 no_r=nrow(obs_matrix)
15 no_c=ncol(obs_matrix)
16 df=(no_r-1)*(no_c-1)
17 t_stat=0
18 for(i in 1:dim(obs_matrix)[1])
19 {
20   for(j in 1:dim(obs_matrix)[2])
21   {
22     x=(obs_matrix[i,j]-exp_matrix[i,j])^2/exp_

```

```

          matrix[i,j]
18      t_stat=t_stat+x
19  }
20 }
21 print(paste(" critical value" ,round(t_stat,2)))
22 print(paste(" df =" ,df))
23 alpha=0.05
24 t_critical=qchisq(1-alpha ,df=df)
25 if(t_stat<=t_critical)
26 {
27   print("Accept H0")
28 }else
29 {
30   print("Reject H0")
31 }
32 x<-seq(0,15 ,length=100)
33 curve(dchisq(x ,df=df) ,from=0 ,to=15 ,
34        ylab=" density",
35        lwd=2 ,
36        col='steelblue')
37 y<-dchisq(x ,df=df)
38 abline(v=0)
39 abline(v=t_critical ,lwd=2 ,col='red')
40 abline(v=t_stat ,lwd=2 ,col='green')
41 polygon(c(x[x>=t_critical] ,t_critical ) ,c(y[x>=t_
    critical] ,0) ,col="blue")
42 text(10 ,0.1 ,expression(alpha ==0.05))
43 mtext((expression(chi^2==12.99)) ,side=1 ,at=t_stat ,
    cex=1)
44 mtext(round(t_critical ,2) ,side=1 ,at=t_critical ,cex
    =1)

```

---

### R code Exa 11.10 Test of Independence example2

1 #apge no: 481–482

```

2 library(MASS)
3 obs_matrix<-matrix(c
4   (35,18,4,42,48,5,53,63,11,15,33,15,10,31,17),ncol
5   =5)
6 rownames(obs_matrix)<-c("high","medium","low")
7 colnames(obs_matrix)<-c('high_anx','med_hig_anx',
8   'med_anx','med_low_anx','low_anx')
9 View(obs_matrix)
10 H_Sum=0
11 for(i in 1:dim(obs_matrix)[1])
12 {
13   j=1
14   H_Sum=H_Sum+obs_matrix[i,j]
15 }
16 H_A_sum=0
17 for(j in 1:dim(obs_matrix)[2])
18 {
19   i=1
20   H_A_sum=H_A_sum+obs_matrix[i,j]
21 }
22 total=0
23 for(i in 1:dim(obs_matrix)[1])
24 {
25   for(j in 1:dim(obs_matrix)[2])
26   {
27     total=total+obs_matrix[i,j]
28   }
29 }
30 E1=(H_Sum*H_A_sum)/total
31 print(paste("a. solution : ", round(E1,2)))
32 L_Sum=0
33 for(i in 1:dim(obs_matrix)[1])
34 {
35   j=4
36   L_Sum=L_Sum+obs_matrix[i,j]
37 }
38 M_L_A_Sum=0
39 for(j in 1:dim(obs_matrix)[2])

```

```

37 {
38   i=3
39   M_L_A_Sum=M_L_A_Sum+obs_matrix[i,j]
40 }
41 E2=(L_Sum*M_L_A_Sum)/total
42 print(paste("b. solution : ", total))
43 print(paste("c. solution : ", round(E2,2)))
44 print(paste("d. solution : ", round(E2,0)))

```

---

### R code Exa 11.11 Test of Homogeneity

```

1 #page no: 483–484
2 library(MASS)
3 obs_matrix<-matrix(c(72,91,84,86,49,88,45,35),ncol=4)
4 rownames(obs_matrix)<-c("males","females")
5 colnames(obs_matrix)<-c('dormitory','apart',,
  withparents','other')
6 View(obs_matrix)
7 obs_table<-as.table(obs_matrix)
8 View(obs_table)
9 x=chisq.test(obs_table)
10 t_stat=x$statistic
11 df=x$parameter
12 print(paste("\u03c7 = ",round(t_stat,2)))
13 print(paste("df =",df))
14 alpha=0.05
15 t_critical=round(qchisq(1-alpha,df=df),3)
16 if(t_stat<=t_critical)
17 {
18   print("Accept H0")
19 }else
20 {
21   print("Reject H0")
22 }

```

```
23 print(paste(" critical value ",t_critical))
24 x<-seq(0,15,length=100)
25 curve(dchisq(x,df=df),from=0,to=15,
26         ylab=" density",
27         lwd=2,
28         col='steelblue')
29 y<-dchisq(x,df=df)
30 abline(v=0)
31 abline(v=t_critical,lwd=2,col='red')
32 abline(v=t_stat,lwd=2,col='green')
33 polygon(c(x[x>=t_critical],t_critical ),c(y[x>=t_
critical],0),col="blue")
34 text(10,0.1,expression(alpha ==0.05))
35 mtext(expression(chi^2==10.13)),side=1,at=t_stat,
cex=1)
36 mtext(t_critical,side=1,at=t_critical,cex=1)
```

---

# Chapter 12

## F Distribution and one way ANOVA

R code Exa 12.1 Test of two variances

```
1 #page no: 515–516
2 library(MASS)
3 n1=10
4 n2=10
5 s1sq=52.3
6 s2sq=89.9
7 f_stat=round((s2sq)/(s1sq),3)
8 alpha=0.01
9 df1=n1-1
10 df2=n2-1
11 t_critical=round(qf(1-alpha,df1=df1,df2=df2),3)
12 if(f_stat<=t_critical)
13 {
14   print("Accept H0")
15 }else
16 {
17   print("Reject H0")
18 }
19 print(paste("the critical value ",t_critical))
```

```

20 print(paste("the f-static ",f_stat))
21 x<-seq(0,10,length=100)
22 curve(df(x,df1=df1,df2=df2),from=0,to=10,
23         ylab="density",
24         lwd=2,
25         col='steelblue')
26 y<-df(x,df1=df1,df2=df2)
27 abline(v=0)
28 abline(v=t_critical,lwd=2,col='red')
29 abline(v=f_stat,lwd=2,col='green')
30 polygon(c(x[x>=t_critical],t_critical ),c(y[x>=t_
critical],0),col="blue")
31 text(9,0.1,expression(alpha ==0.01))
32 mtext(expression(F[c]==1.719)),side=1,at=f_stat,cex
=1)
33 mtext(round(t_critical,2),side=1,at=t_critical,cex
=1)

```

---

### R code Exa 12.2 The F distribution and the F Ratio example1

```

1 #page no : 519-521
2 plan1<-c(5,4.5,4,3)
3 plan2<-c(3.5,7,4.5)
4 plan3<-c(8,4,3.5)
5 plan4<-c(plan1,plan2,plan3)
6 n<-c(length(plan1),length(plan2),length(plan3))
7 s<-c(sum(plan1),sum(plan2),sum(plan3))
8 term1=0
9 term2=0
10 n_sum=0
11 n_count=length(n)
12 for(i in 1:n_count)
13 {
14   term1=term1+(s[i]^2)/n[i]
15   term2=term2+s[i]

```

```

16     n_sum=n_sum+n[i]
17 }
18 ss_between=term1-((term2)^2/n_sum)
19 t_term1=0
20 t_term2=0
21 for(i in 1:length(plan4))
22 {
23 t_term1=t_term1+plan4[i]^2
24 t_term2=t_term2+plan4[i]
25 }
26 s_total=t_term1-((t_term2)^2/n_sum)
27 ss_within=s_total-ss_between
28 df_between=n_count-1
29 df_within=n_sum-n_count
30 df=n_sum-1
31 ms_between=ss_between/df_between
32 ms_within=ss_within/df_within
33 f_stat=ms_between/ms_within
34 print(paste("ss_between= ",round(ss_between,4)))
35 print(paste("ss_within= ",round(ss_within,4)))
36 print(paste("ss_total= ",round(s_total,1)))
37 print(paste("ms_between= ",round(ms_between,4)))
38 print(paste("ms_within= ",round(ms_within,4)))
39 print(paste("f_stat= ",round(f_stat,4)))

```

---

### R code Exa 12.3 The F distribution and the F Ratio example2

```

1 #page no : 521-522
2 v1<-c(2625,2997,4915)
3 v2<-c(5348,5682,5482)
4 v3<-c(6583,8560,3830)
5 v4<-c(7285,6897,9230)
6 v5<-c( 6277,7818,8677)
7 v6<-c(v1,v2,v3,v4,v5)
8 n<-c(length(v1),length(v2),length(v3),length(v4),

```

```

        length(v5))
9 s<-c(sum(v1),sum(v2),sum(v3),sum(v4),sum(v5))
10 term1=0
11 term2=0
12 n_sum=0
13 n_count=length(n)
14 for(i in 1:n_count)
15 {
16   term1=term1+(s[i]^2)/n[i]
17   term2=term2+s[i]
18   n_sum=n_sum+n[i]
19 }
20 ss_between=term1-((term2)^2/n_sum)
21 t_term1=0
22 t_term2=0
23 for(i in 1:length(v6))
24 {
25   t_term1=t_term1+v6[i]^2
26   t_term2=t_term2+v6[i]
27 }
28 s_total=t_term1-((t_term2)^2/n_sum)
29 ss_within=s_total-ss_between
30 df_between=n_count-1
31 df_within=n_sum-n_count
32 df=n_sum-1
33 ms_between=ss_between/df_between
34 ms_within=ss_within/df_within
35 f_stat=ms_between/ms_within
36 print(paste("ss_b=",round(ss_between,0)))
37 print(paste("ss_w=",round(ss_within,0)))
38 print(paste("ss_t=",round(s_total,0)))
39 print(paste("ms_b=",round(ms_between,0)))
40 print(paste("ms_w=",round(ms_within,1)))
41 print(paste("f_stat=",round(f_stat,4)))
42 alpha=0.05
43 df1=df_between
44 df2=df_within
45 p_value=round(pf(f_stat,df1=df1,df2=df2,lower.tail=

```

```

        FALSE) ,4)
46 print(paste("P(F>4.481)= ",p_value))
47 if(f_stat<=p_value)
48 {
49   print("Accept H0")
50 }else
51 {
52   print("Reject H0")
53 }
54 if(alpha<=p_value)
55 {
56   print("Accept H0")
57 }else
58 {
59   print("Reject H0")
60 }
61 x<-seq(0,5,length=100)
62 curve(df(x,df1=df1,df2=df2),from=0,to=5,
63        ylab=" density",
64        lwd=2,
65        col='steelblue')
66 y<-df(x,df1=df1,df2=df2)
67 abline(v=0)
68 abline(v=f_stat,lwd=2,col='green')
69 text(4,0.1,expression(alpha ==0.05))
70 mtext((expression(F==4.481)),side=1,at=f_stat,cex=1)

```

---

#### R code Exa 12.4 The F distribution and the F Ratio example3

```

1 #page no : 523–525
2 v1<-c(2.17,1.85,2.83,1.69,3.33)
3 v2<-c(2.63,1.77,3.25,1.86,2.21)
4 v3<-c(2.63,3.78,4.00,2.55,2.45)
5 v4<-c(3.79,3.45,3.08,2.26,3.18)
6 v5<-c(v1,v2,v3,v4)

```

```

7 n<-c(length(v1),length(v2),length(v3),length(v4))
8 s<-c(sum(v1),sum(v2),sum(v3),sum(v4))
9 term1=0
10 term2=0
11 n_sum=0
12 n_count=length(n)
13 for(i in 1:n_count)
14 {
15   term1=term1+(s[i]^2)/n[i]
16   term2=term2+s[i]
17   n_sum=n_sum+n[i]
18 }
19 ss_between=term1-((term2)^2/n_sum)
20 t_term1=0
21 t_term2=0
22 for(i in 1:length(v5))
23 {
24   t_term1=t_term1+v5[i]^2
25   t_term2=t_term2+v5[i]
26 }
27 s_total=t_term1-((t_term2)^2/n_sum)
28 ss_within=s_total-ss_between
29 df_between=n_count-1
30 df_within=n_sum-n_count
31 df=n_sum-1
32 ms_between=ss_between/df_between
33 ms_within=ss_within/df_within
34 f_stat=ms_between/ms_within
35 print(paste("ss_b= ",round(ss_between,0)))
36 print(paste("ss_w= ",round(ss_within,0)))
37 print(paste("ss_t= ",round(s_total,0)))
38 print(paste("ms_b= ",round(ms_between,0)))
39 print(paste("ms_w= ",round(ms_within,1)))
40 print(paste("f_stat= ",round(f_stat,2)))
41 alpha=0.01
42 df1=df_between
43 df2=df_within
44 p_value=round(pf(f_stat,df1=df1,df2=df2,lower.tail=

```

```

        FALSE) ,4)
45 print(paste("P(F>2.23) = ",round(p_value,4)))
46 if(alpha<=p_value)
47 {
48   print("Accept H0")
49 }else
50 {
51   print("Reject H0")
52 }
53 x<-seq(0,5,length=100)
54 curve(df(x,df1=df1,df2=df2),from=0,to=5,
55        ylab=" density",
56        lwd=2,
57        col='steelblue')
58 y<-df(x,df1=df1,df2=df2)
59 abline(v=0)
60 abline(v=f_stat,lwd=2,col='green')
61 polygon(c(x[x>=f_stat],f_stat),c(y[x>=f_stat],0),
62           col="blue")
63 text(4,0.1,expression(italic(p) ==0.1241))
64 mtext((expression(F==2.23)),side=1,at=f_stat,cex=1)

```

---

### R code Exa 12.5 The F distribution and the F Ratio example4

```

1 #page no : 525-526
2 v1<-c(24,21,23,30,23)
3 v2<-c(25,31,23,20,28)
4 v3<-c(23,27,22,30,20)
5 v4<-c(v1,v2,v3)
6 n<-c(length(v1),length(v2),length(v3))
7 s<-c(sum(v1),sum(v2),sum(v3))
8 n_group=length(n)
9 SM_v1=mean(v1)
10 SM_v2=mean(v2)
11 SM_v3=mean(v3)

```

```

12 SV_v1=var(v1)
13 SV_v2=var(v2)
14 SV_v3=var(v3)
15 v5=c(SM_v1,SM_v2,SM_v3)
16 VG_Means=var(v5)
17 n=length(v1)
18 ms_between=n*VG_Means
19 v6=c(SV_v1,SV_v2,SV_v3)
20 s_pooled=mean(v6)
21 ms_within=s_pooled
22 f_stat=round(ms_between/ms_within,3)
23 df_num=n_group-1
24 df_deno=length(v4)-n_group
25 print(paste("variance= ",round(VG_Means,3)))
26 print(paste("mean = ",round(s_pooled,3)))
27 print(paste("ms_b= ",round(ms_between,3)))
28 print(paste("ms_w= ",round(ms_within,3)))
29 print(paste("f_stat= ",round(f_stat,4)))
30 alpha=0.03
31 df1=df_num
32 df2=df_deno
33 p_value=round(pf(f_stat,df1=df1,df2=df2,lower.tail=
    FALSE),4)
34 print(paste("P(F>0.134) = ",round(p_value,4)))
35 if(alpha<=p_value)
36 {
37   print("Accept H0")
38 }else
39 {
40   print("Reject H0")
41 }

```

---

# Chapter 13

## Linear Regression and Correlation

**R code Exa 13.2** Linear Equations example1

```
1 #page no : 556
2 x<-seq(-5,20,length=100)
3 y=-1+2*x
4 plot(x,y,type="l",ylab="y=-1+2x")
```

---

**R code Exa 13.5** The Regression Equations example1

```
1 #page no: 571
2 x<-c(65,67,71,71,66,75,67,70,71,69,69)
3 y<-c(175,133,185,163,126,198,153,163,159,151,159)
4 plot(x,y,xlab="3rd exam",ylab="final exam")
```

---

**R code Exa 13.6** The Regression Equations example2

```
1 #page no: 576
2 x<-c(65,67,71,71,66,75,67,70,71,69,69)
3 y<-c(175,133,185,163,126,198,153,163,159,151,159)
4 ypredict=lm(y~x,data=faithful)
5 coeffs=coefficients(ypredict)
6 score1=66
7 eq1=round(coeffs[1],2)+round(coeffs[2],2)*score1
8 print(paste("a. solution =",eq1))
9 score2=90
10 eq2=round(coeffs[1],2)+round(coeffs[2],2)*score2
11 print(paste("b. solution =",eq2))
```

---